

Do we need a new cosmological model ?

GMO-CLONES, a solution to the precision era dilemma

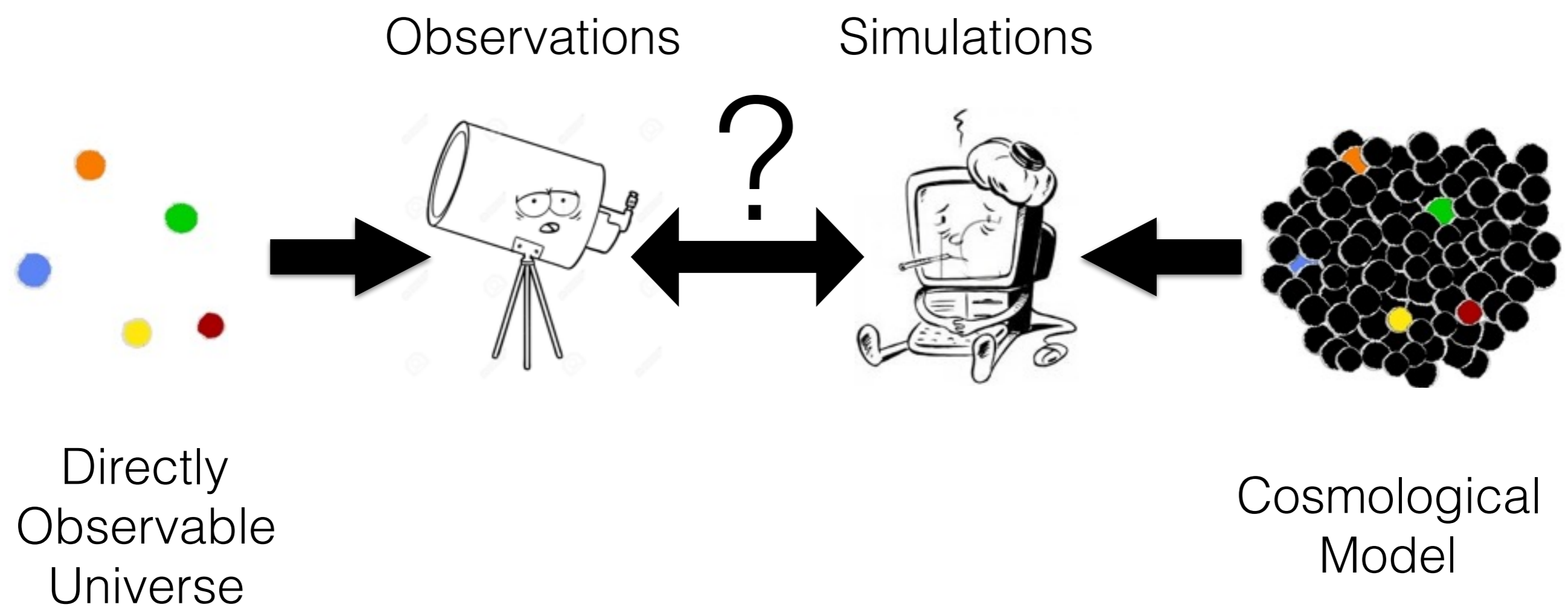


Jenny Sorce

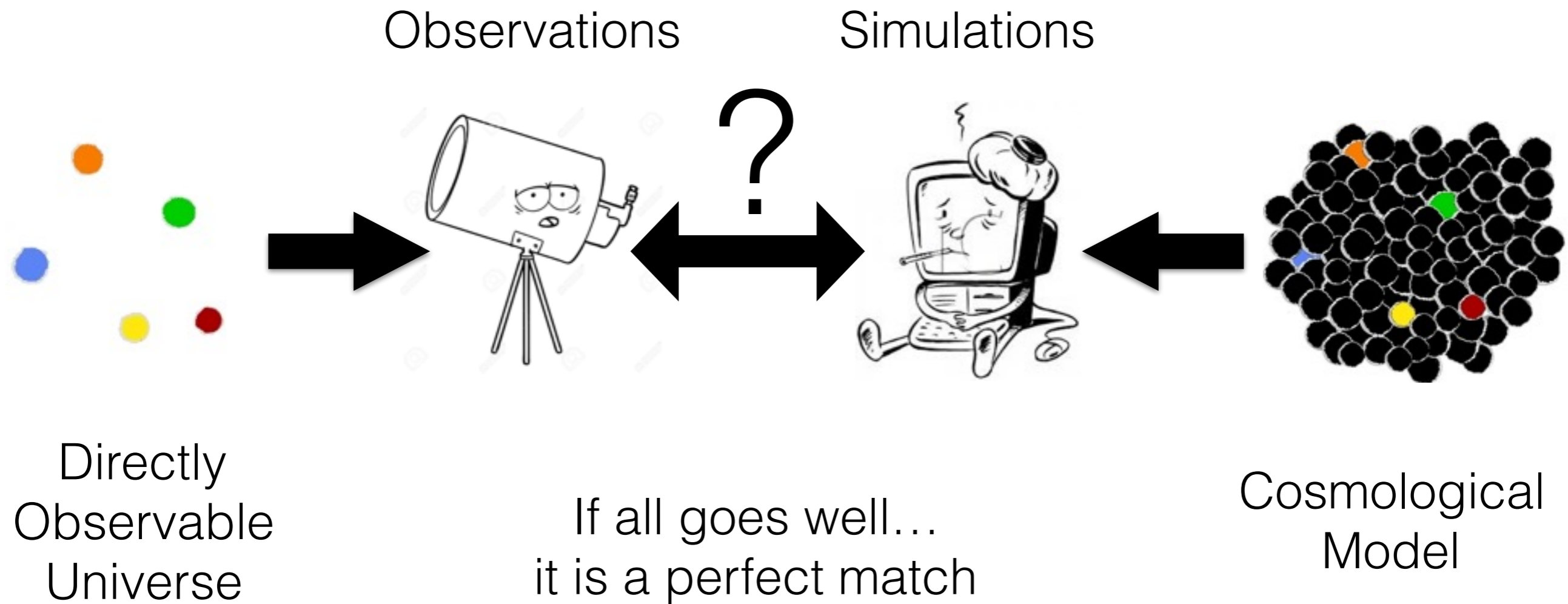
Centre de Recherche Astrophysique de Lyon
OCA - Nice, January 29th 2019

Collaborators: Blaizot, Richard, Tresse (CRAL), Dubois (IAP), Hahn (OCA),
de La Torre (LAM), Pontzen, Peiris, Rey (UCL), Ocvirk (ObAS)

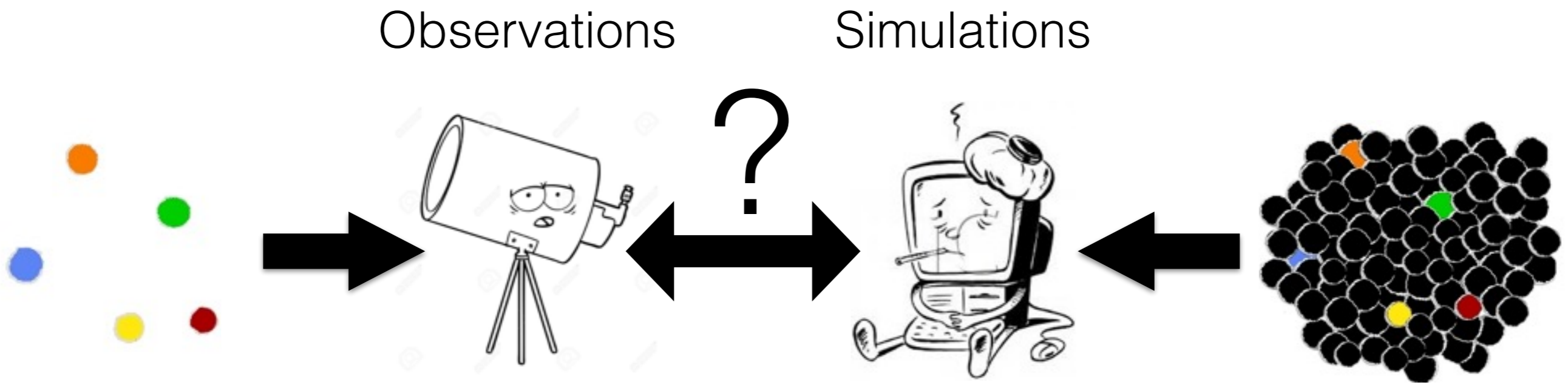
Motivation : Λ CDM? \blacktriangleright Current strategy



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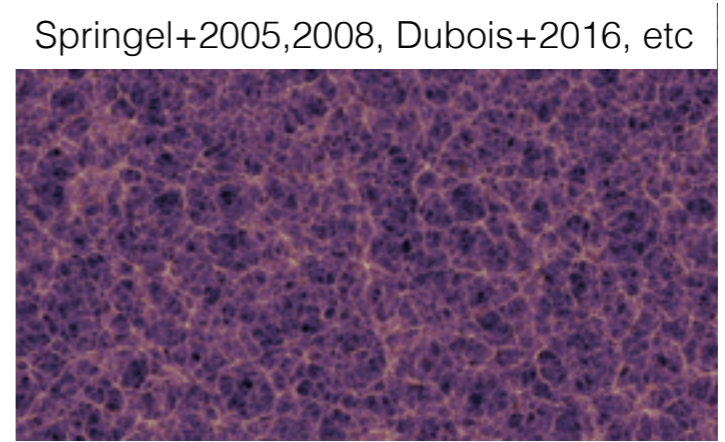
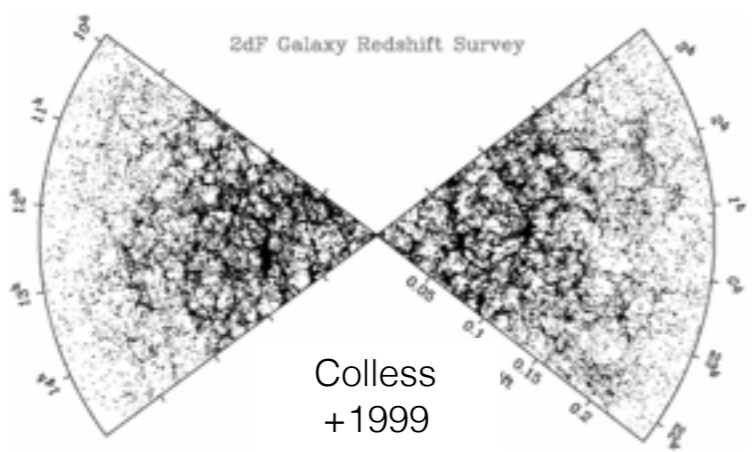
Motivation : Λ CDM? ▶ In practice



Directly
Observable
Universe

Overall: Λ CDM

Cosmological
Model



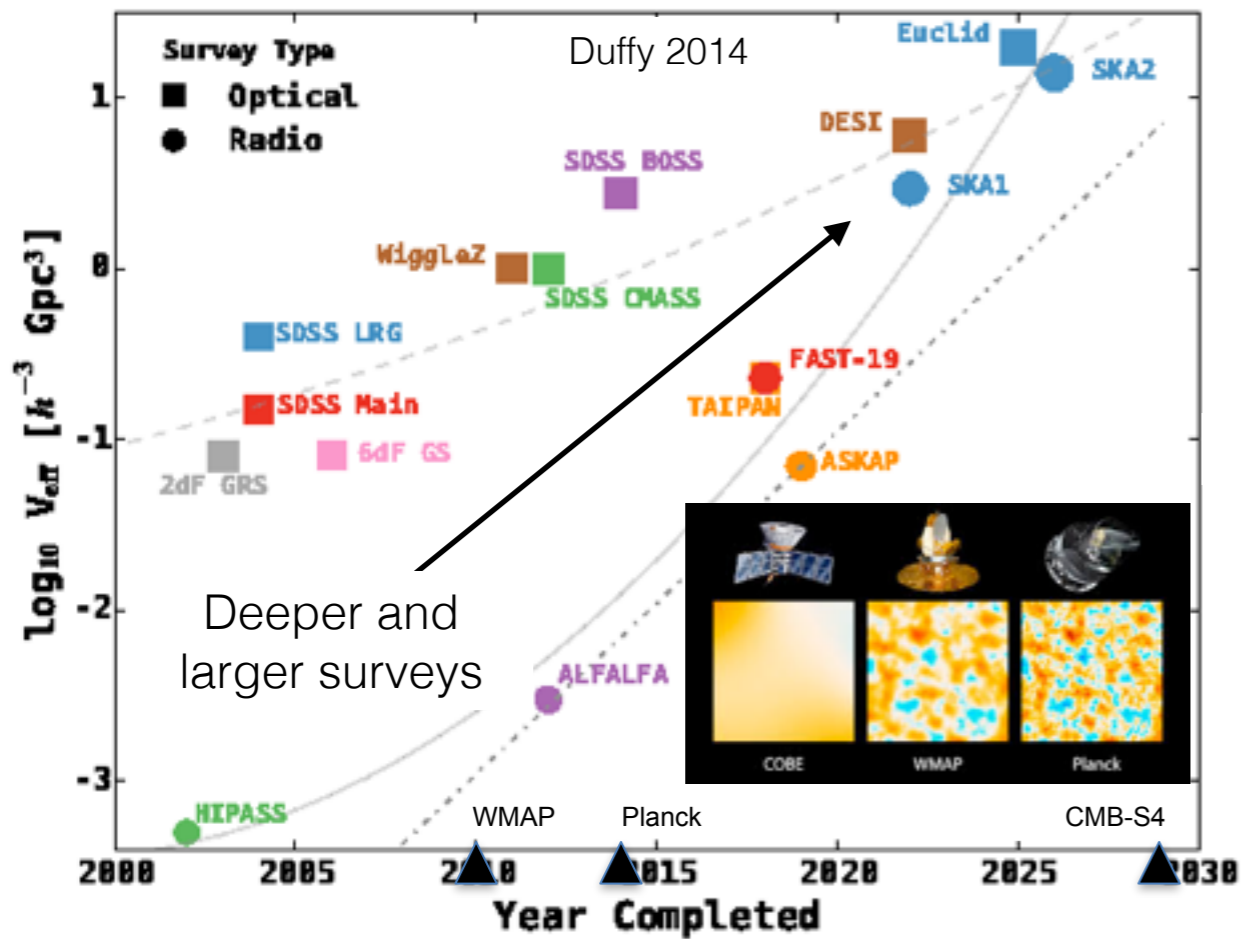
Motivation : Λ CDM? \blacktriangleright Toward precision cosmology



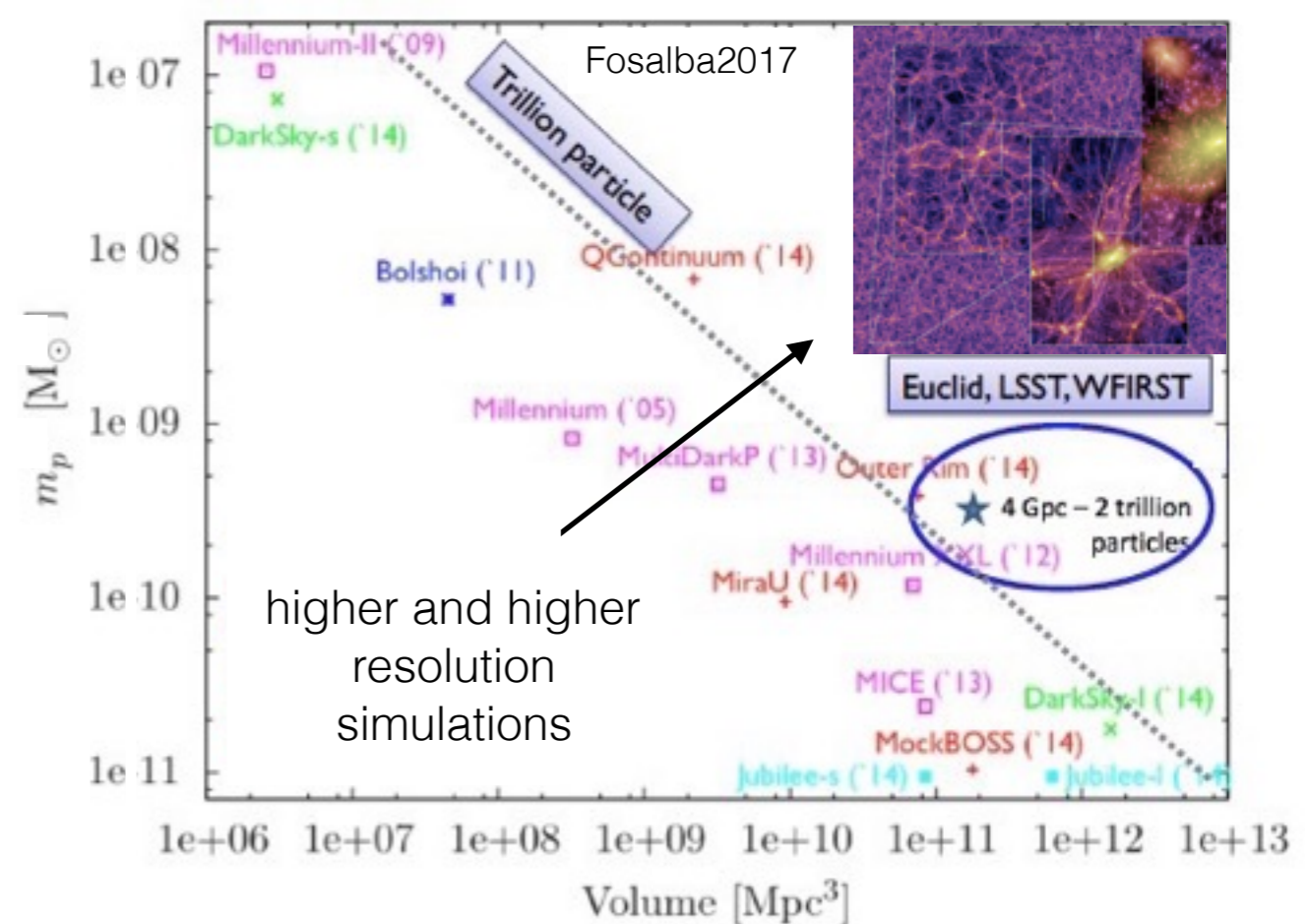
Precision Era:
1-2% precision

Λ CDM checked on all scales

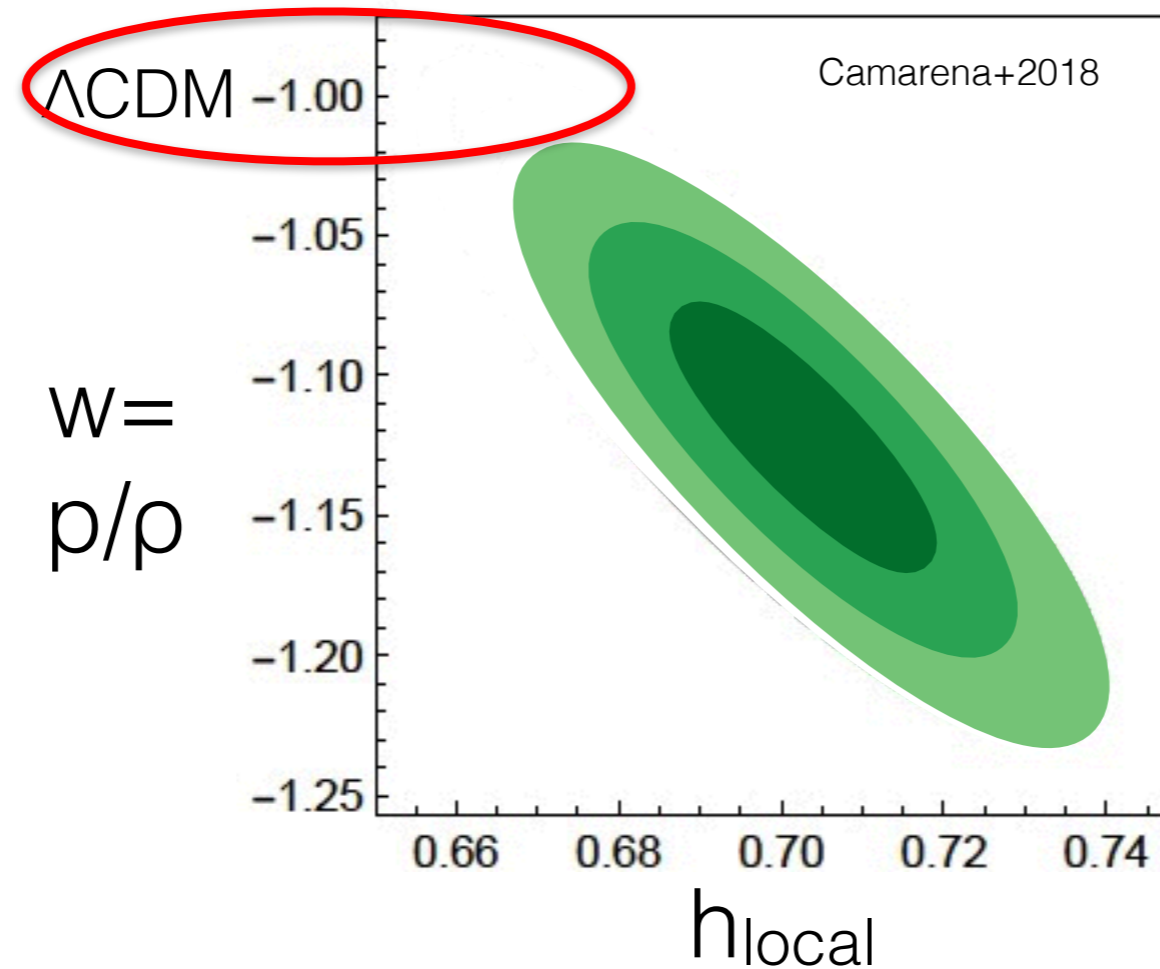
Observational



Numerical



Example: Equation of state of the dark energy

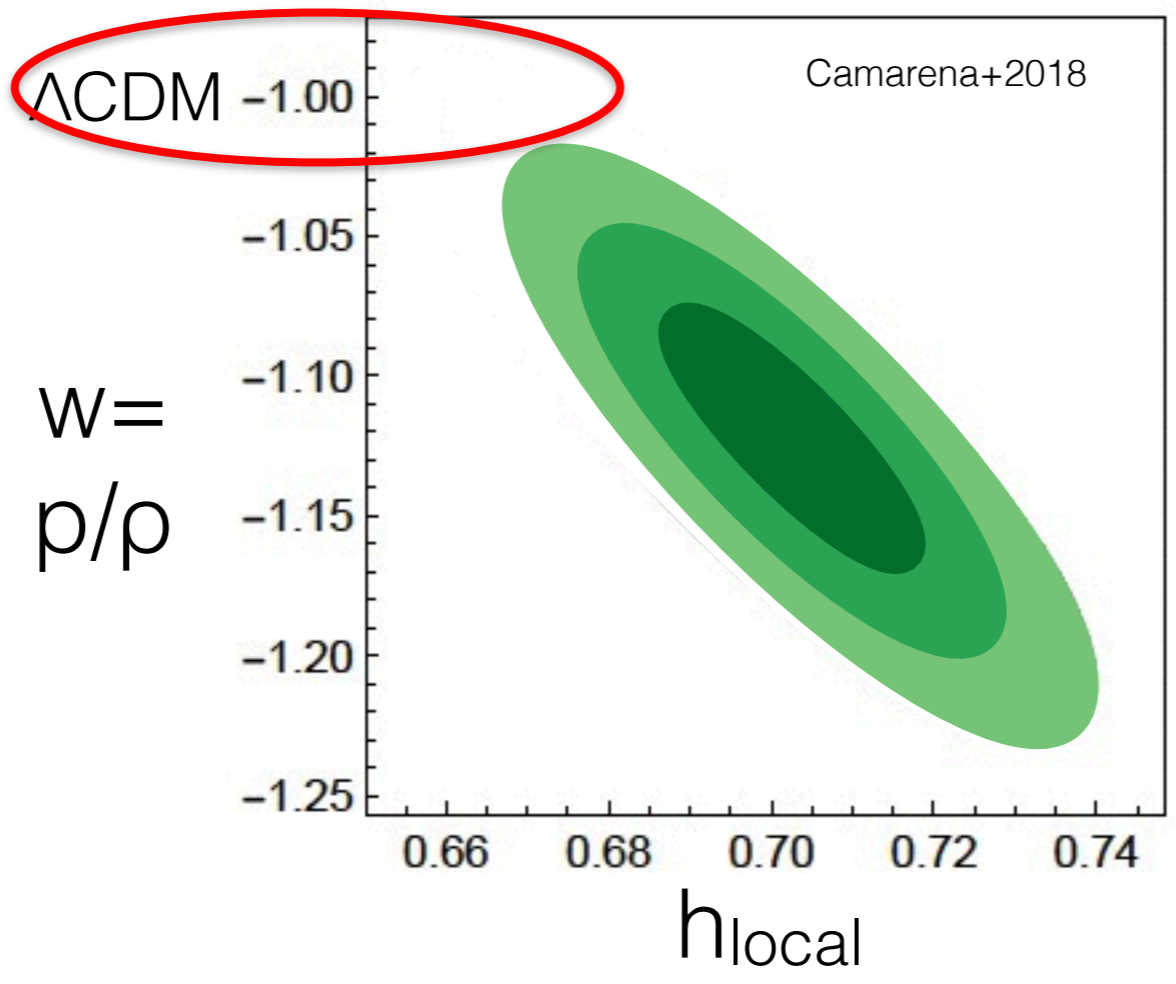


Precision is not accuracy !



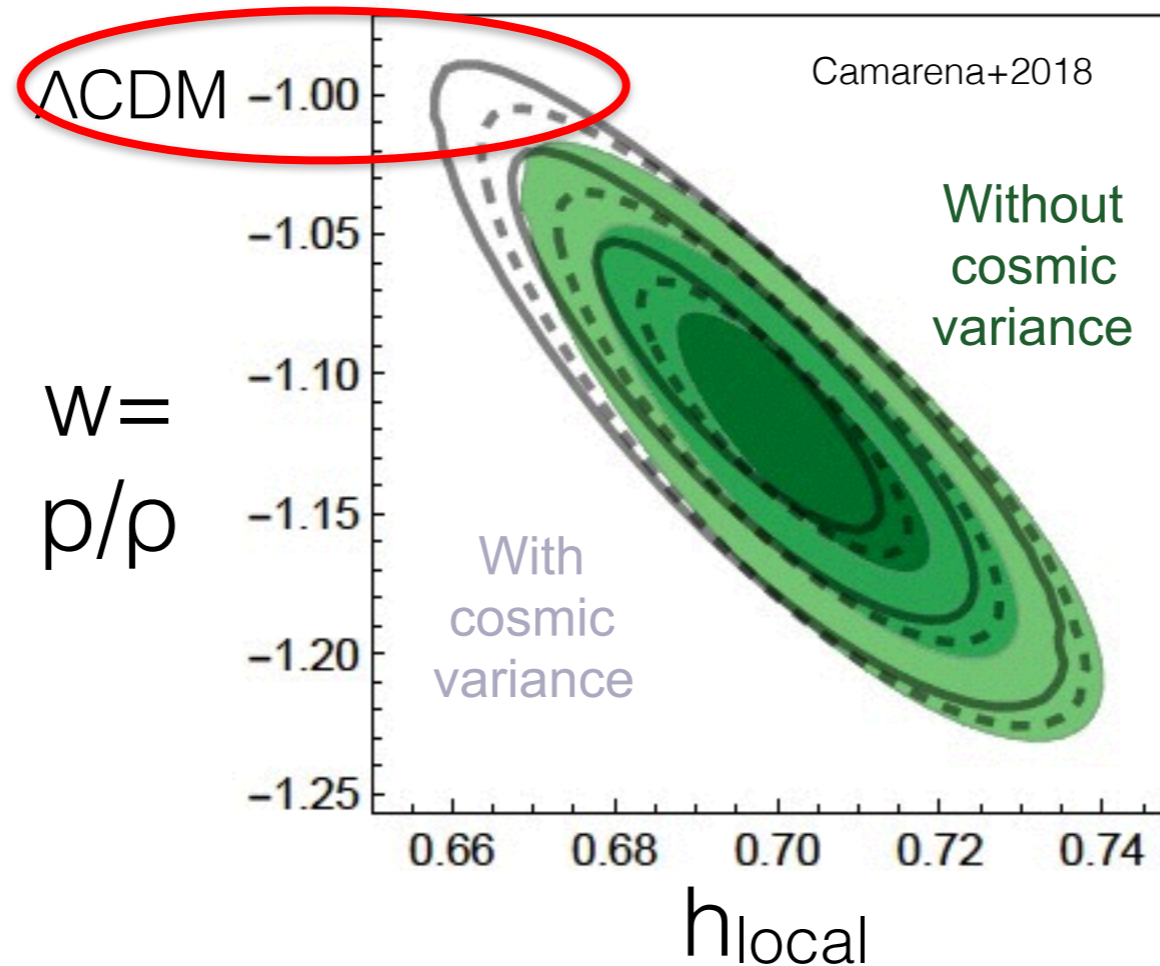
Motivation : Λ CDM? Precision is not accuracy: environmental biases?

Example: Equation of state of the dark energy



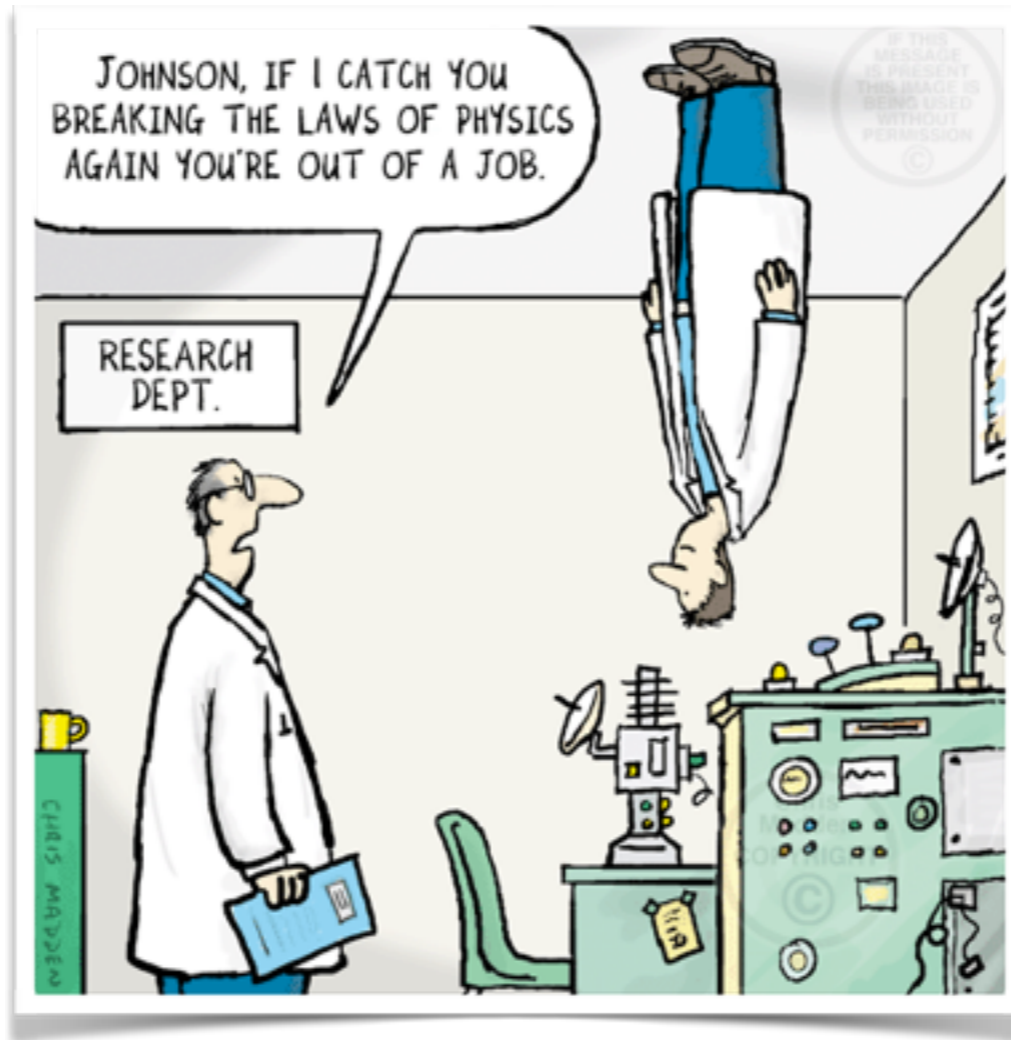
Motivation : Λ CDM? Both precision and accuracy are required!

Example: Equation of state of the dark energy



Accuracy:
1% bias non-negligible

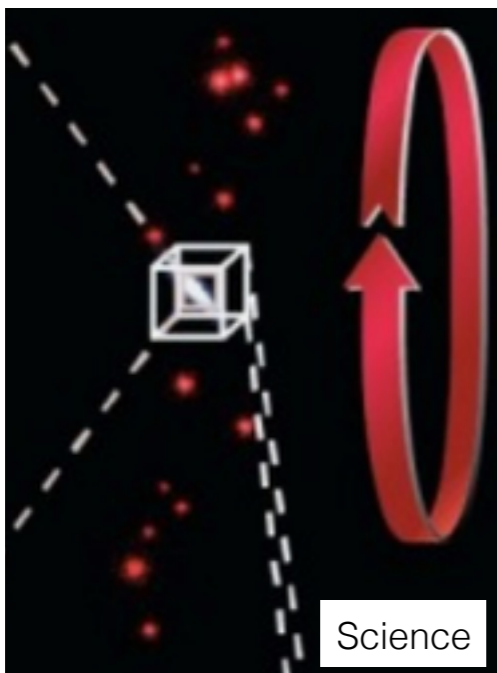
When observations challenge Λ CDM



A few examples

Small scales

Thin disks of satellites

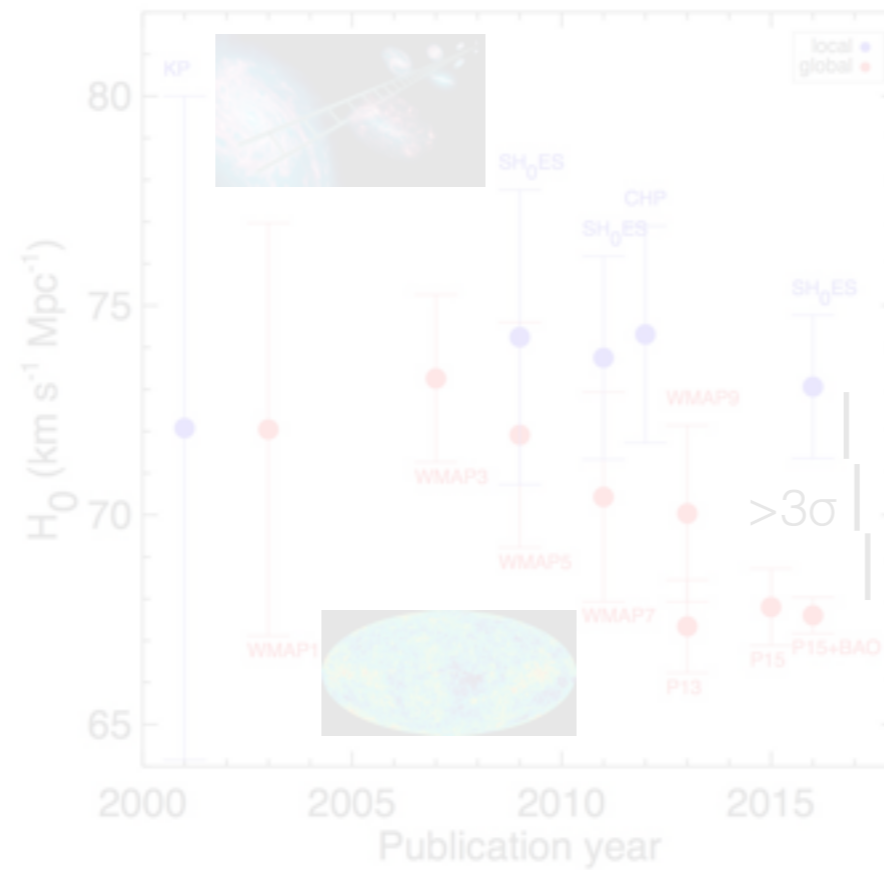


Observed... not simulated

Famaey+2013, Bullock+2017

local scales

local / global H_0

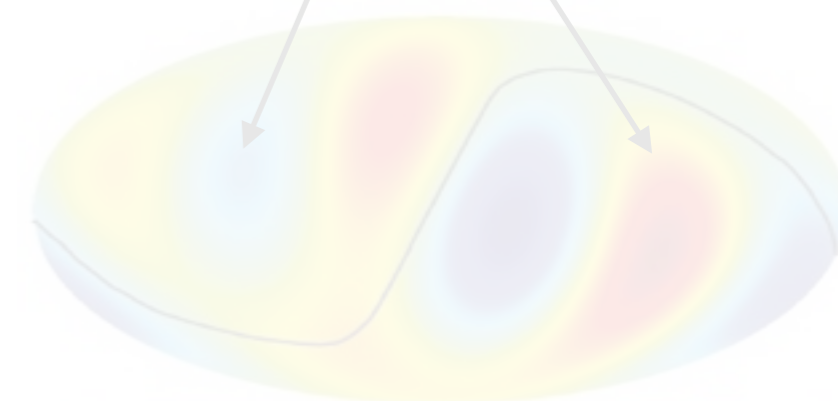


Freedman+2017

Large scales

CMB

North/South Asymmetry



Francis+2010

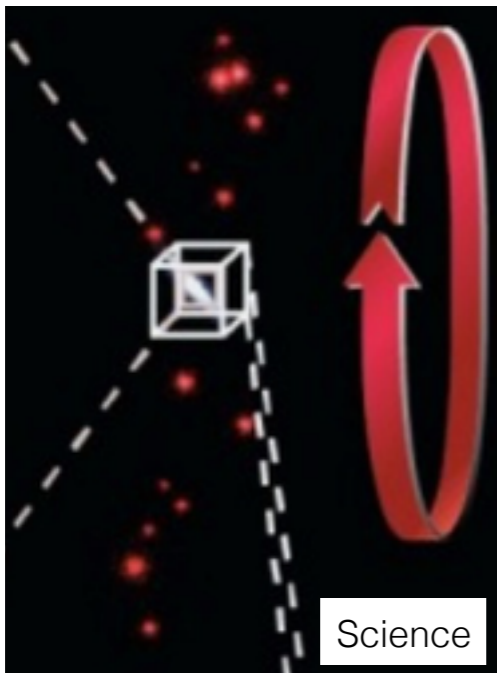
very unlikely...

e.g. Schwarz+2016

A few examples

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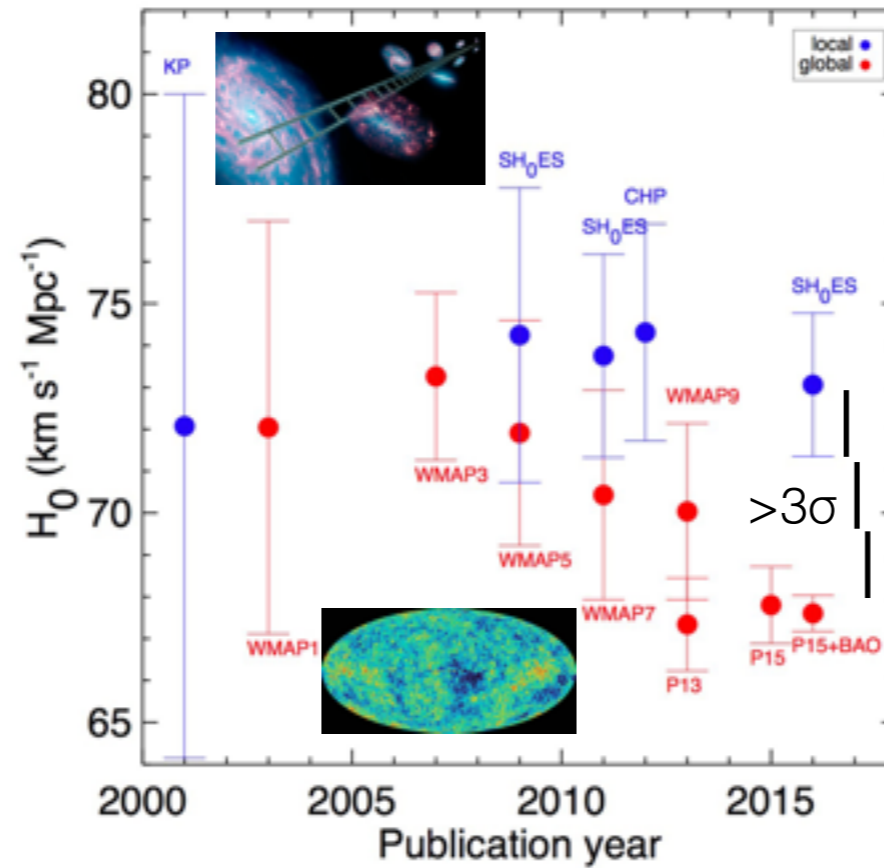


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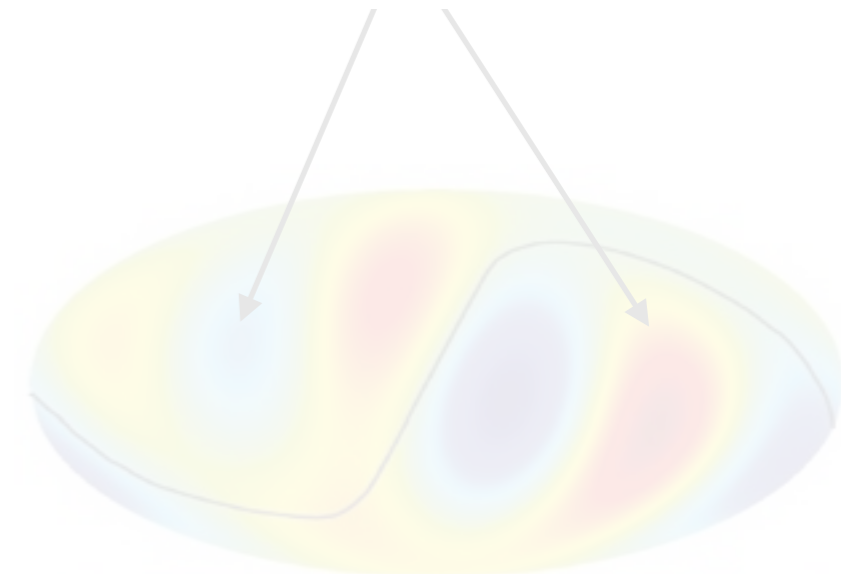


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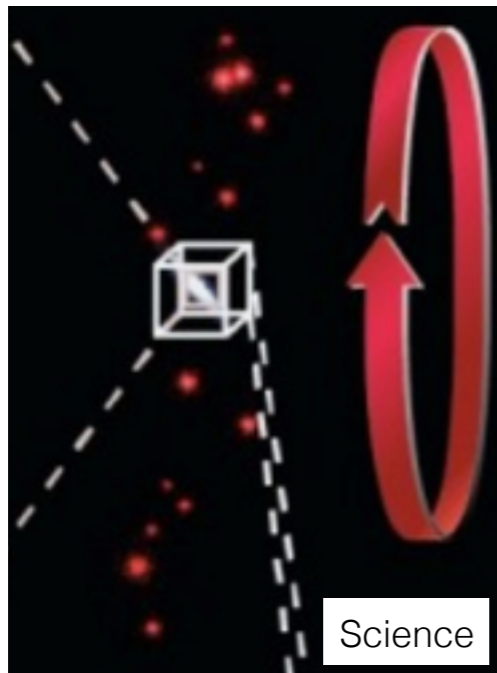
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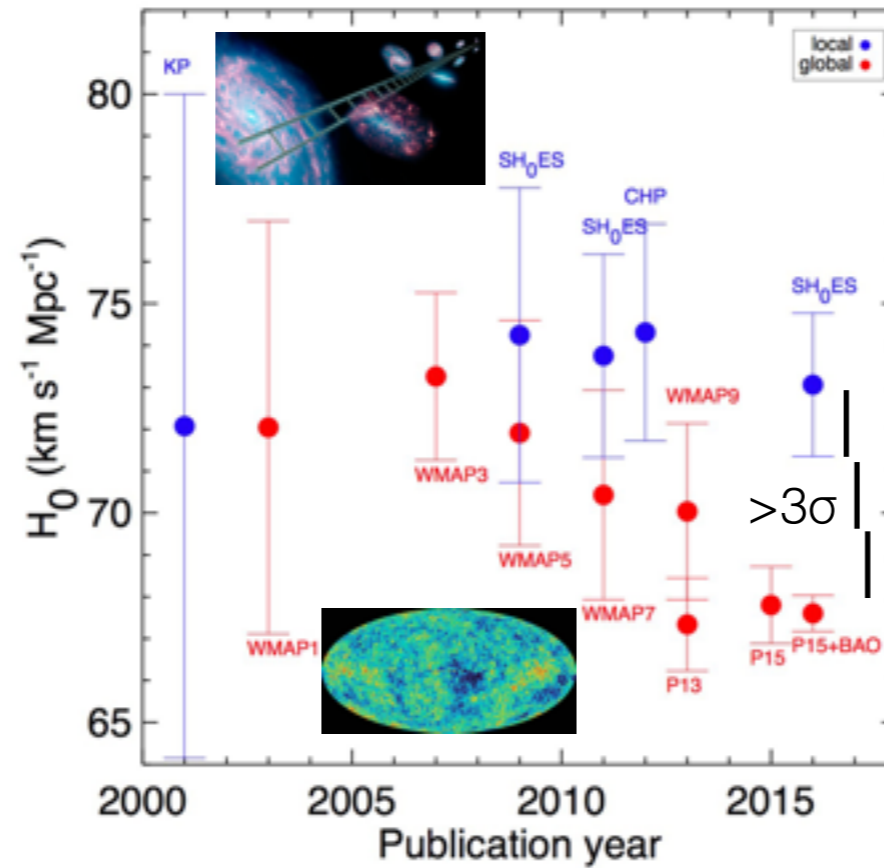


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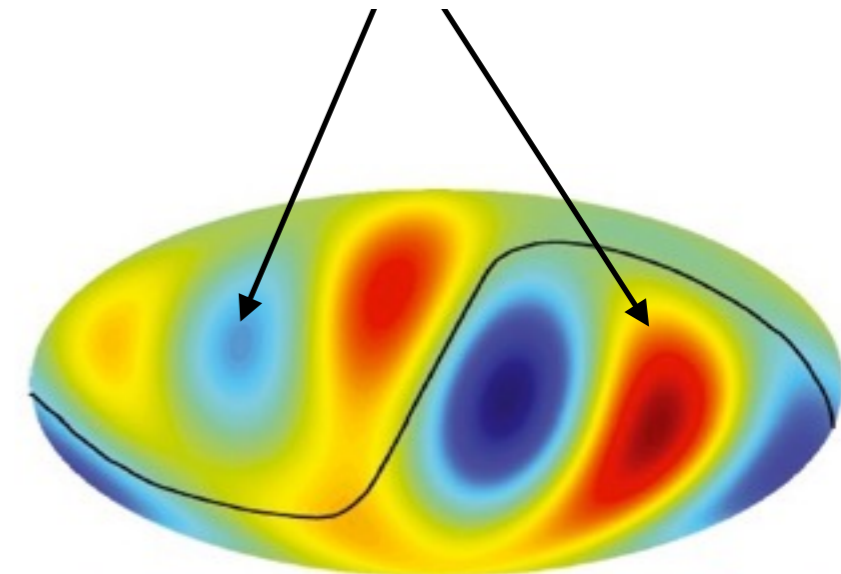


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More examples...

Small scales

local void emptier
with larger galaxies



Observed



Simulated

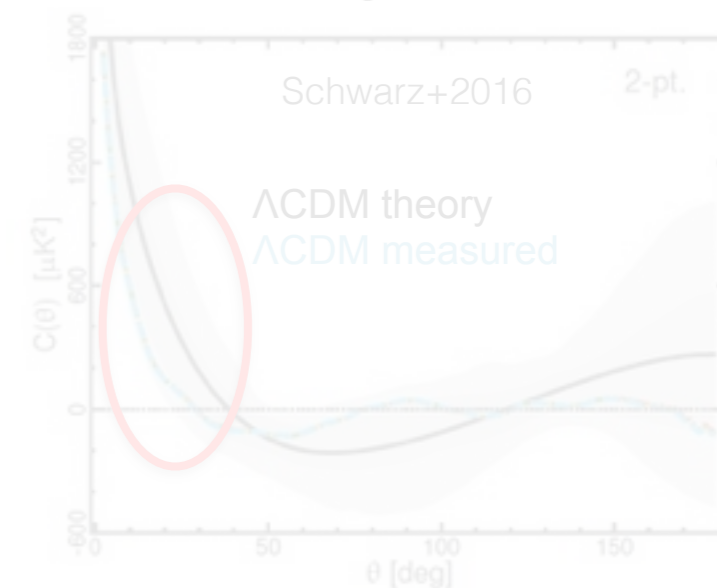
local scales

local / global cosmological
parameter values



Large scales

CMB



Lack of angular correlation
at large angles

Even more examples: local correlations slope and scatter, missing satellites, cold spot, etc

More examples...

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local void emptier
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Observed



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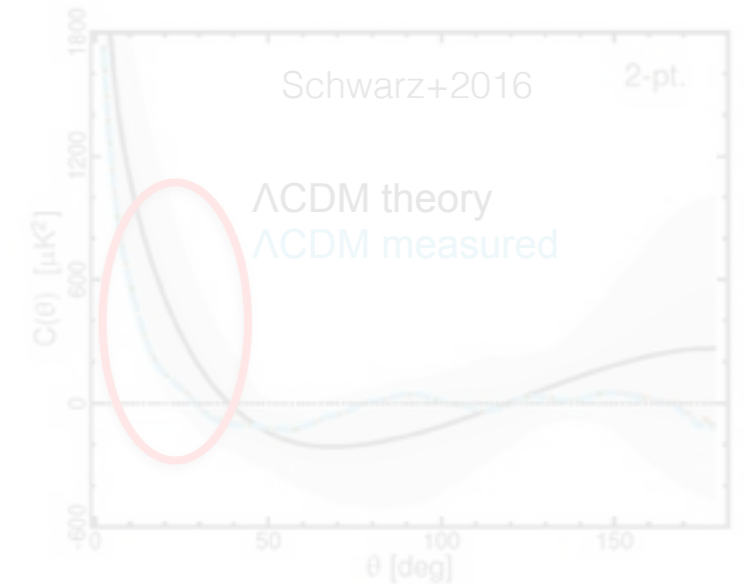
Planck SZ / CMB

$\sigma_8: 0.77 \pm 0.02 / 0.834 \pm 0.027$

$\Omega_m: 0.29 \pm 0.02 / 0.314 \pm 0.020$

Large scales

CMB



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More examples...

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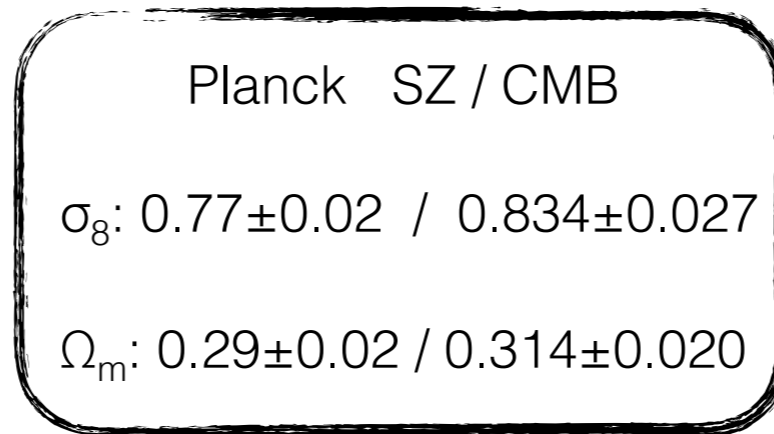
Observed



Simulated

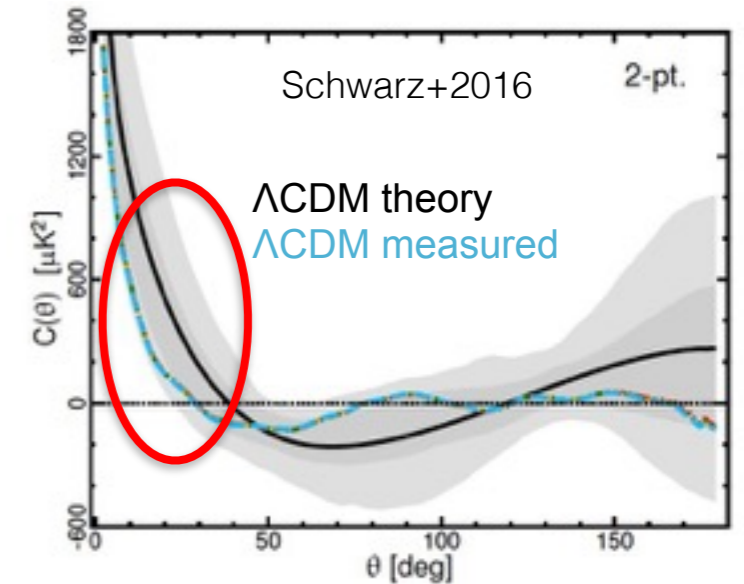
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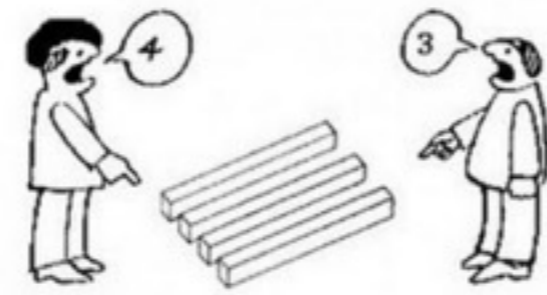
Questions?

Small scales



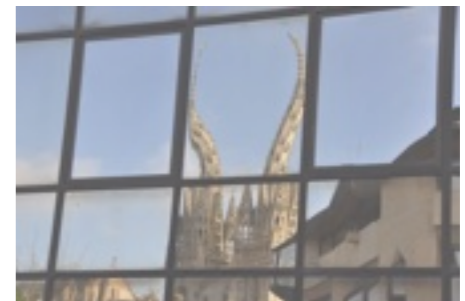
Are we comparing apple to apple?

local scales



Are we a neutral observer?

Large scales



What about a foreground effect?

Local-induced biases

How can our local environment bias our "perception" at the 1-2% level preventing us from reaching 1-2% precision?

Small scales



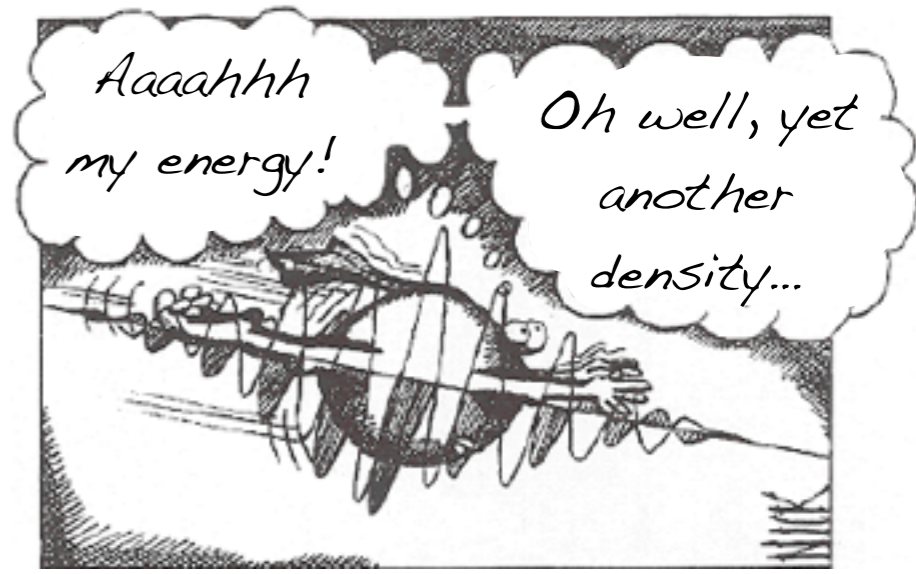
Clear... correlation with environment

local scales



A neutral environment?
Very unlikely...

Large scales



Photons travel a lot before reaching us...

and eventually this can decrease *or increase* tensions with Λ CDM !

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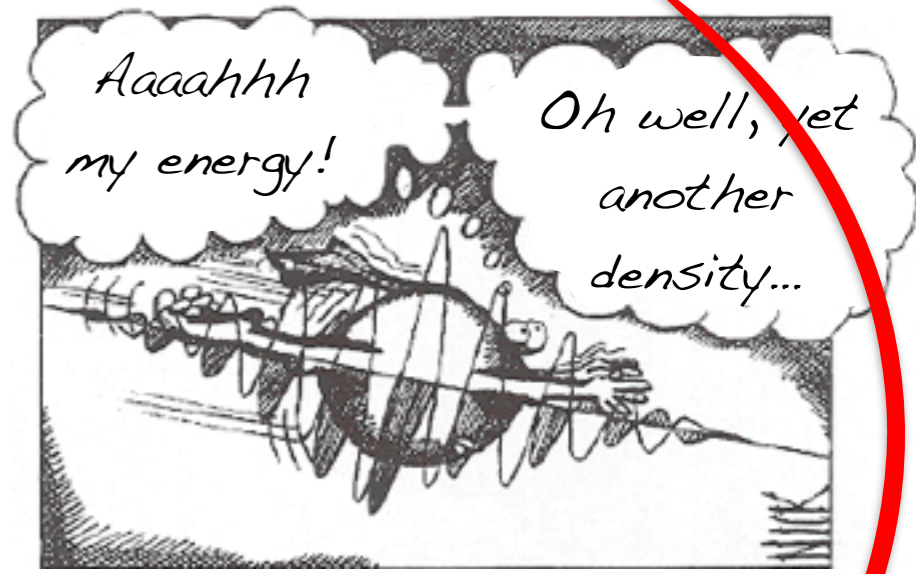
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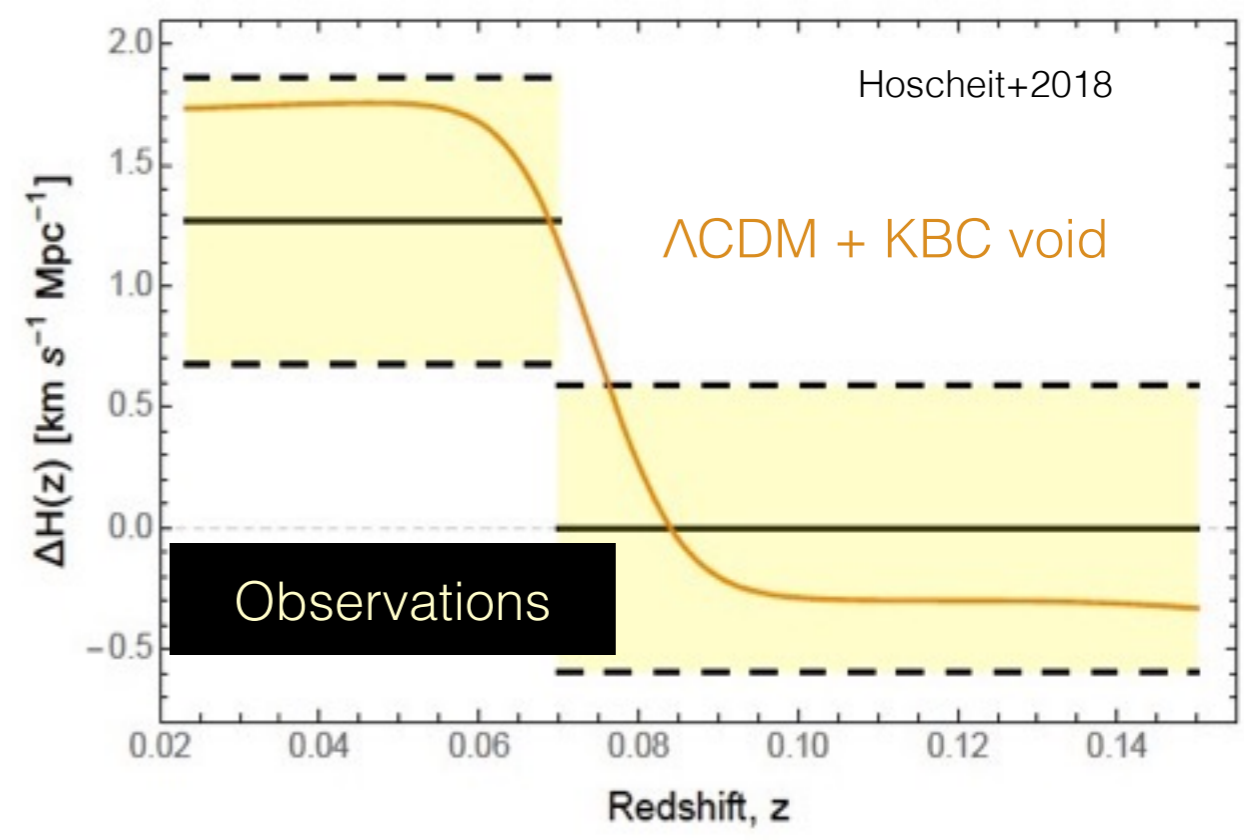
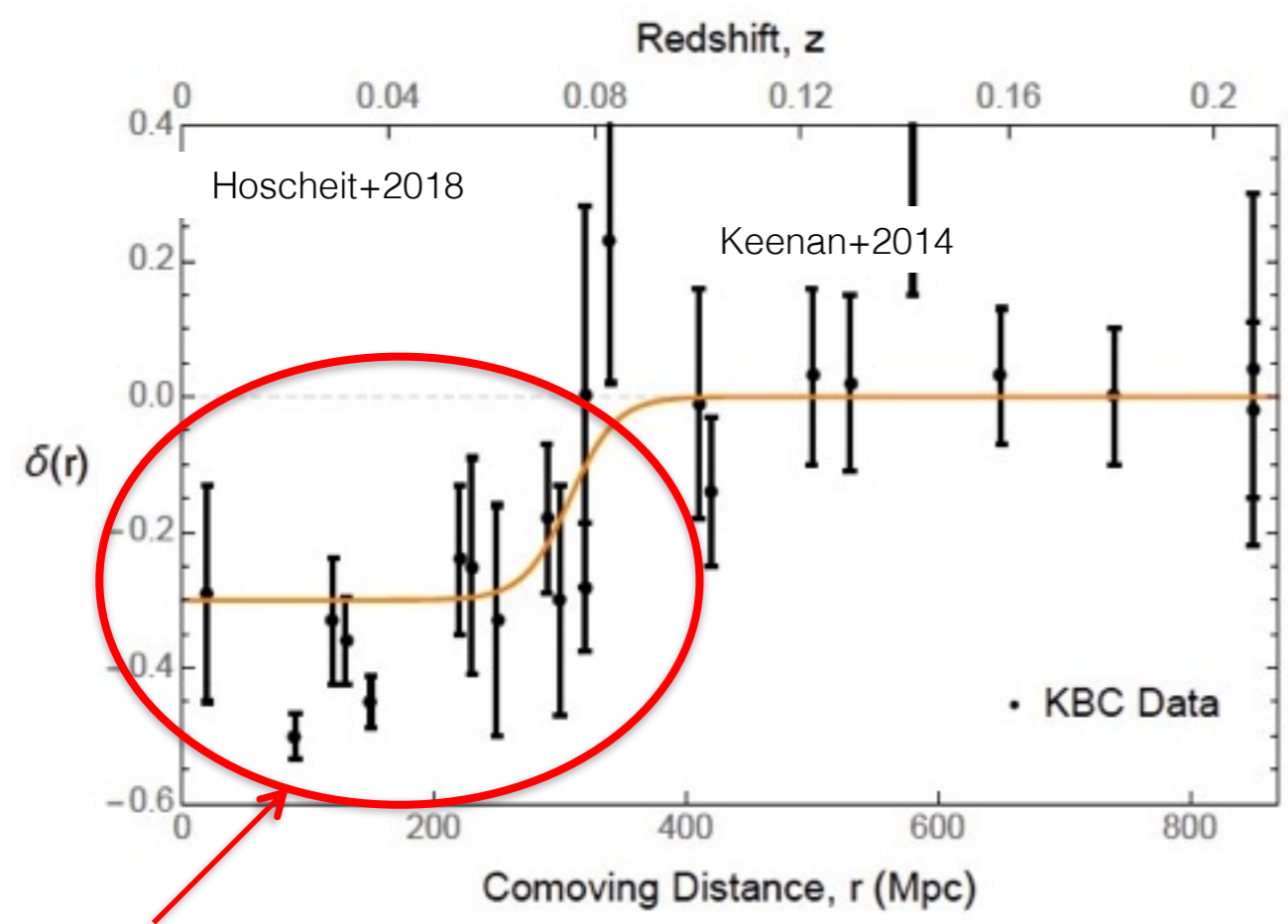


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Local-induced biases on the local scales

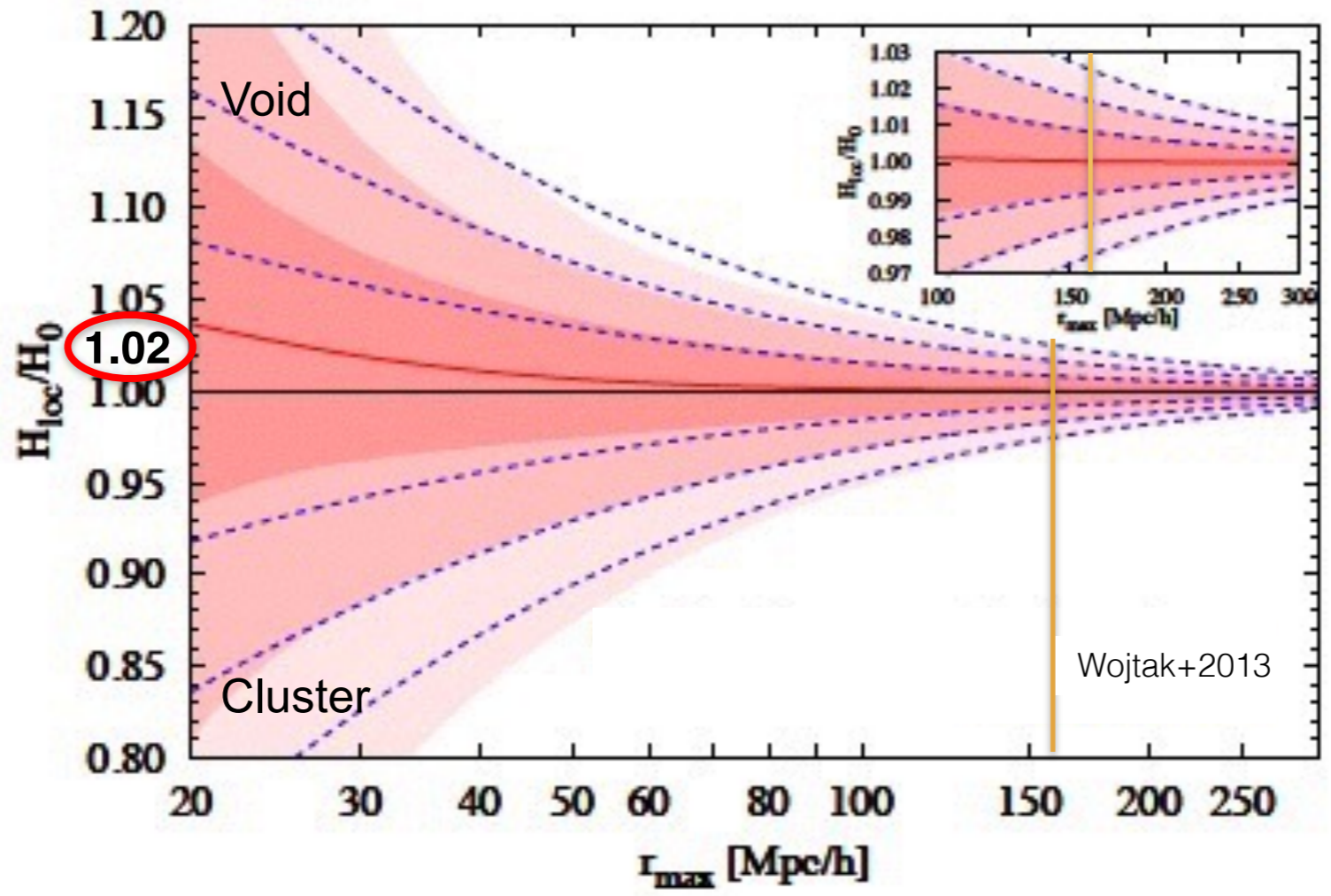
A simple example: we live in a spherical underdensity



An example: Hint at a local underdensity up to $z=0.07$

Local-induced biases on the local scales

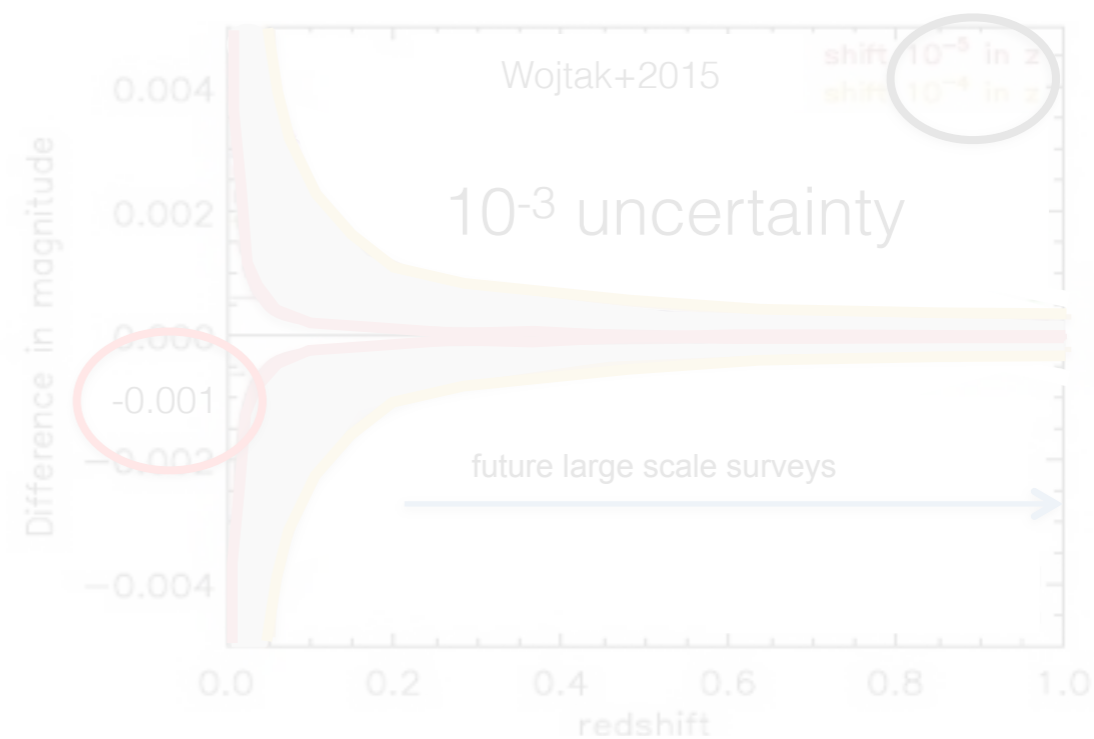
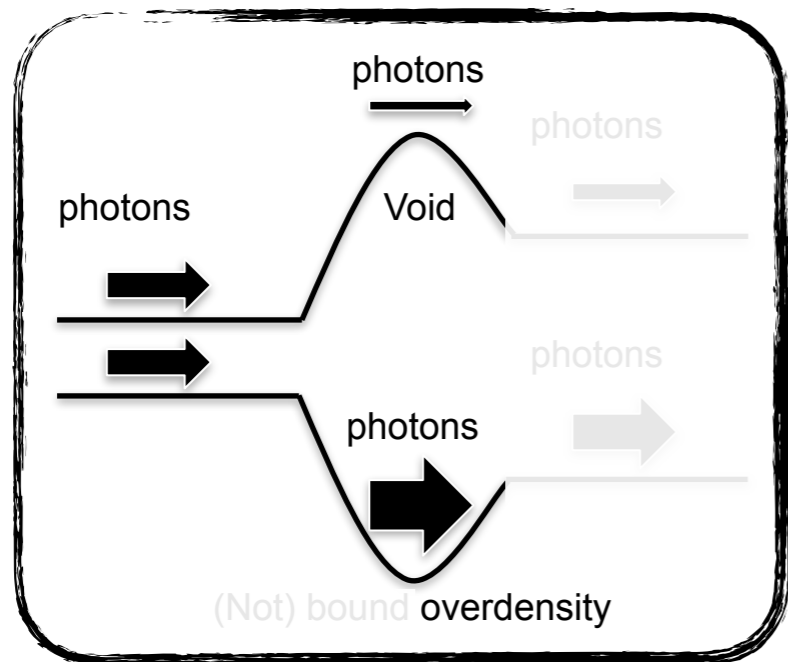
As many effect values as environments



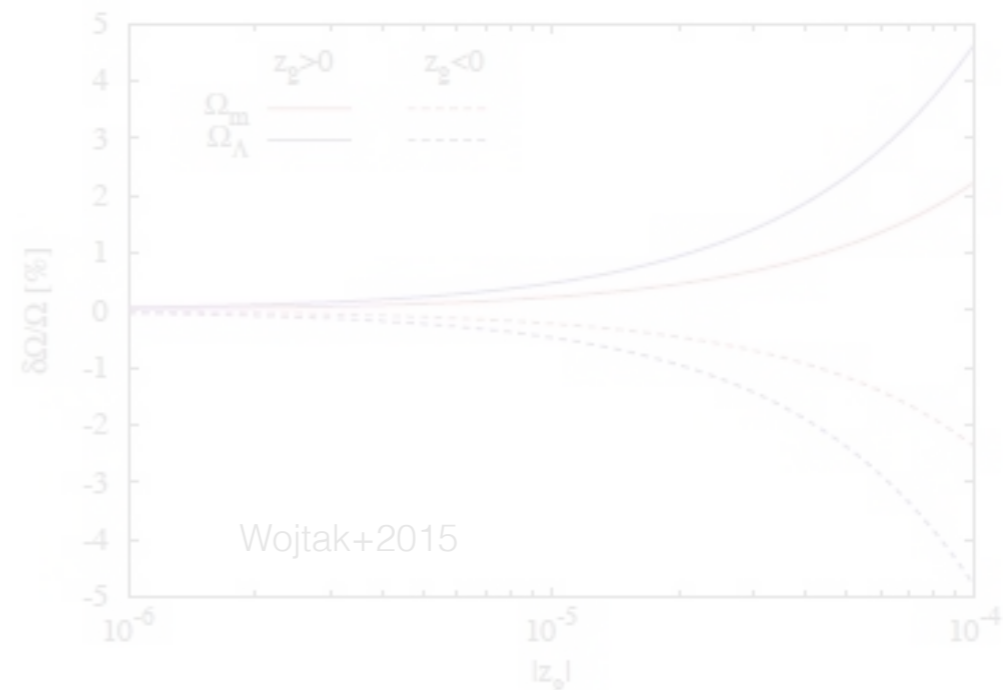
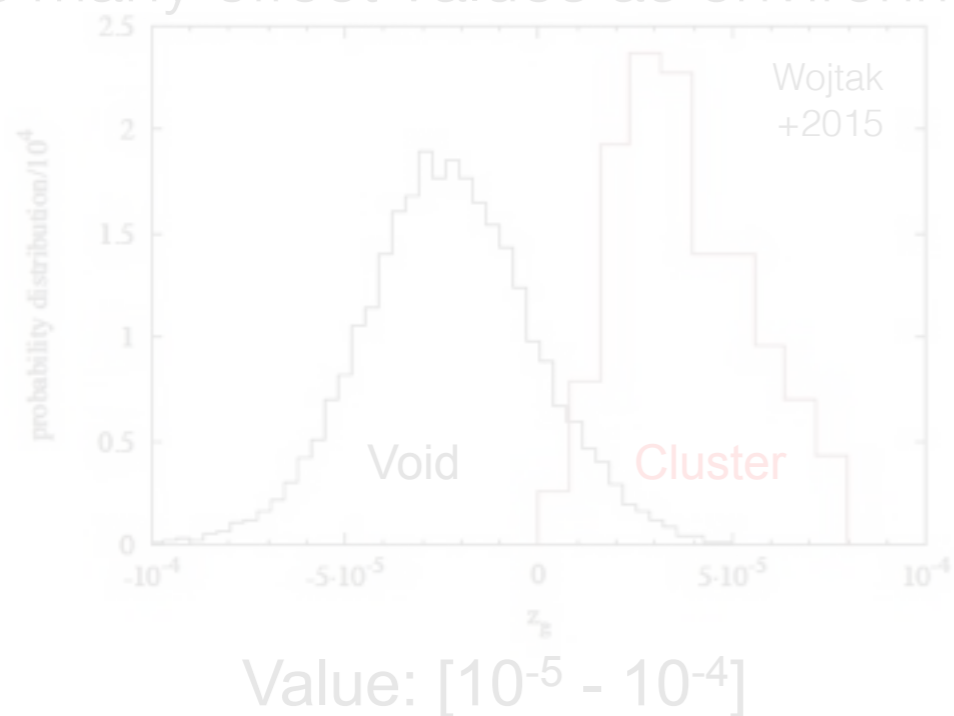
For an average environment: a 2% bias !

Local-induced biases on the large scales

Gravitational redshifts and the large scale surveys



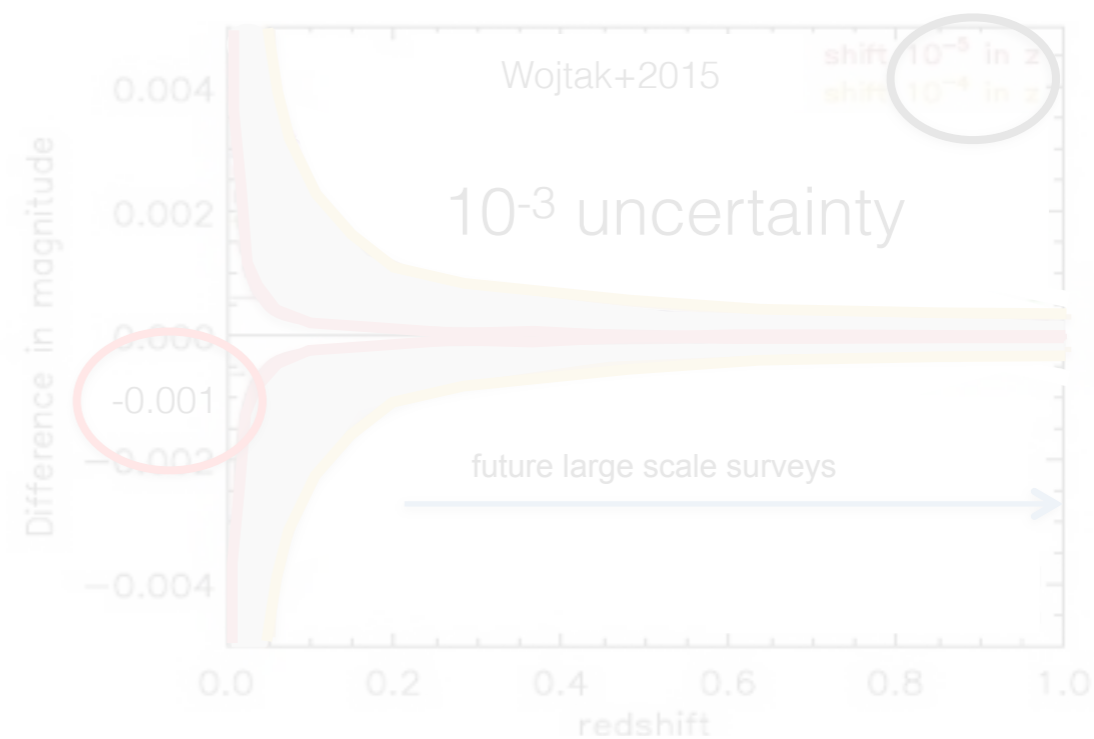
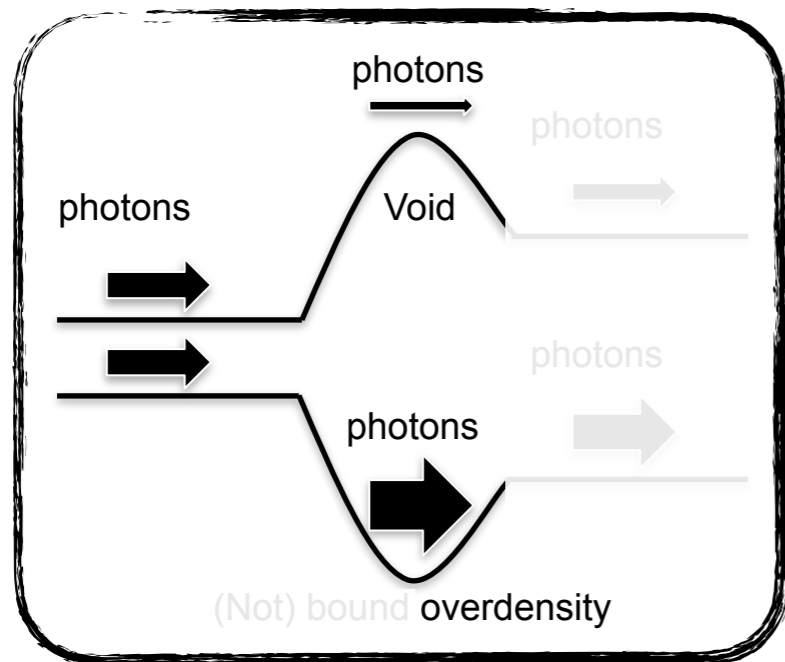
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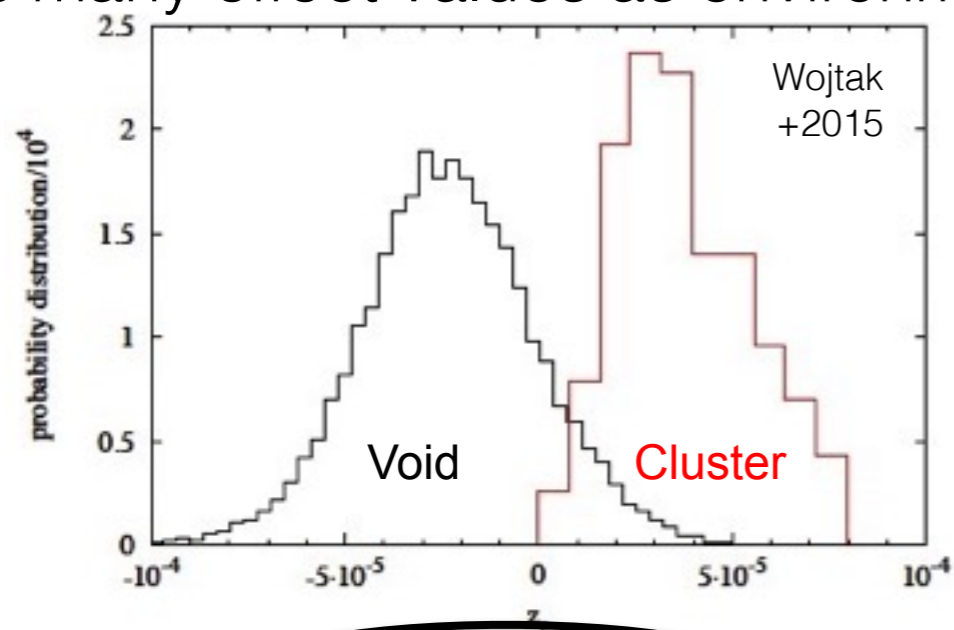
For an average environment: a 1-2% bias !

Local-induced biases ▶ on the large scales

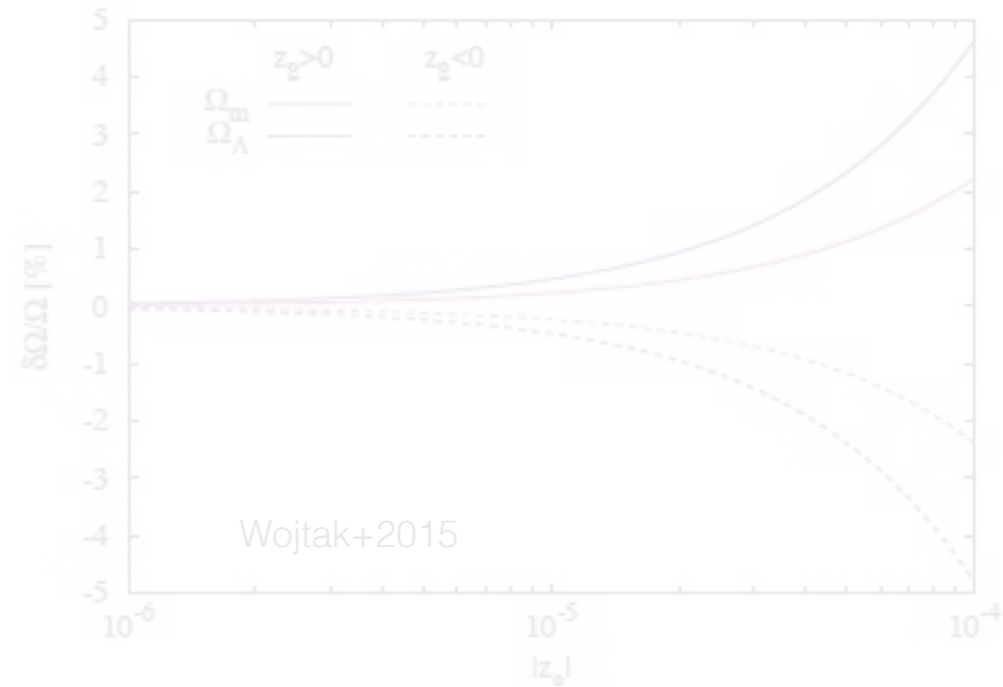
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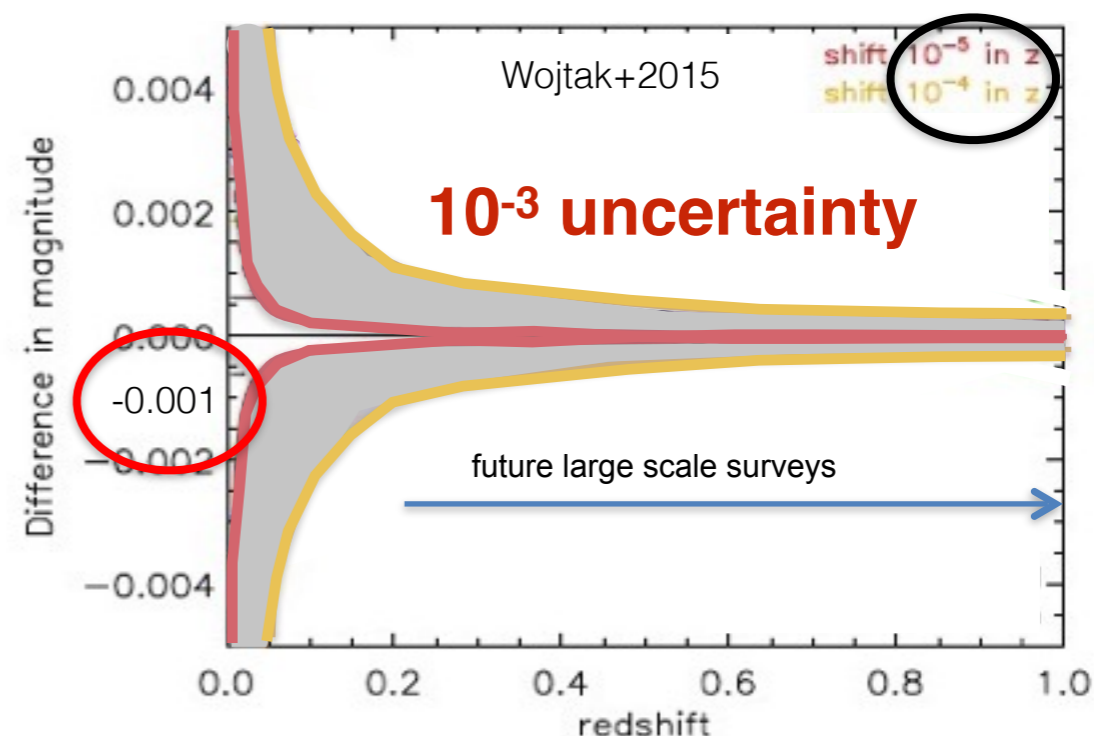
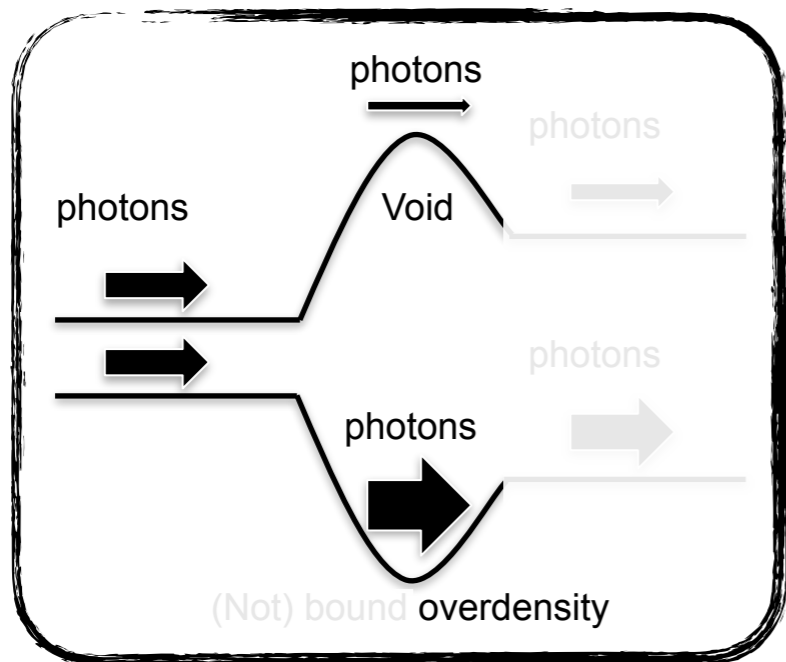
Value: $[10^{-5} - 10^{-4}]$



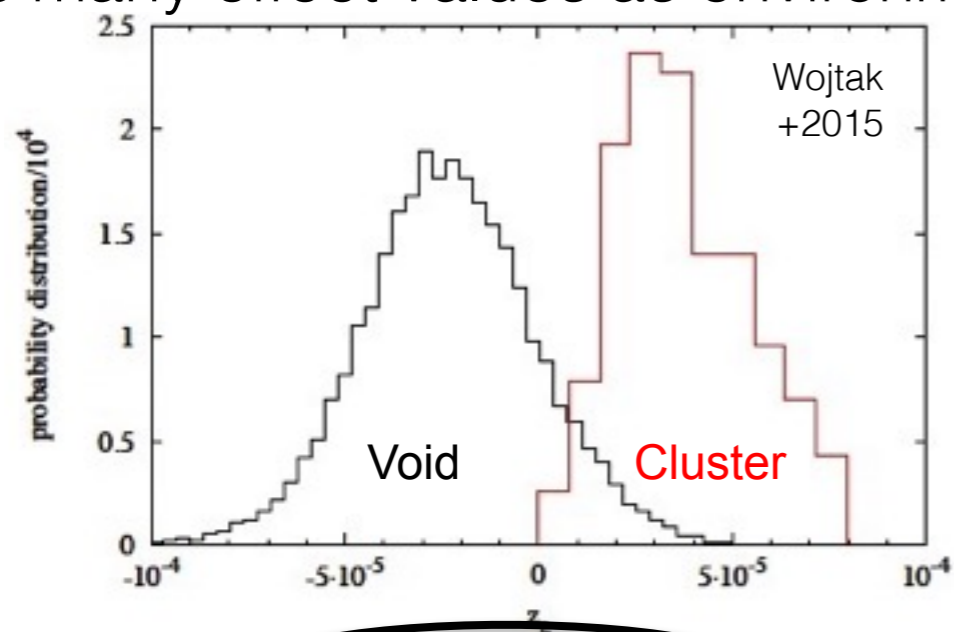
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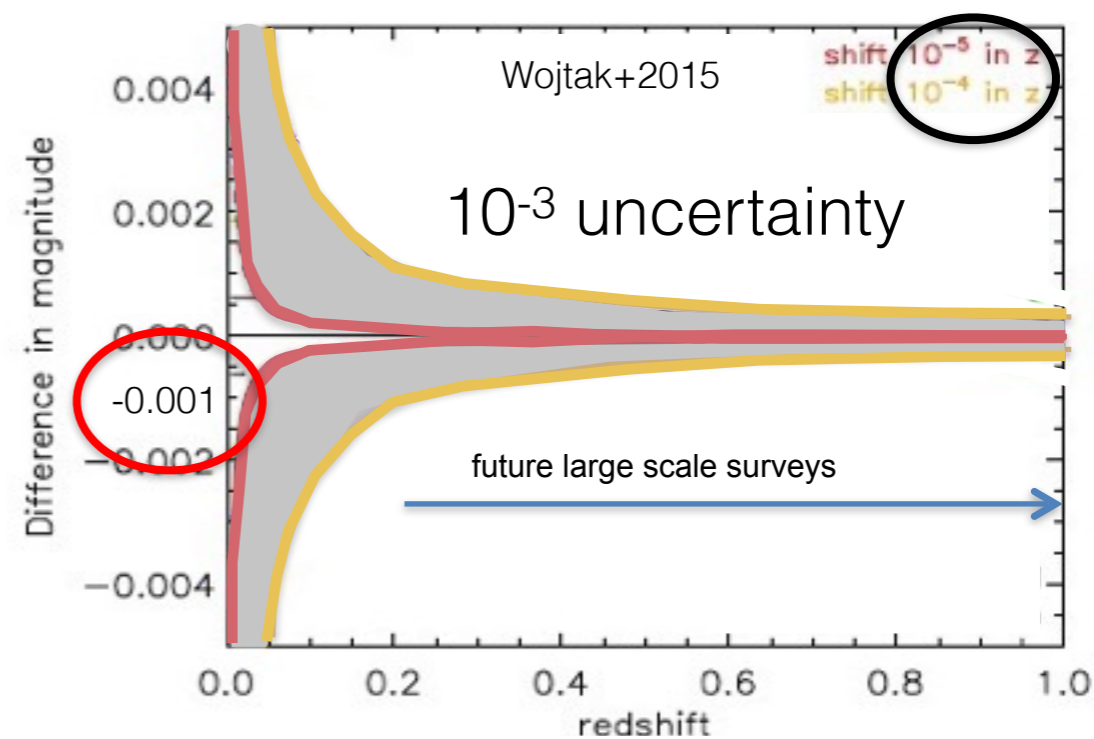
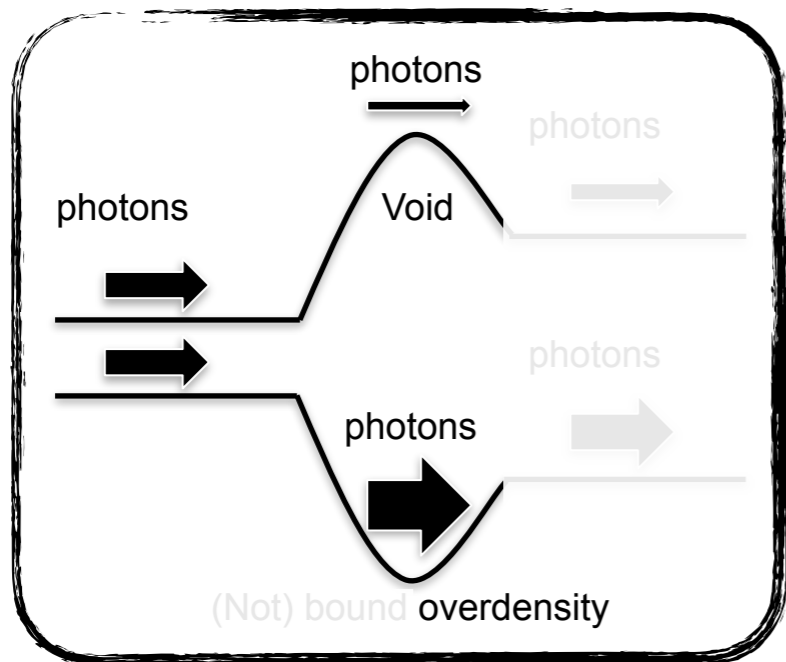
Value: [10⁻⁵ - 10⁻⁴]



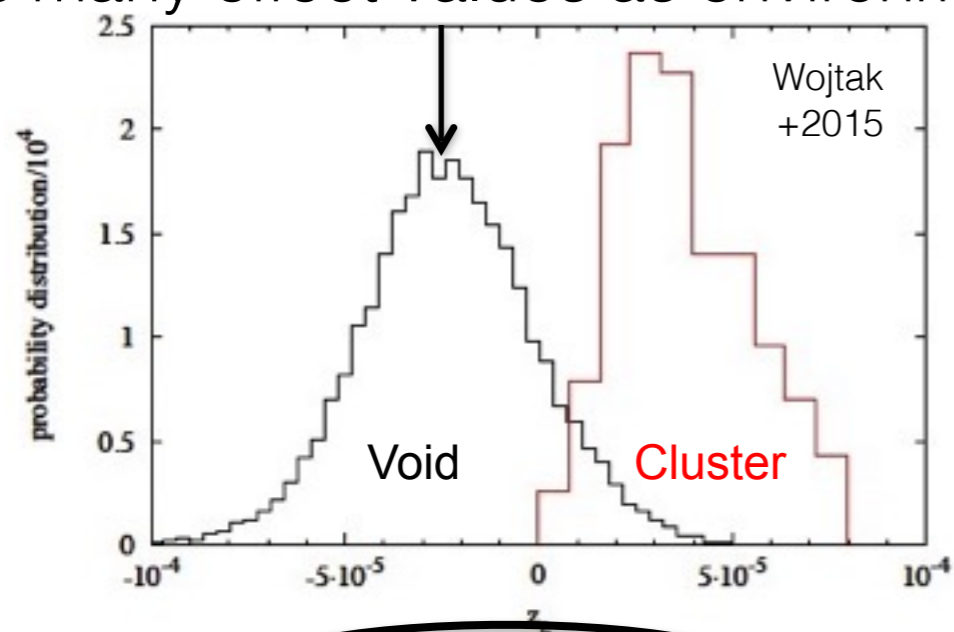
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Local-induced biases on the large scales

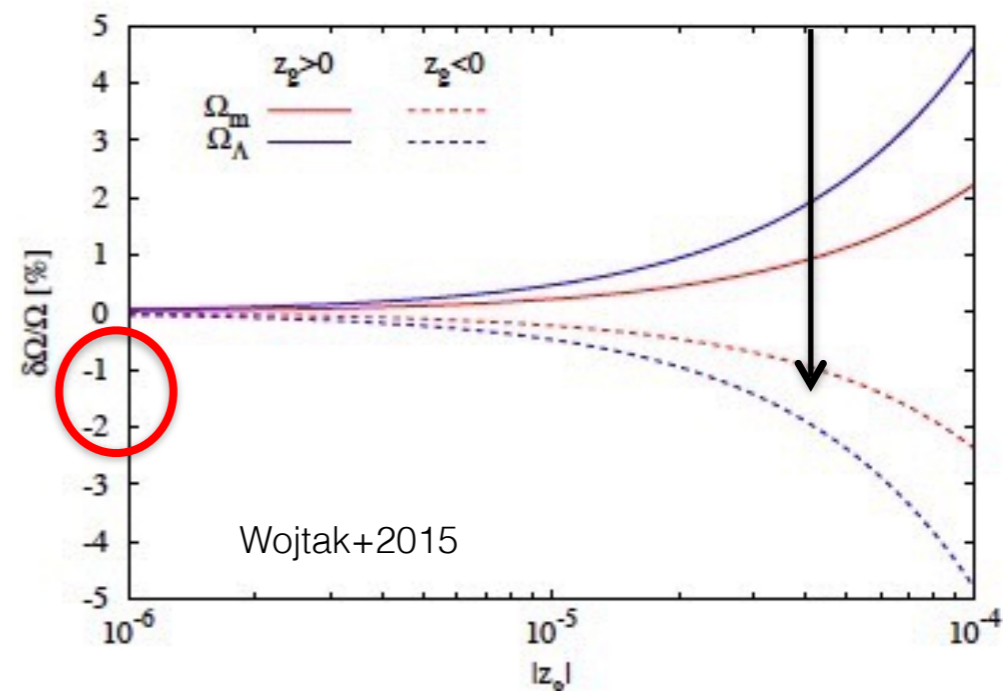
Gravitational redshifts and the large scale surveys



As many effect values as environments



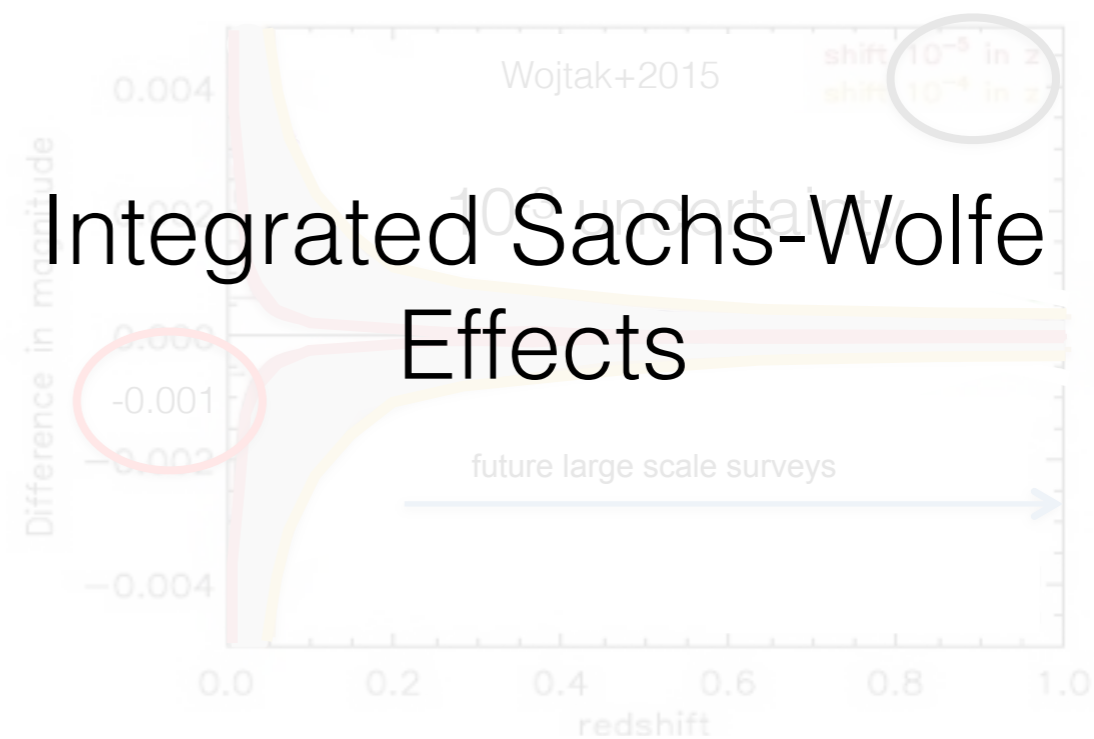
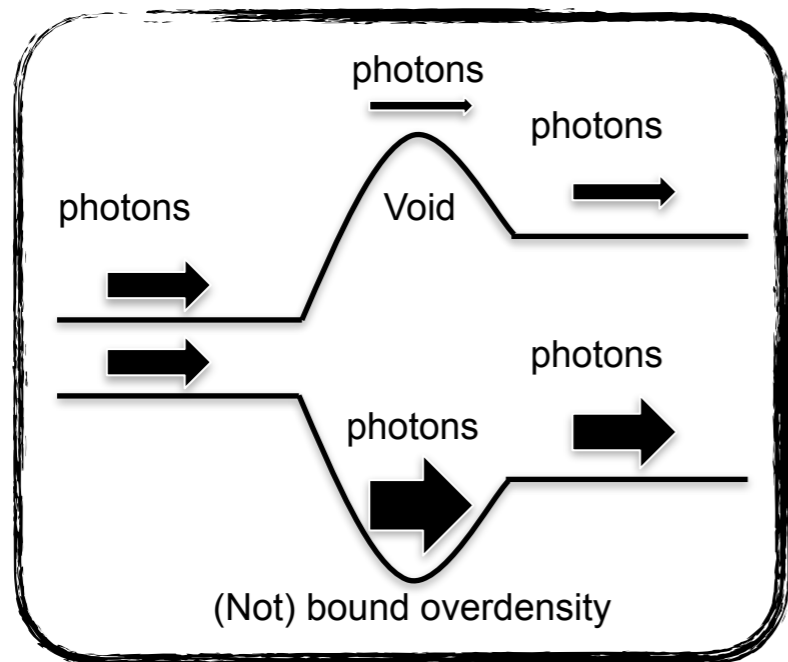
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For an average environment: a 1-2% bias !

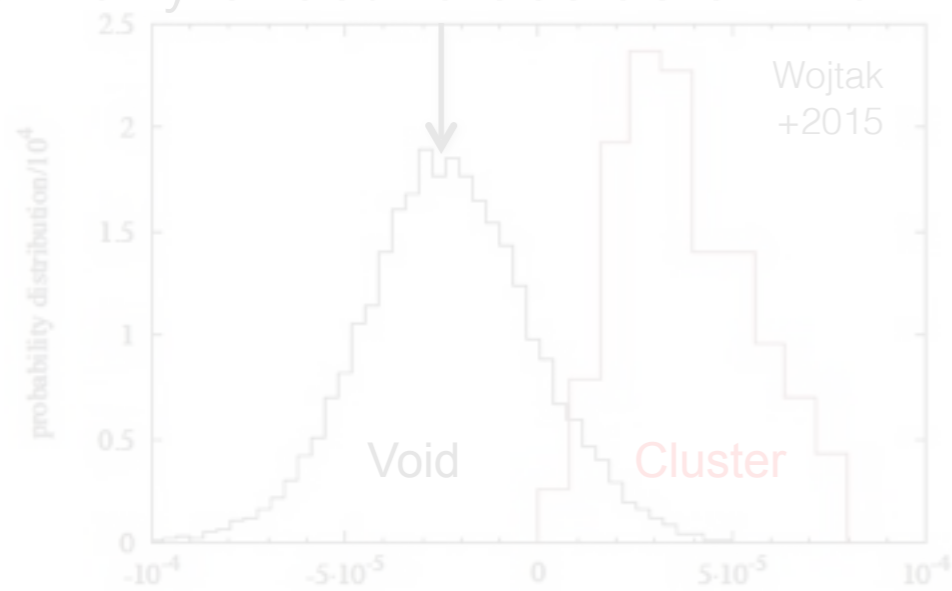
Local-induced biases on the large scales

Gravitational redshifts and the large scale surveys

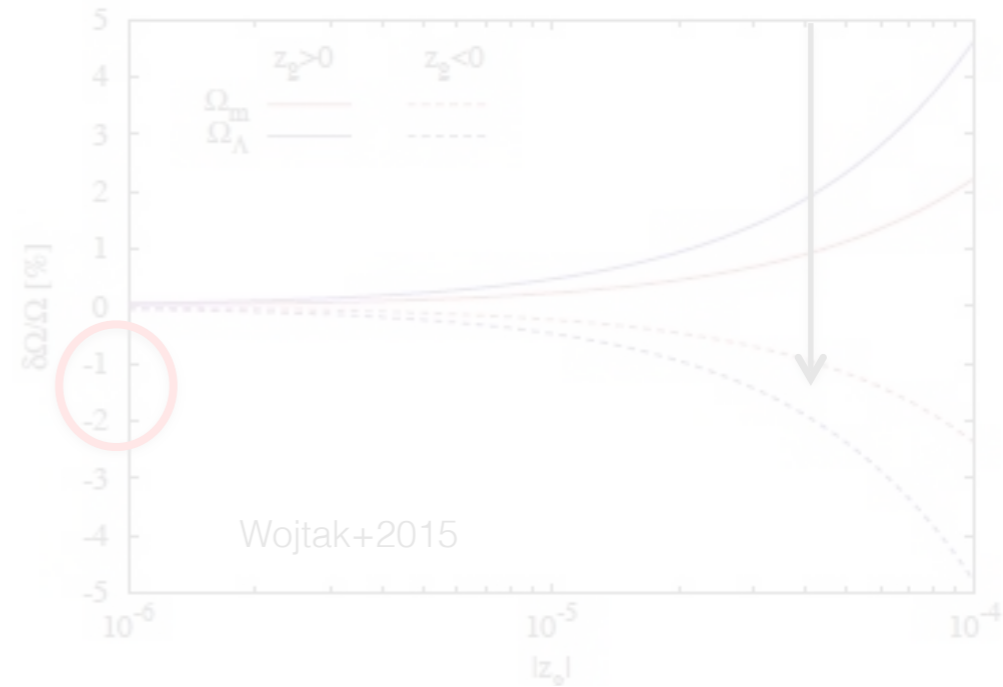


Integrated Sachs-Wolfe Effects

As many effect values as environments



Value: $[10^{-5} - 10^{-4}]$



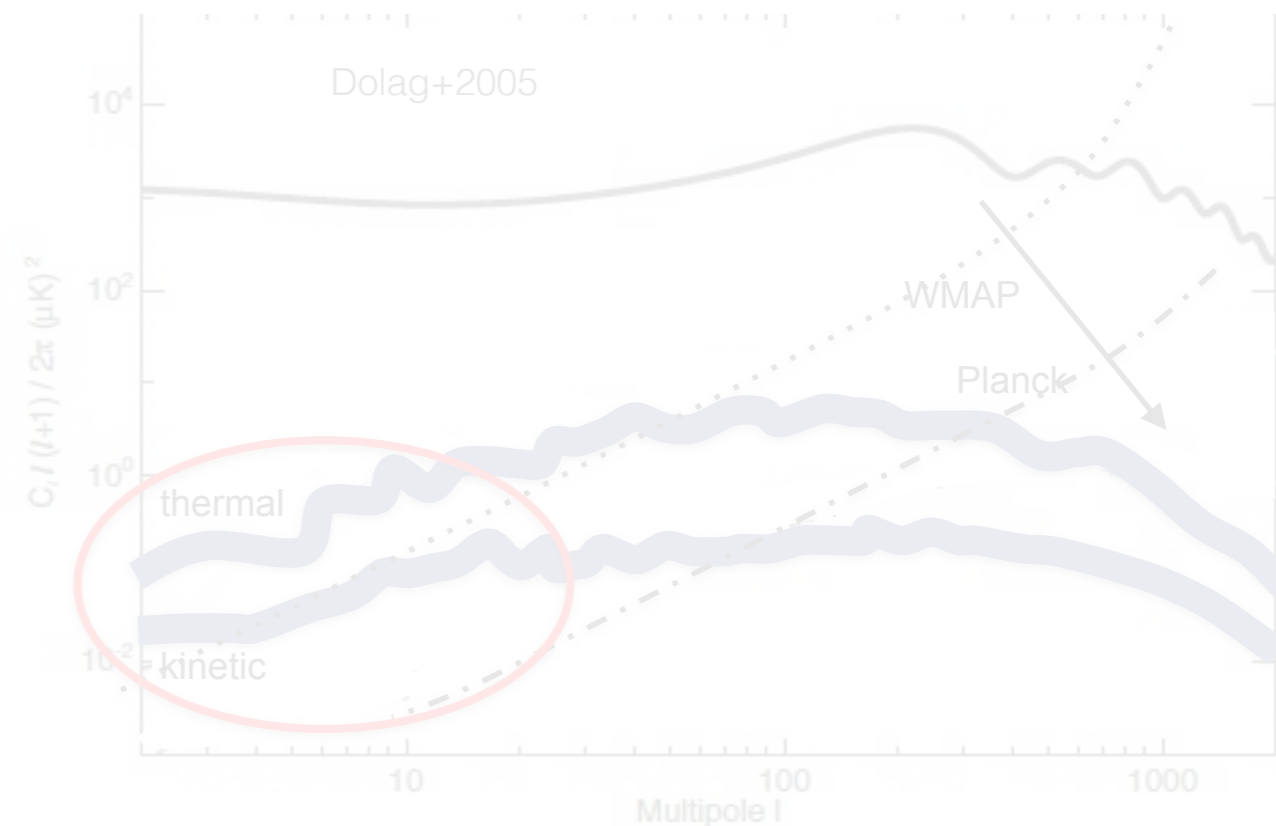
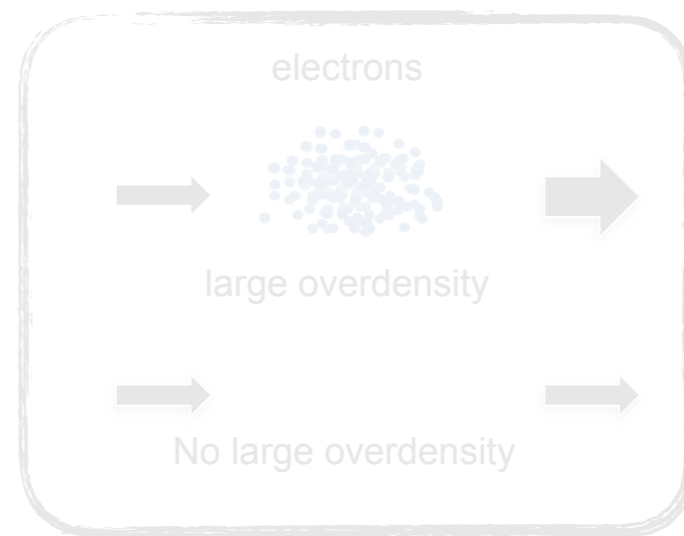
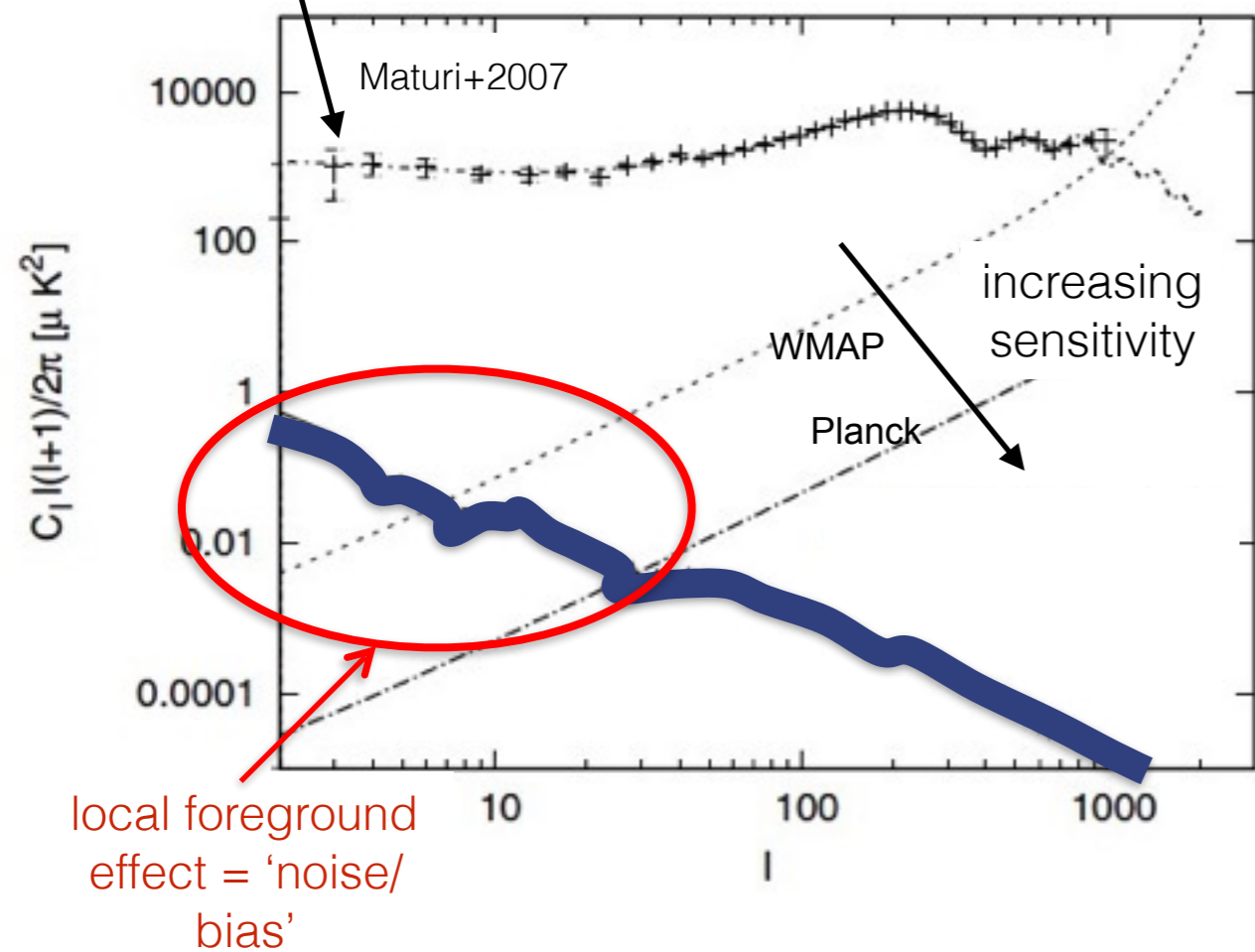
For an average environment: a 1-2% bias !

Local-induced biases on the large scales

Gravitational redshift, Sunyaev Zel'dovich and the CMB

increasing precision
= reducing error bars

Rees-Sciama

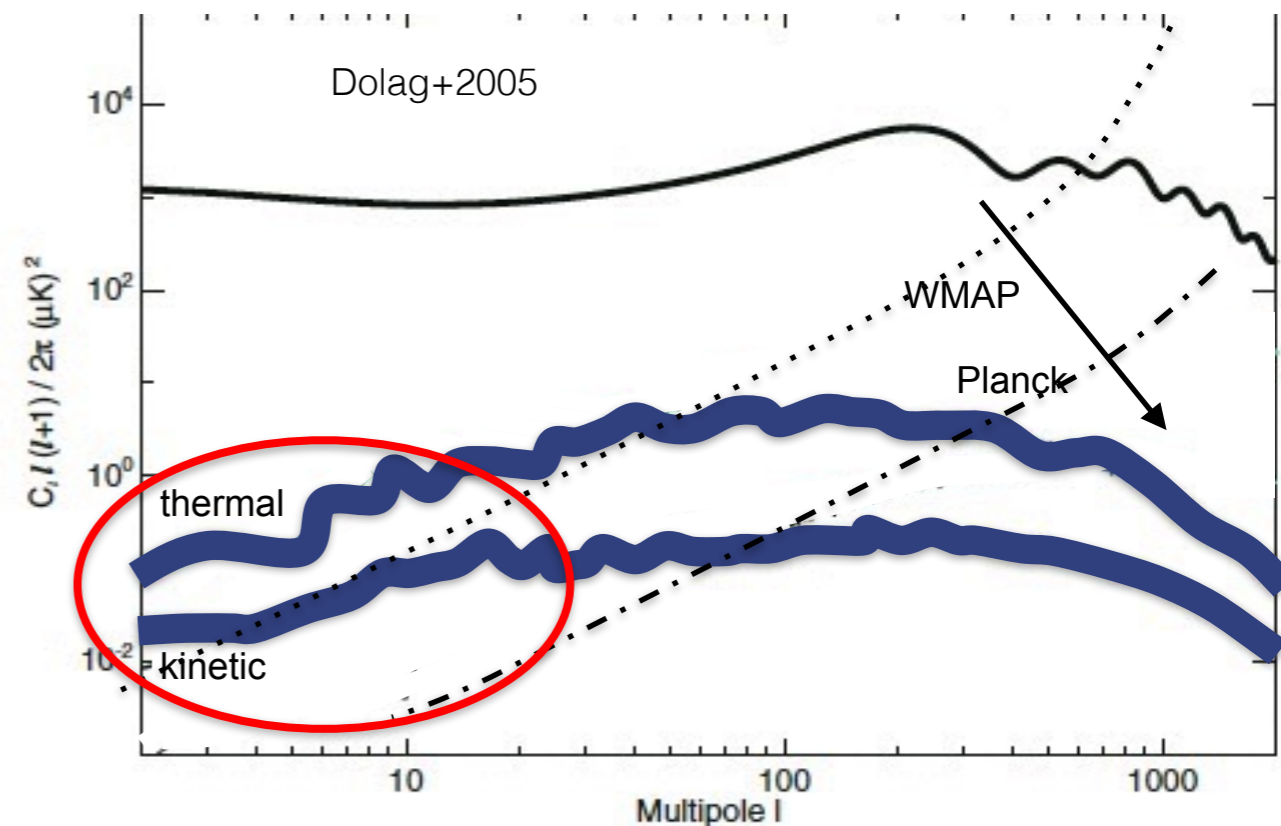
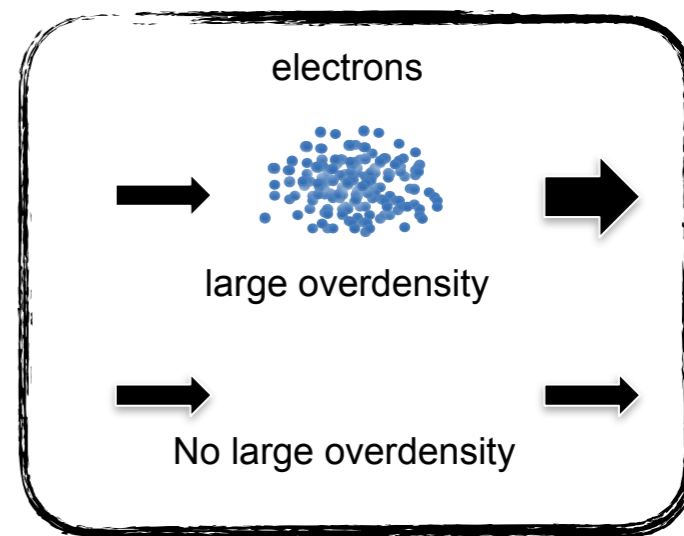
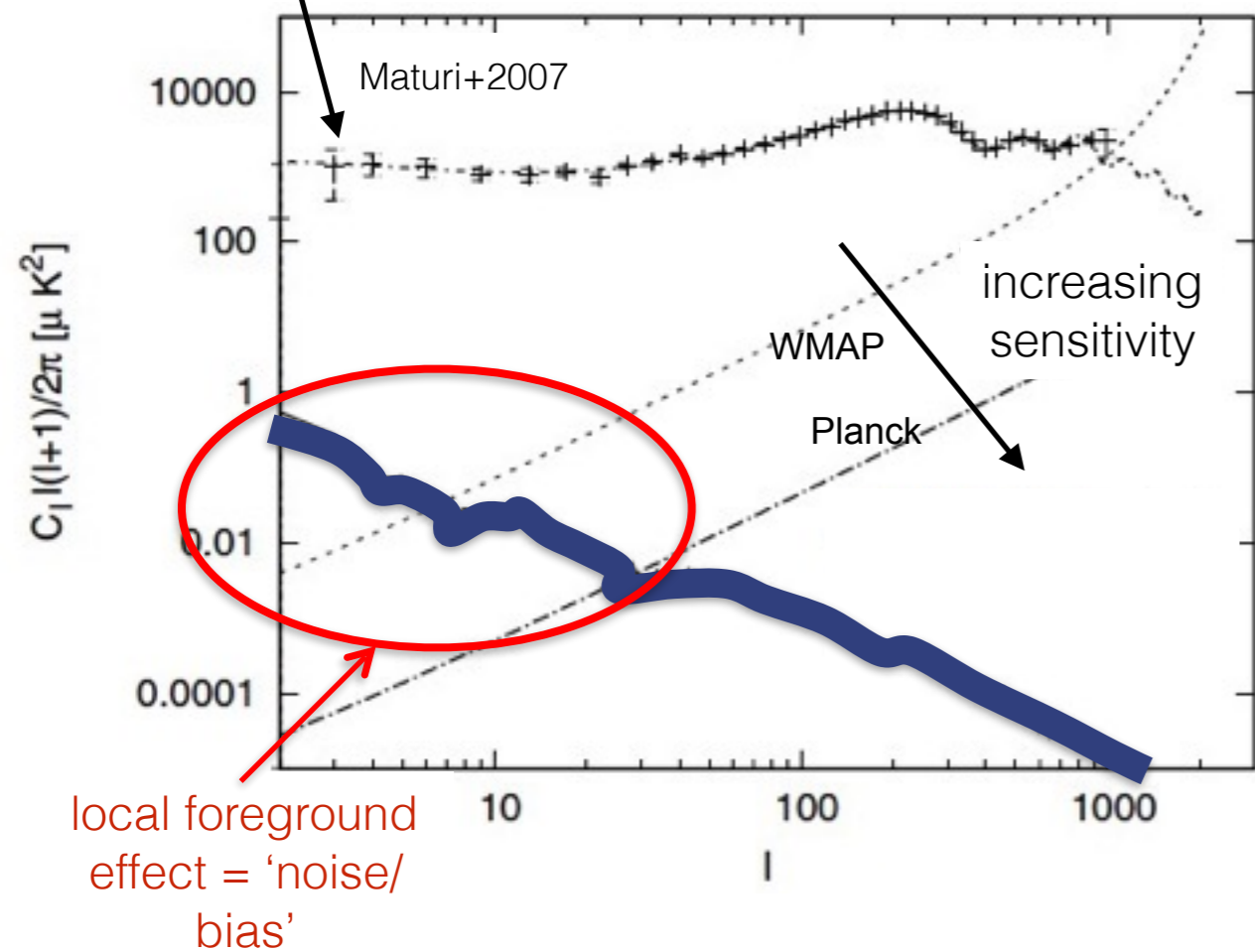


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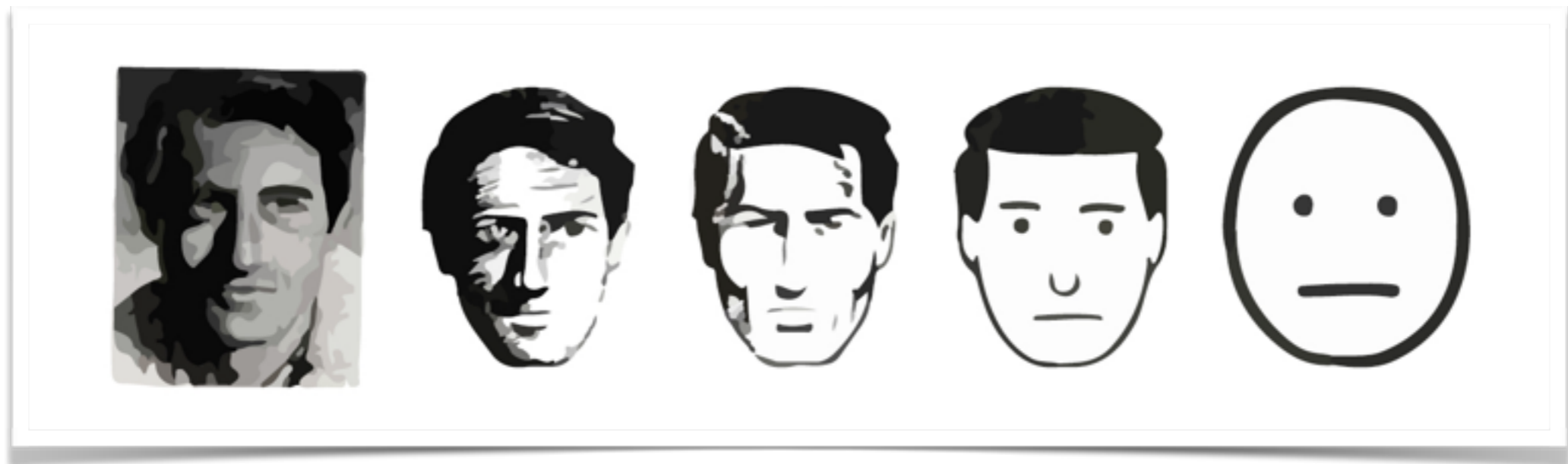
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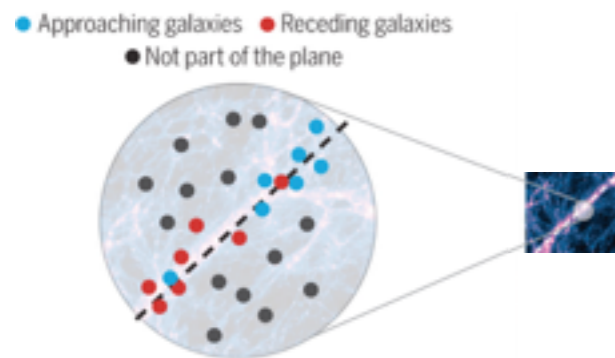
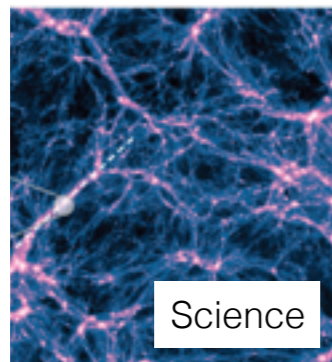
A crude modeling is a beginning...



but not nearly enough...

Accounting for the effects crude modeling

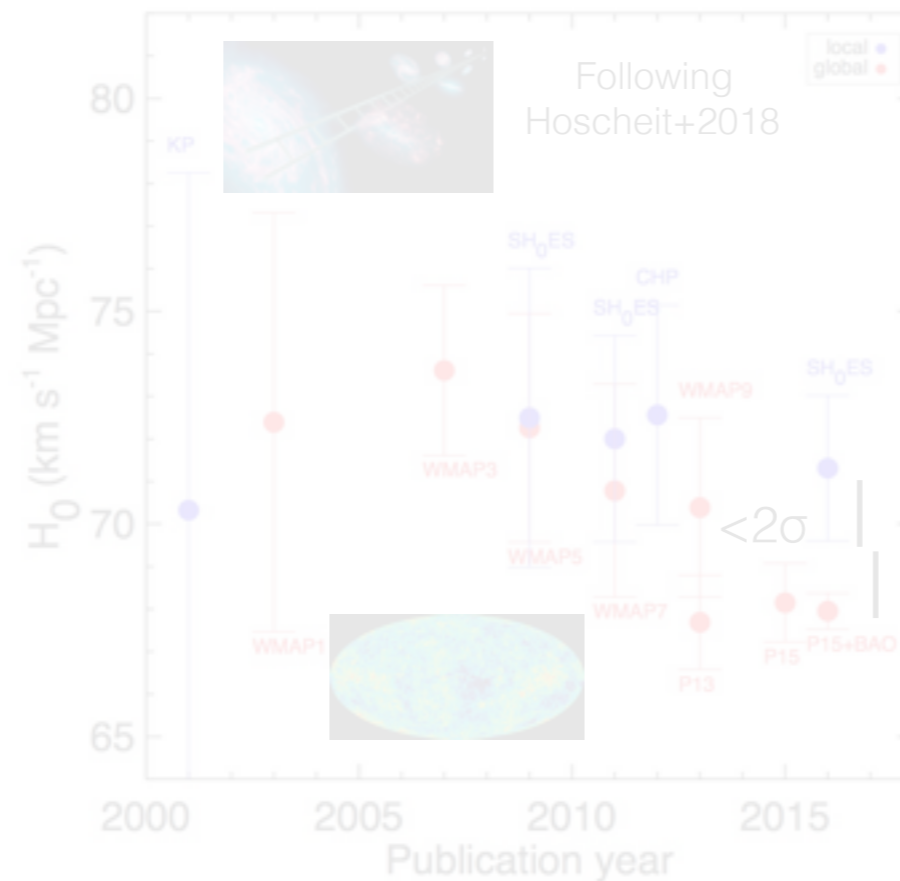
Small scales



Do we live in a filament that reproduces exactly that thin plane?

A few examples

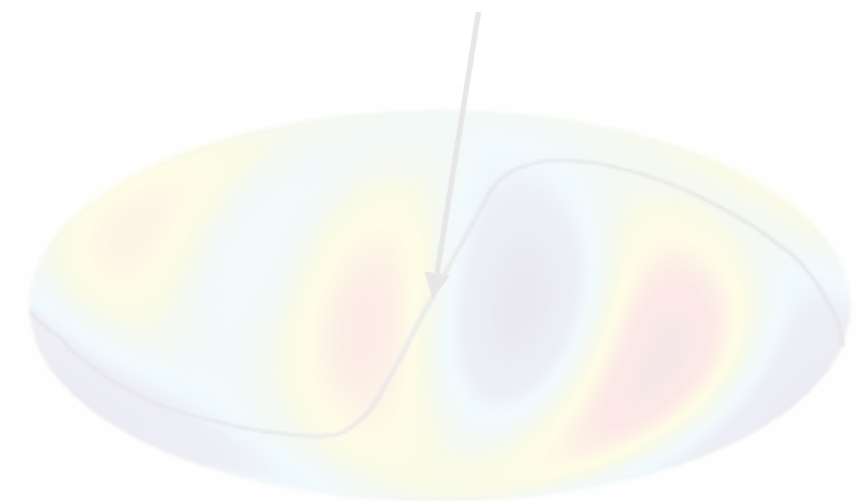
Local scales



In what kind of density do we live exactly?

Large scales

broken North/South asymmetry



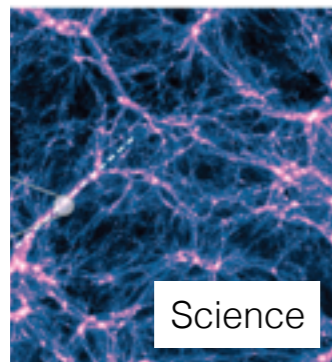
Francis+2010

But correction from redshift surveys only...

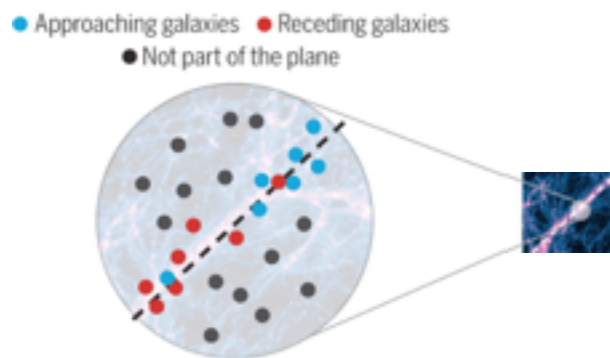
Accounting for the effects crude modeling

A few examples

Small scales

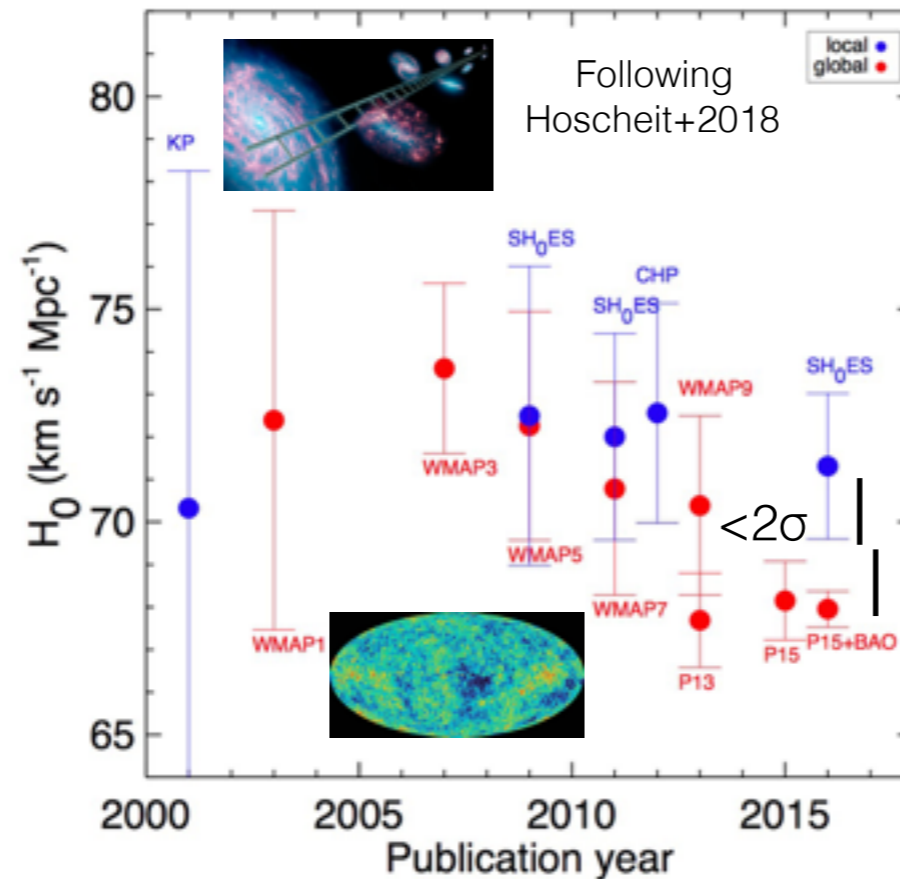


Science



Do we live in a filament that reproduces exactly that thin plane?

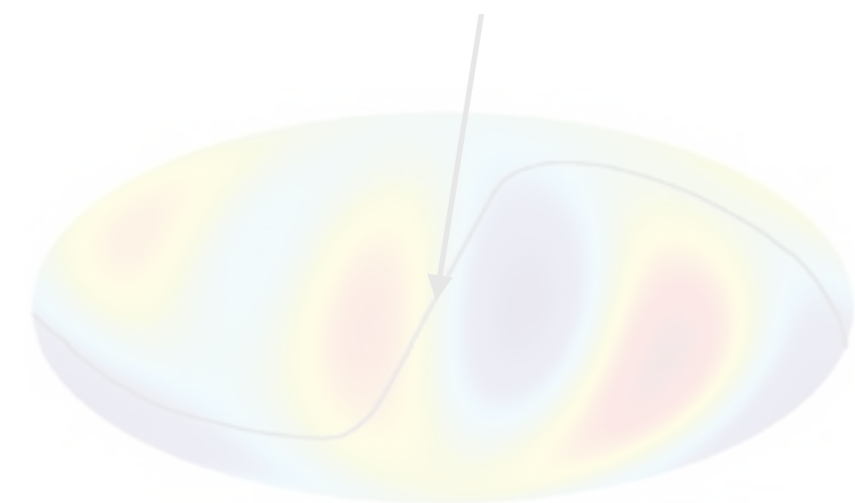
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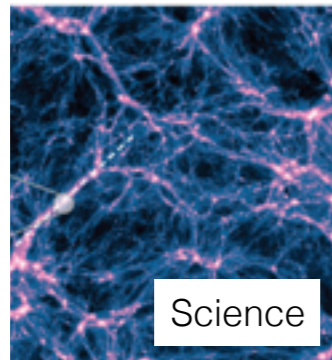


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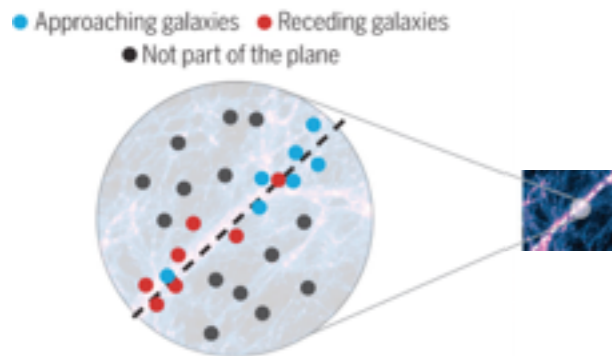
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A few examples

Small scales

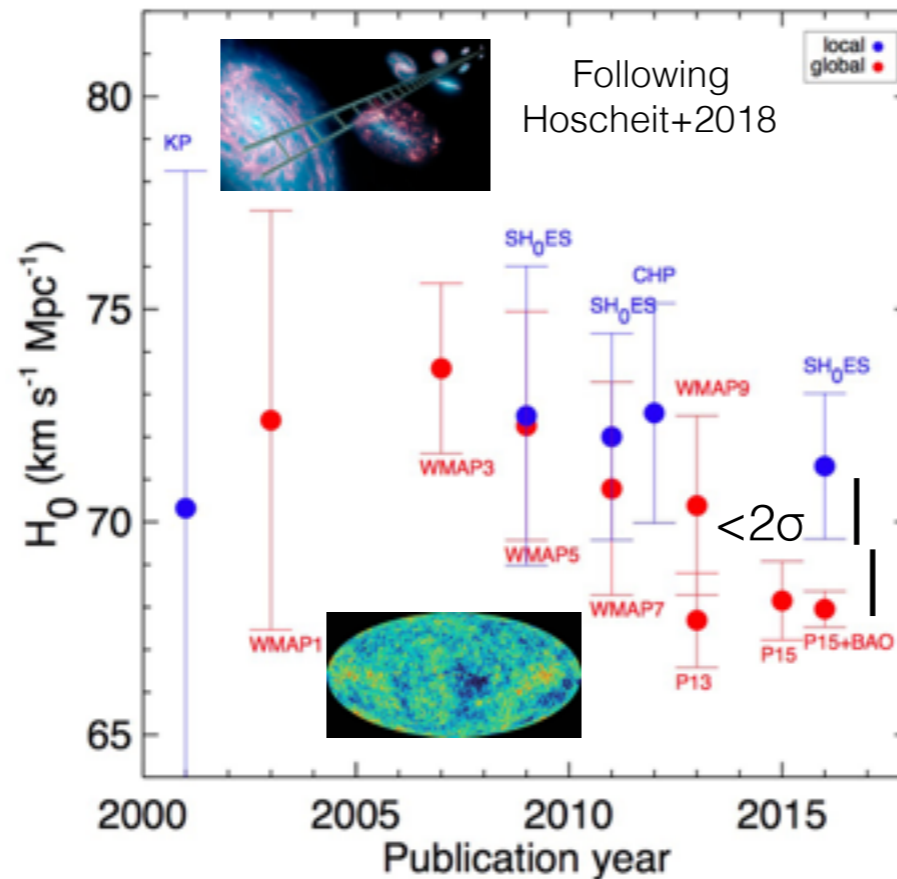


Science



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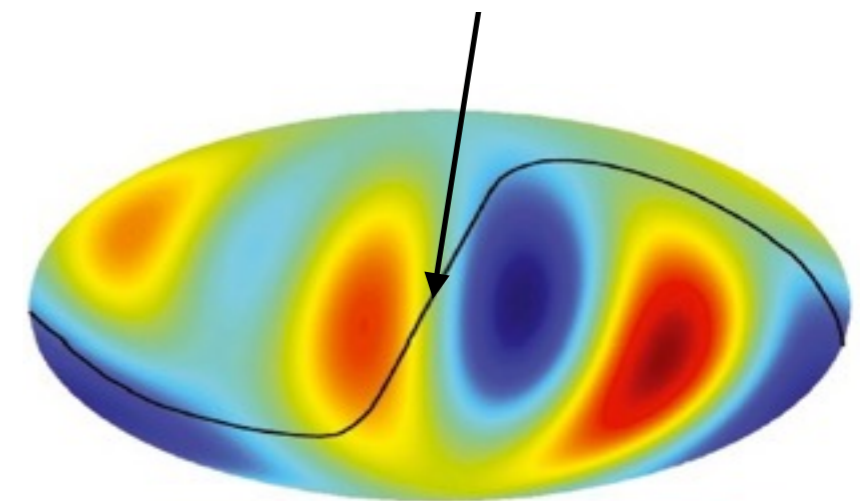
Local scales



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But correction from redshift surveys only...

Importance of our local environment !

We need a very acute knowledge of the total *local* distribution of matter (map)

to reach an accurate precision cosmology:

- **on the small scale: compare apple to apple**
- **on the local scale: become a neutral observer**
- **on the large scale: correct for foreground effects**

Importance of our local environment !

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Observations

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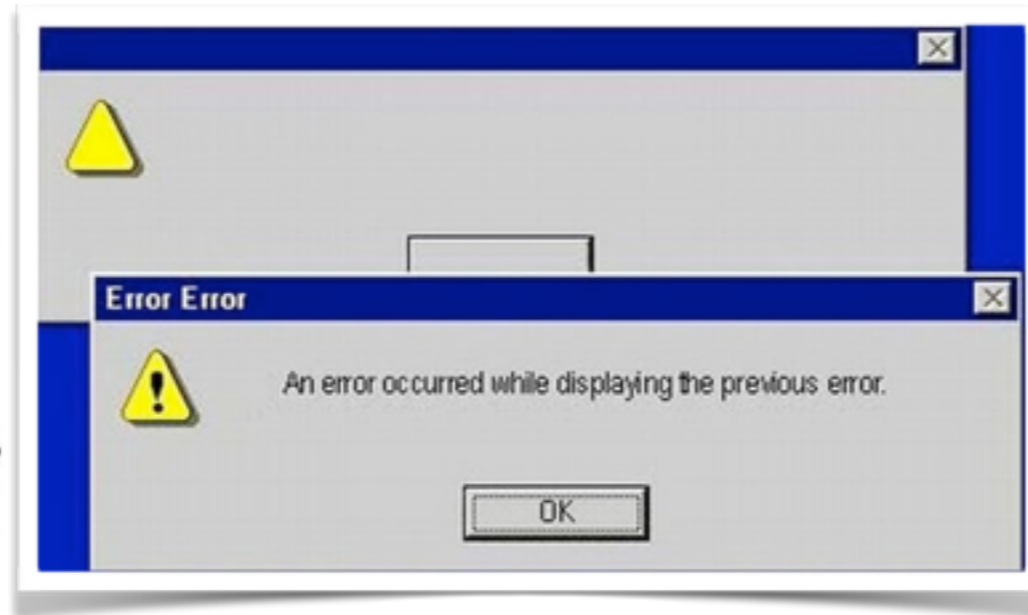
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Initial conditions of the local Universe

Obtaining the initial conditions of the local Universe



Local Universe's initial conditions ▶ constrained initial conditions

PATH INTEGRAL METHODS FOR PRIMORDIAL DENSITY PERTURBATIONS: SAMPLING OF CONSTRAINED GAUSSIAN RANDOM FIELDS

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ABSTRACT

Path integrals may be used to describe the statistical properties of a random field such as the primordial density perturbation field. In this framework the probability distribution is given for a Gaussian random field subjected to constraints such as the presence of a protovoid or supercluster at a specific location in the initial conditions. An algorithm has been constructed for generating samples of a constrained Gaussian random field on a lattice using Monte Carlo techniques. The method makes possible a systematic study of the density field around peaks or other constrained regions in the biased universe. The method is effective for generating initial conditions for N -body simulations with rare objects in the computational volume

Bayes1761 Wiener1942 Hoffman & Ribak 1991 Zaroubi+1995 van der Weijgaert & Bertshinger 1996

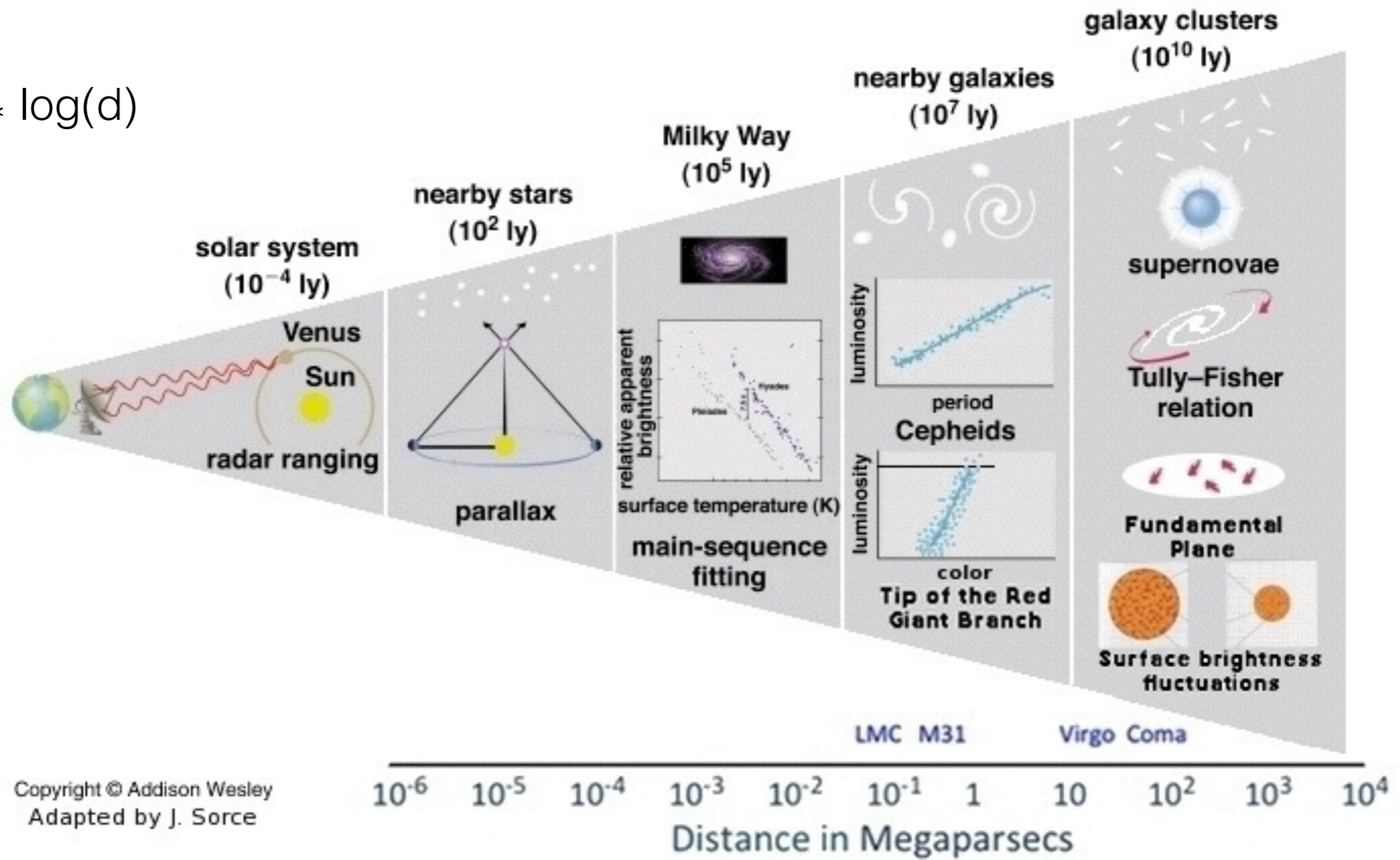
Work	Constraints	Redshift surveys	peculiar velocities + density	peculiar velocities
Kitaura2008,2012, 2013 Hess+2013		☑		
Lavaux2010, Jasche+2013-tdy		☑		
Wang+2014-tdy		☑		
Klypin+2003			☑	
Sorce+2014-tdy				☑



"This identical twin of yours... Can you describe him?"

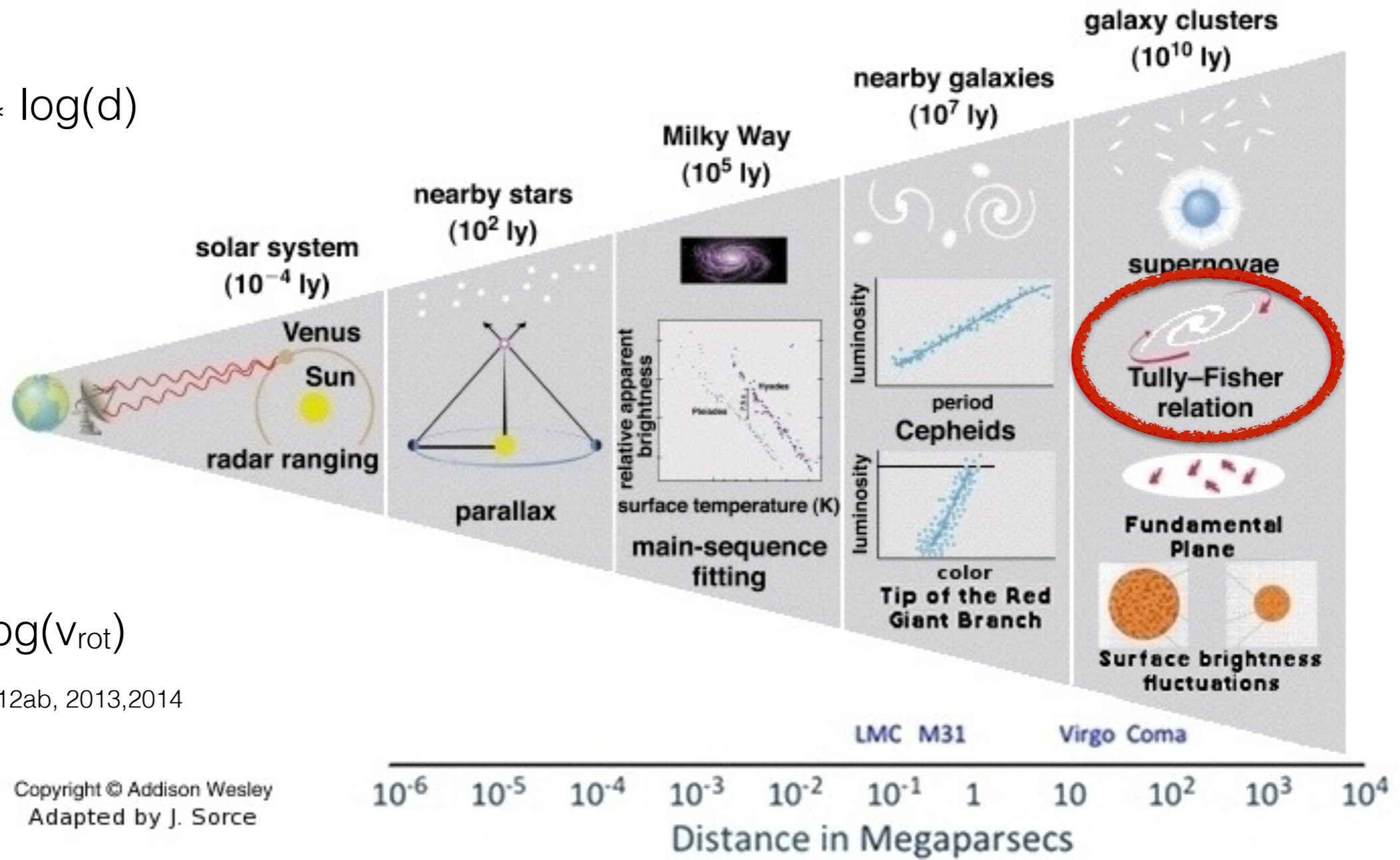
no luminosity bias →

$$m-M \propto \log(d)$$



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Adapted by J. Sorce

$$m-M \propto \log(d)$$

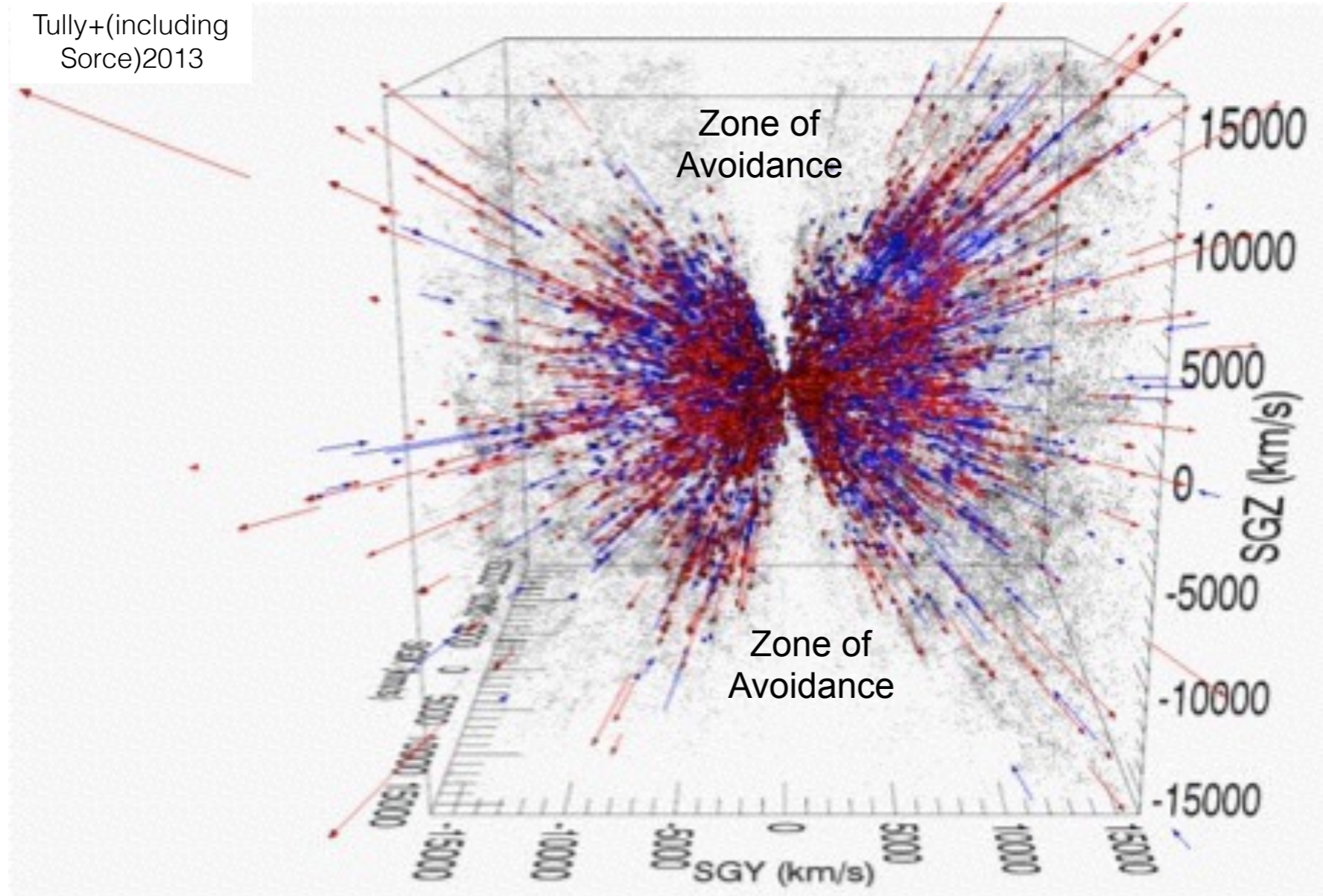


$$M \propto \log(v_{\text{rot}})$$

e.g. Sorce+2012ab, 2013,2014

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$$V_{\text{radial pec}} = V_{\text{obs}} - H_0 \times d$$



- Account for the entire underlying gravitational field
- Correlated on large scale
- Highly linear

Method

Radial peculiar velocity catalog

Grouping

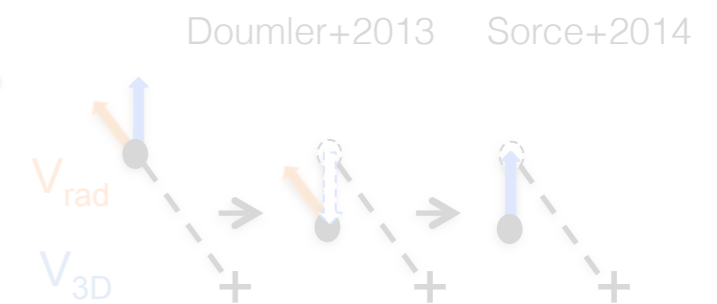
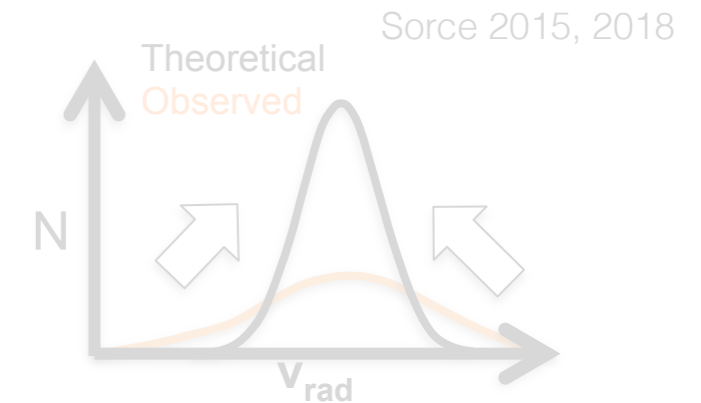
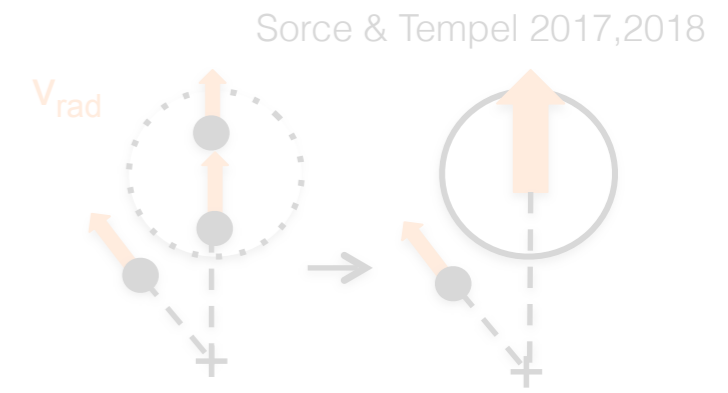
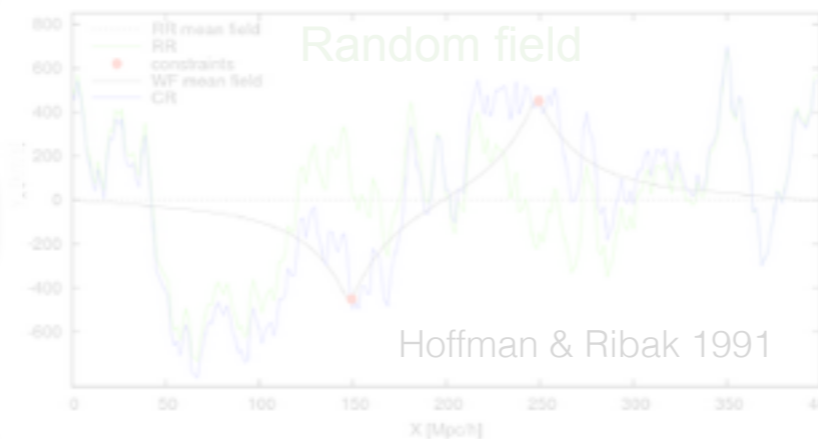
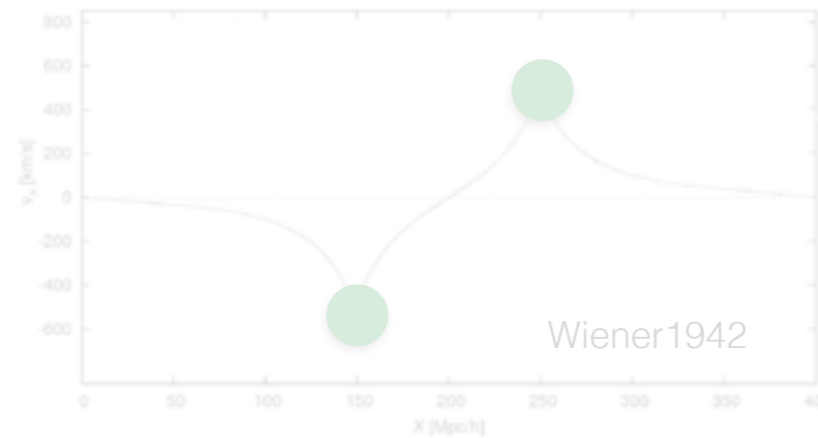
Minimization of biases

Wiener filtering

Reverse Zel'dovich Approximation

Constrained realization

Constrained initial conditions



Method

Radial peculiar velocity catalog

Grouping

Minimization of biases

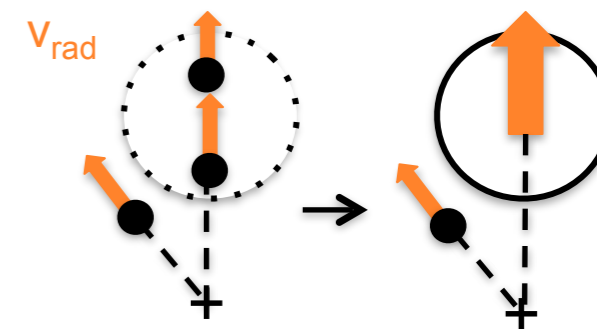
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Sorce & Tempel 2017, 2018



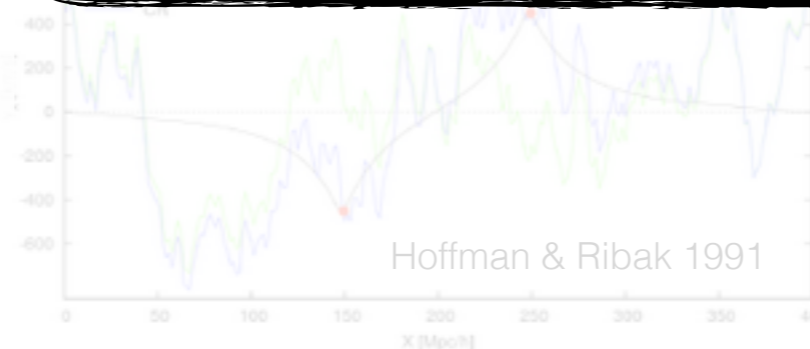
Distance (modulus) of the group and its uncertainty

$$\mu_g = \frac{\sum w \times \mu}{\sum w} ; \sigma_{\mu g} = \sqrt{\frac{1}{\sum w}} \text{ where } w = \frac{1}{\sigma_{\mu}^2},$$

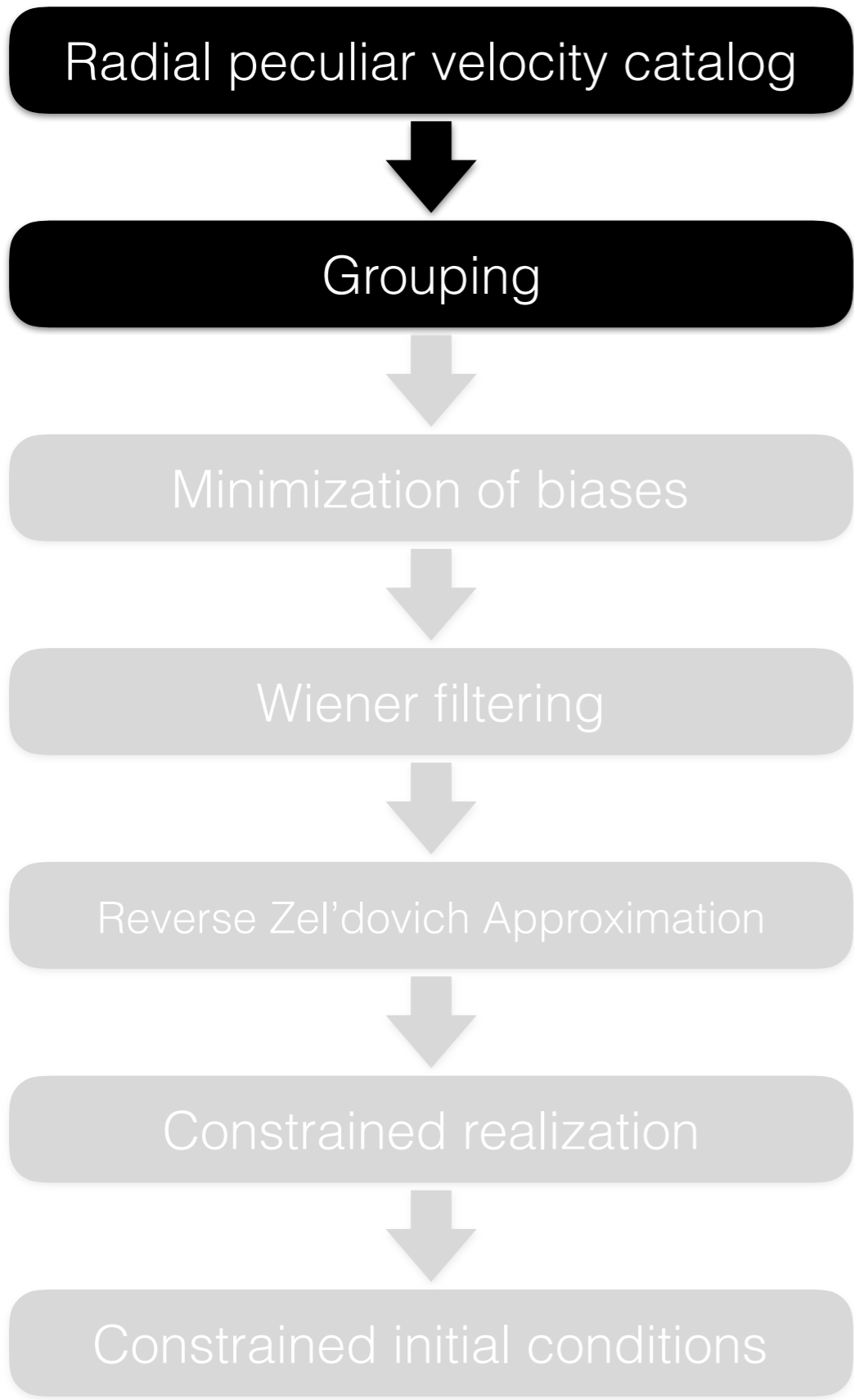
$$d_g = 10^{\frac{\mu_g - 25}{5}} ; \sigma_{d_g} = \sigma_{\mu g} \times \frac{\log(10)}{5}$$

Peculiar velocity of the group and its uncertainty

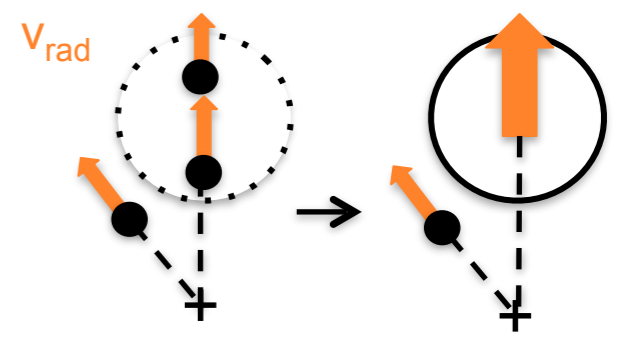
$$v_{\text{pec } g} = v_{\text{tot } g} - H_0 \times d_g ; \sigma_{v_{\text{pec } g}} = \sigma_{d_g} \times d_g \times H_0$$



Method



Sorce & Tempel 2017, 2018

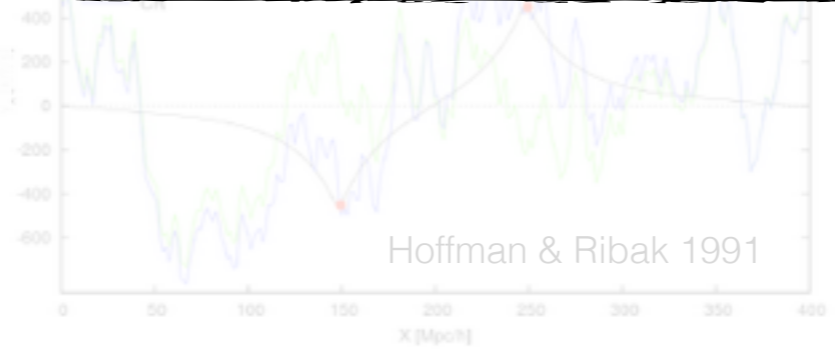


Distance (modulus) of the group and its uncertainty

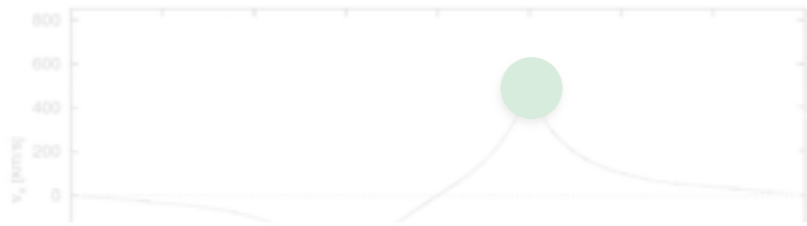
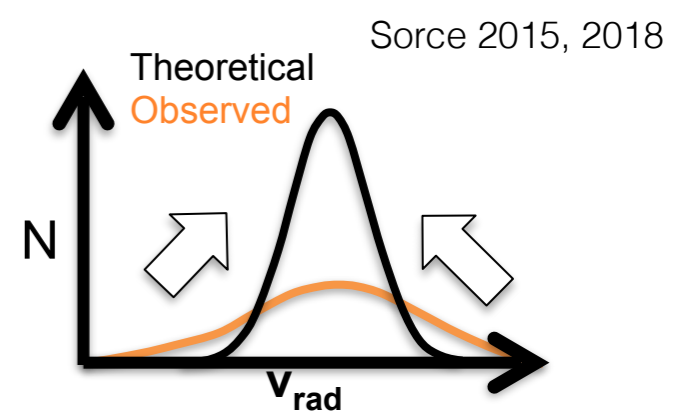
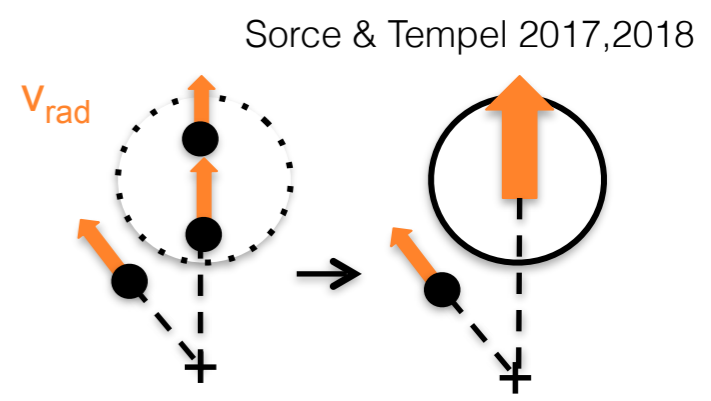
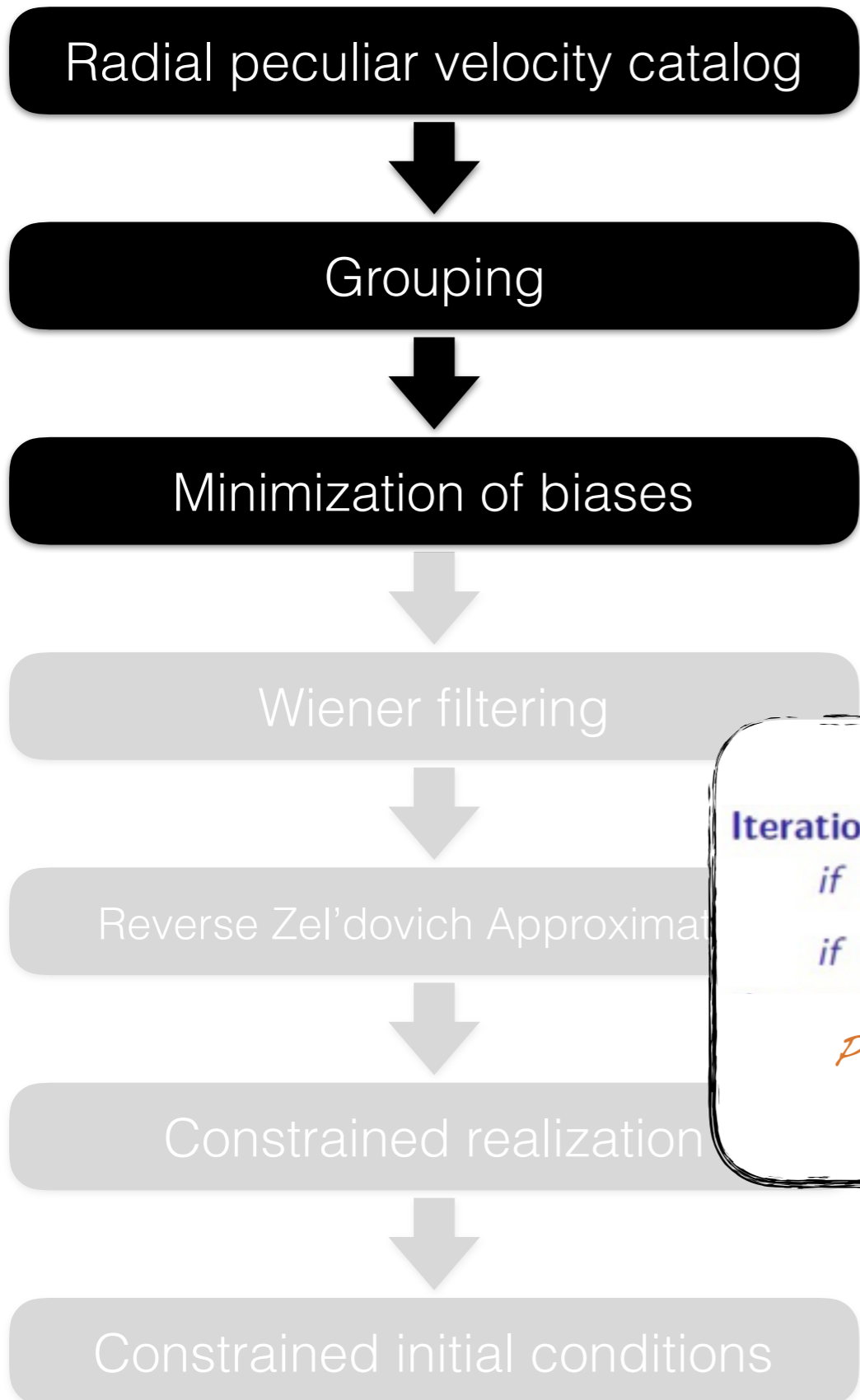
$$\mu_g = \frac{\sum w \times \mu}{\sum w}; \quad \sigma_{\mu g} = \sqrt{\frac{\sum w \times \mu^2}{\sum w} - \left(\frac{\sum w \times \mu}{\sum w}\right)^2}$$

The biggest difficulty is to determine the groups!

Peculiar velocity of the group and its uncertainty

$$v_{pec\ g} = H_0 \times d_g; \quad \sigma_{v_{pec\ g}} = \sigma_{d_g} \times d_g \times H_0$$


Method



Corrected peculiar velocities

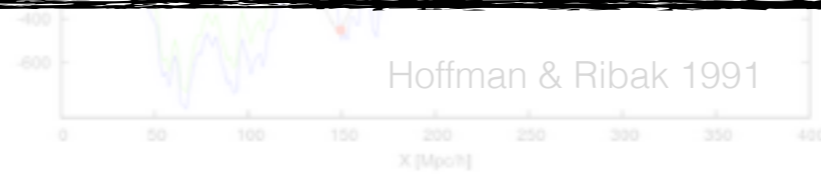
Iterations on:

if $v_{pec} > 0$, $v_{pec c} = (1 - w)[p(v_{pec} - \sigma_{v_{pec}}) + (1 - p)(v_{pec} + \sigma_{v_{pec}})] + w v_{pec}$

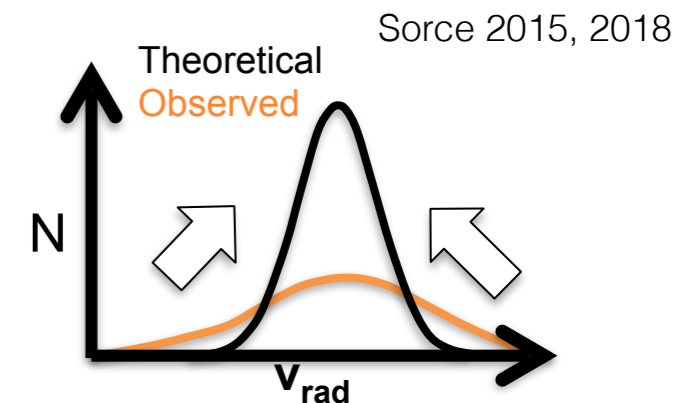
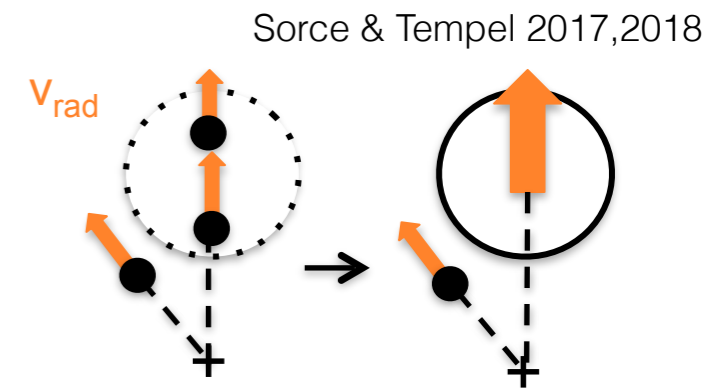
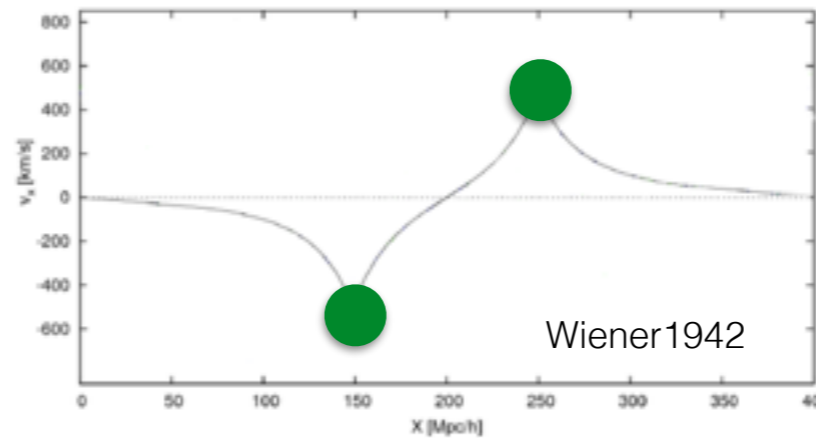
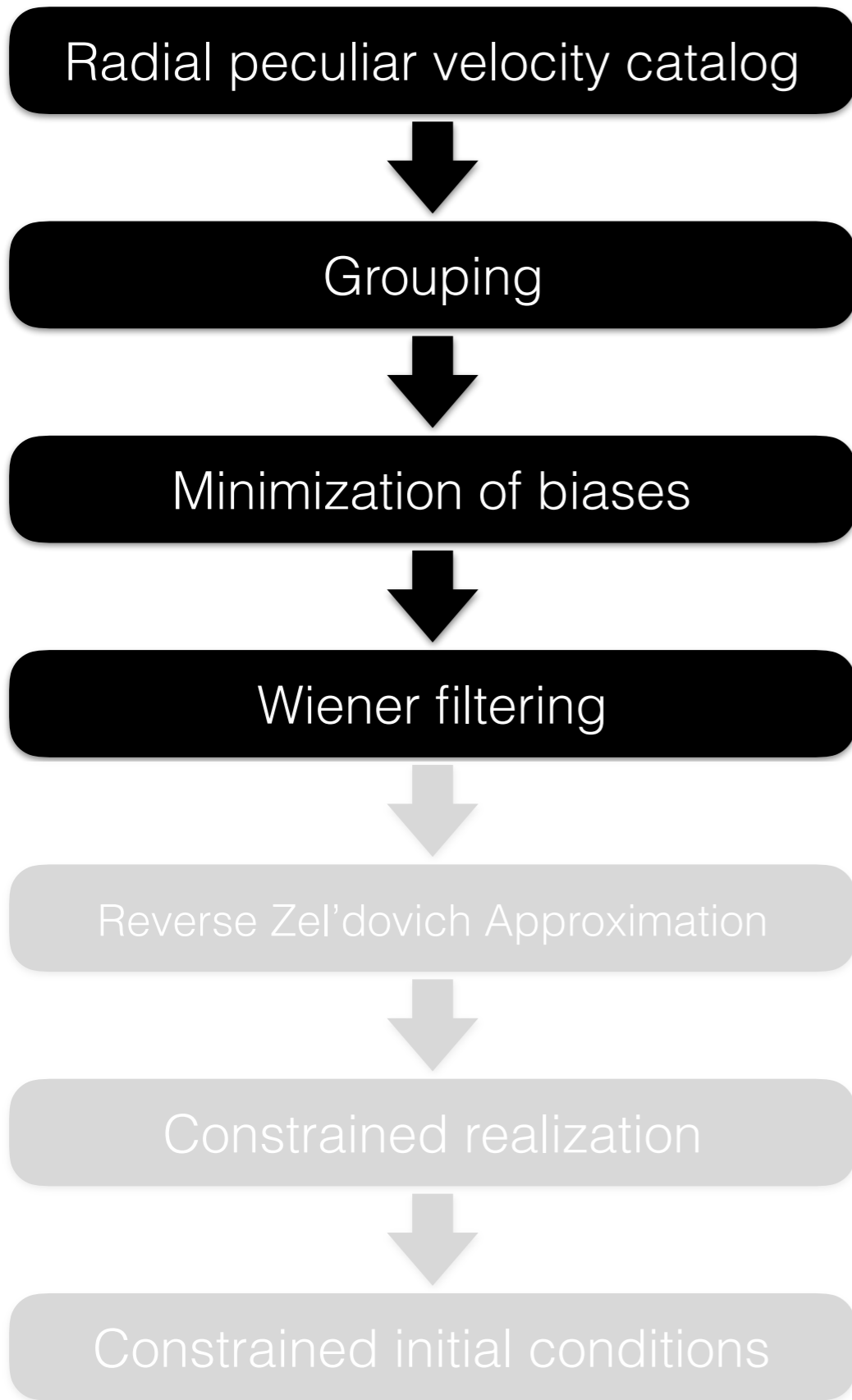
if $v_{pec} < 0$, $v_{pec c} = (1 - w)[p(v_{pec} + \sigma_{v_{pec}}) + (1 - p)(v_{pec} - \sigma_{v_{pec}})] + w v_{pec}$

Probability & Gaussian *Weighted uncertainty*

Final uncertainty $\propto d$ & $n_{constraints}$



Method



Doumler+2013 Sorce+2014

Linear minimum variance estimator

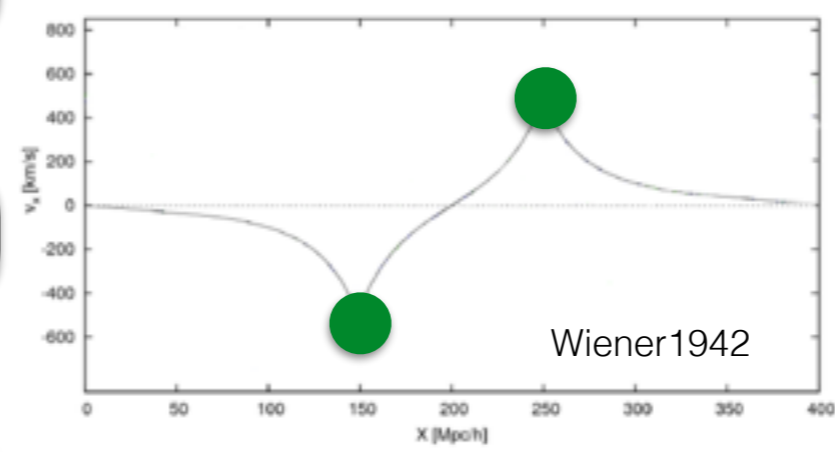
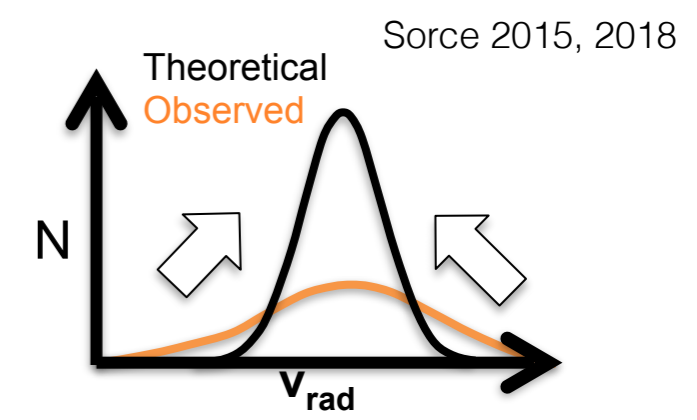
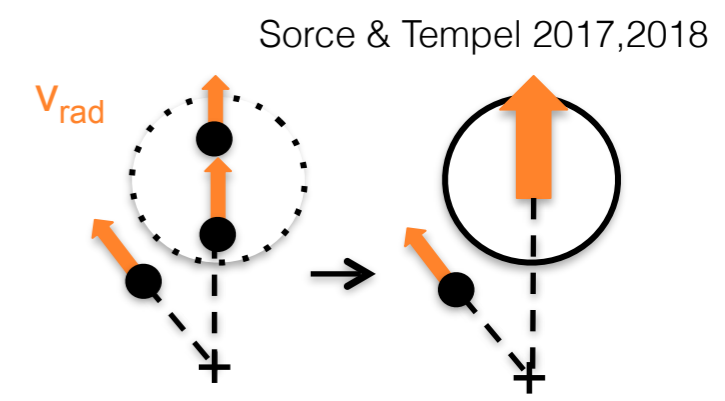
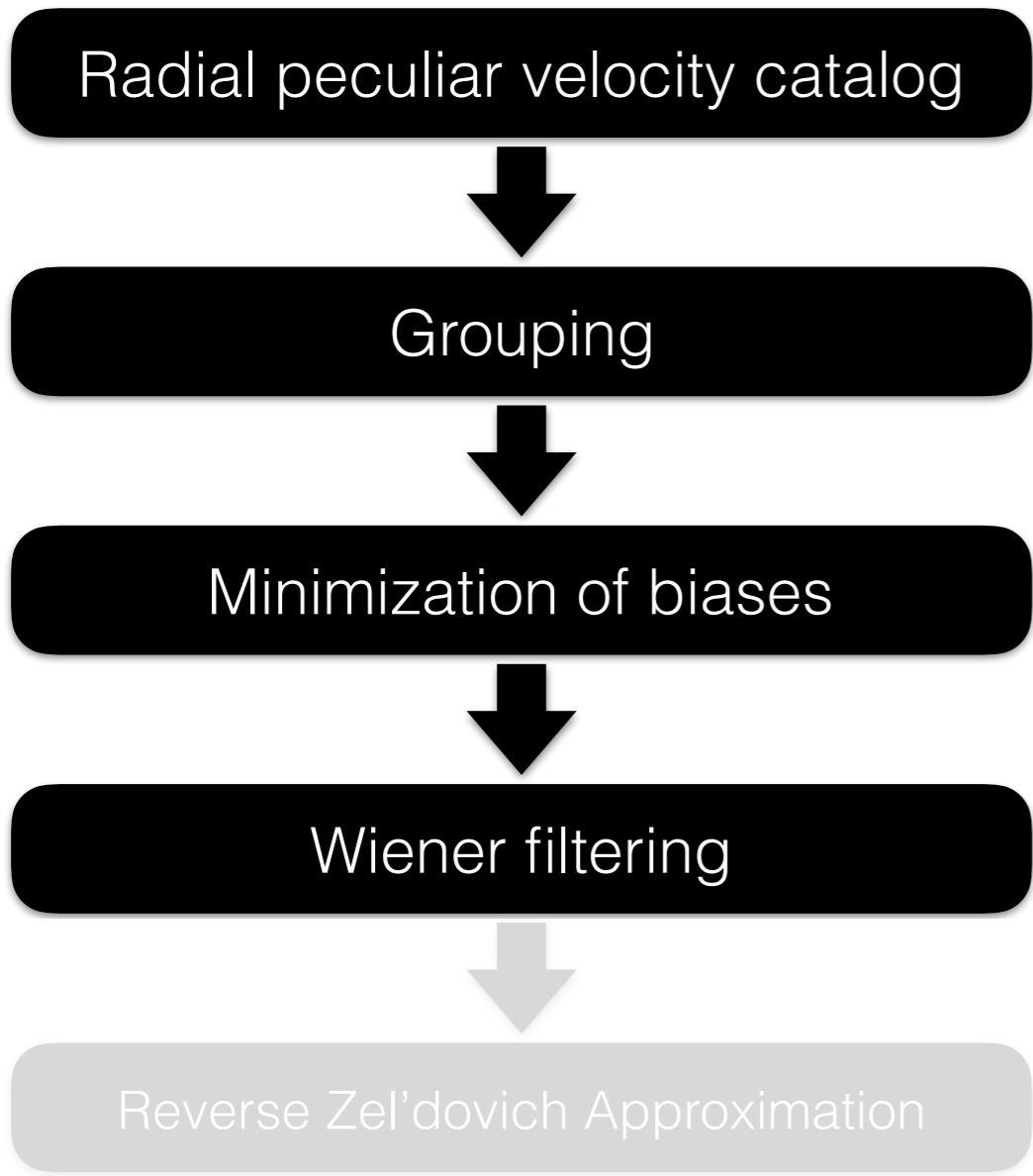
Model

$$f_i = \sum_{j=1}^n \sum_{i=1}^n \langle f_i C_i \rangle \langle C_i C_j \rangle^{-1} C_j$$

Correlation functions

Data = constraints

Method



Doumler+2013 Sorce+2014

power spectrum

$$\langle \delta(\mathbf{r}') v_\alpha(\mathbf{r}'+\mathbf{r}) \rangle = \frac{\dot{a}f}{(2\pi)^3} \int_0^\infty \frac{ik_\alpha}{k^2} P(k) e^{-ik \cdot \mathbf{r}} dk$$

$$\langle v_\alpha(\mathbf{r}') v_\beta(\mathbf{r}'+\mathbf{r}) \rangle = \frac{(\dot{a}f)^2}{(2\pi)^3} \int_0^\infty \frac{k_\alpha k_\beta}{k^4} P(k) e^{-ik \cdot \mathbf{r}} dk$$

Linear minimum variance estimator

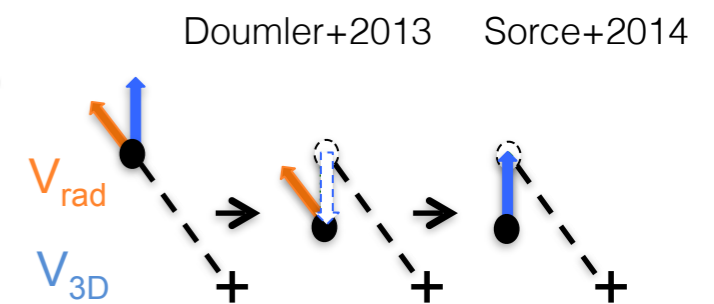
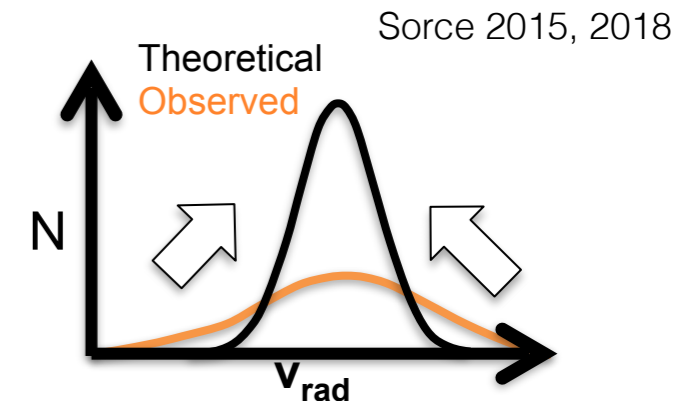
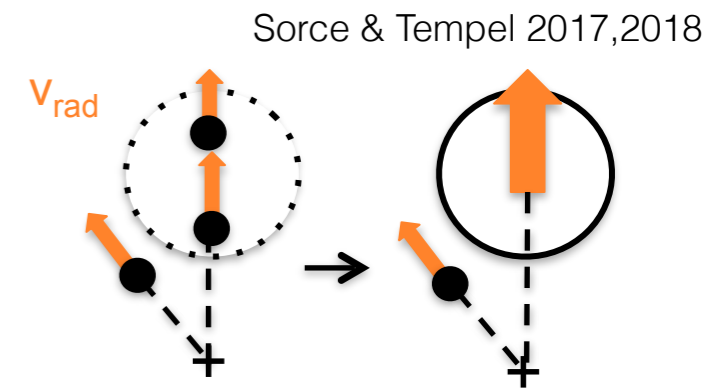
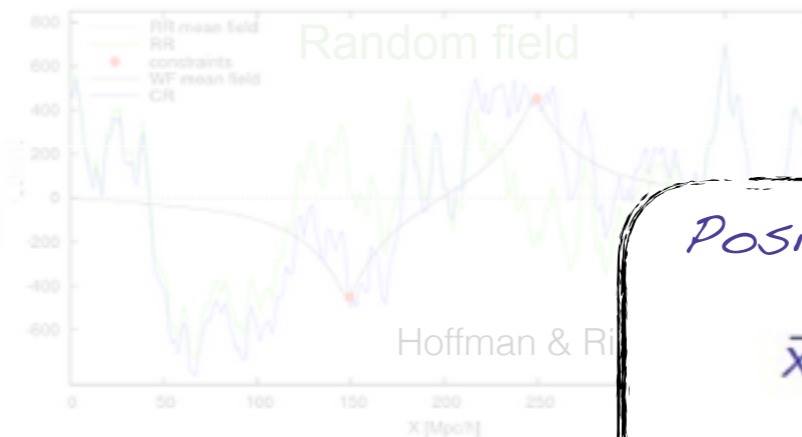
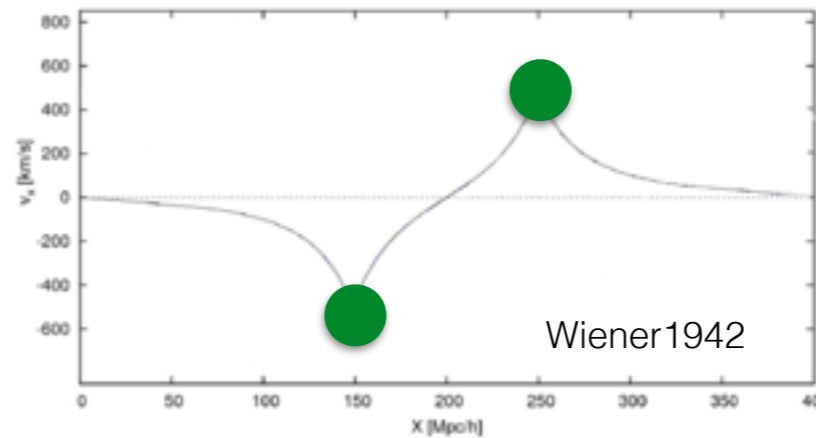
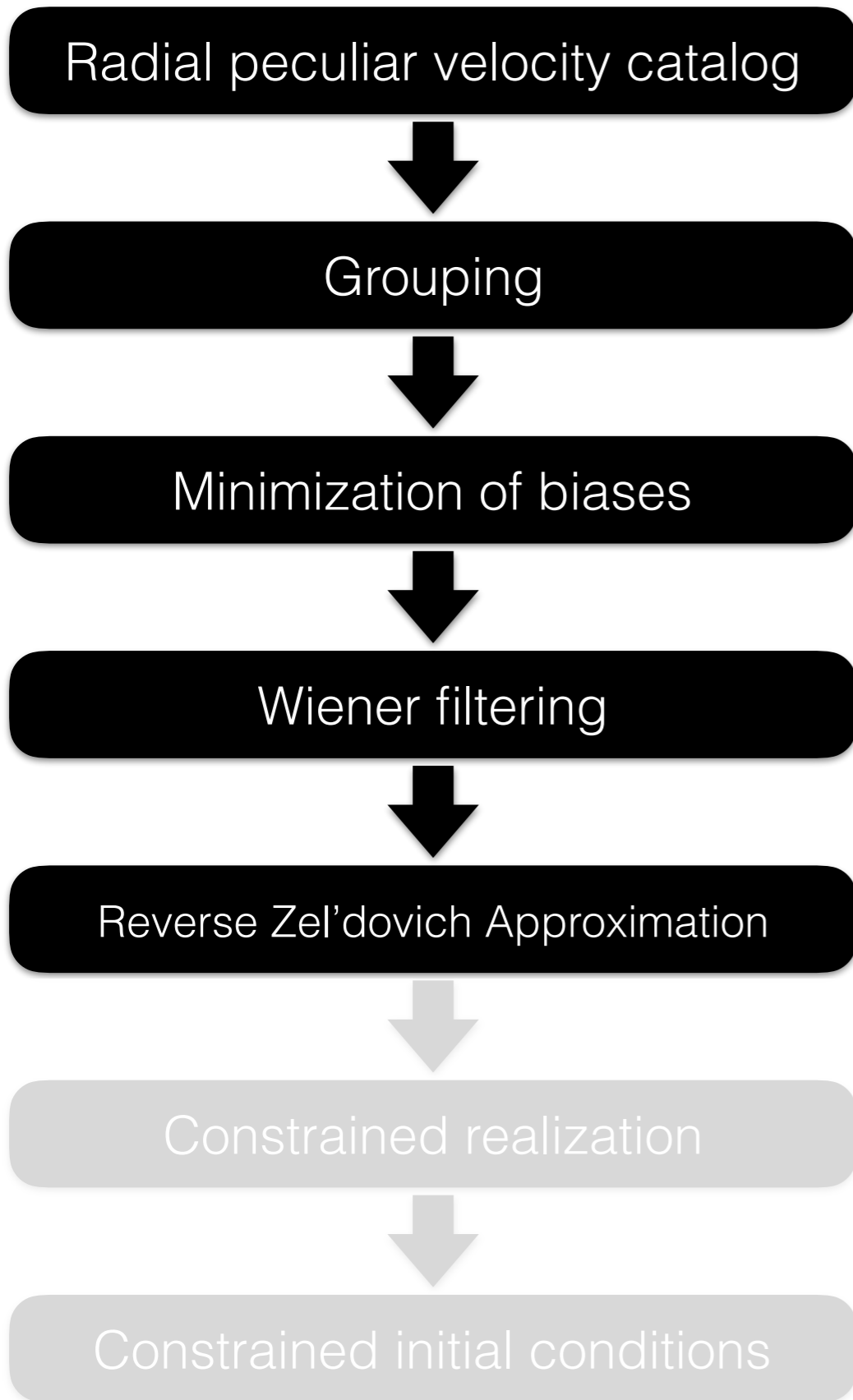
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$$f_i = \sum_{j=1}^n \sum_{i=1}^n \langle f_i C_i \rangle \langle C_i C_j \rangle^{-1} C_j$$

Data = constraints

Correlation functions

Method



Position of the progenitors

$$\vec{x}_{init}^{RZA} = \vec{r} - \frac{\vec{v}}{H_0 f(t_{init})}$$

growth rate

Method

Radial peculiar velocity catalog

Grouping

Minimization of biases

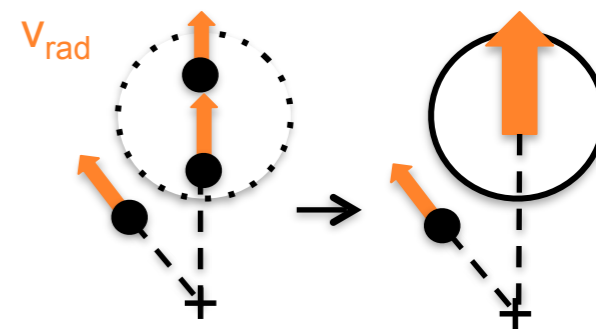
Wiener filtering

Reverse Zel'dovich Approximation

Constrained realization

Constrained initial conditions

Sorce & Tempel 2017, 2018

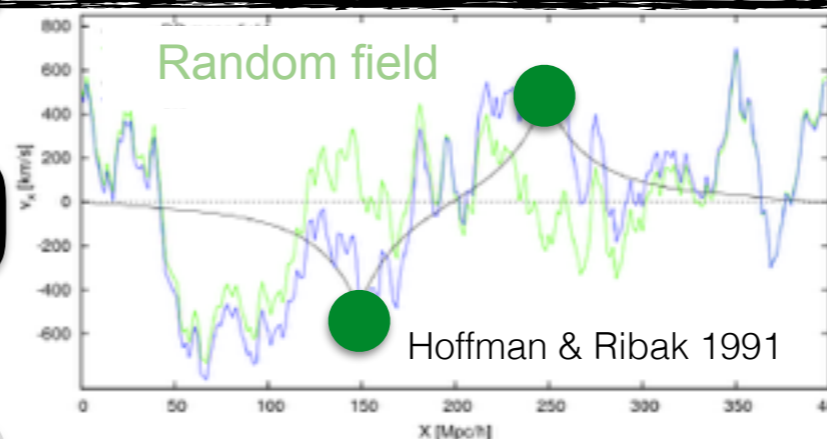


Constrained Realization: Estimate of the residual

$$\tilde{R} = \tilde{f}^{RR} - \tilde{f}^{WF} \quad \& \quad \tilde{f}^{WF} = \sum_{j=1}^n \sum_{i=1}^n \langle f_i \tilde{C}_i \rangle \langle \tilde{C}_i \tilde{C}_j \rangle^{-1} \tilde{C}_j$$

Correlation functions depend only on the model

$$f^{CR} = f^{WF} + \tilde{R} = \tilde{f}^{RR} + \sum_{j=1}^n \sum_{i=1}^n \langle f_i C_i \rangle \langle C_i C_j \rangle^{-1} (C_j - \tilde{C}_j)$$



V_{3D} + + +

Method

Radial peculiar velocity catalog

Grouping

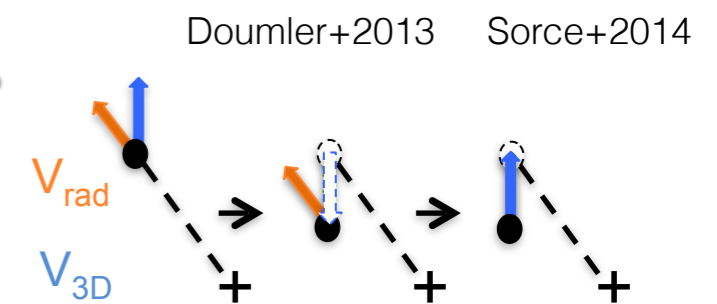
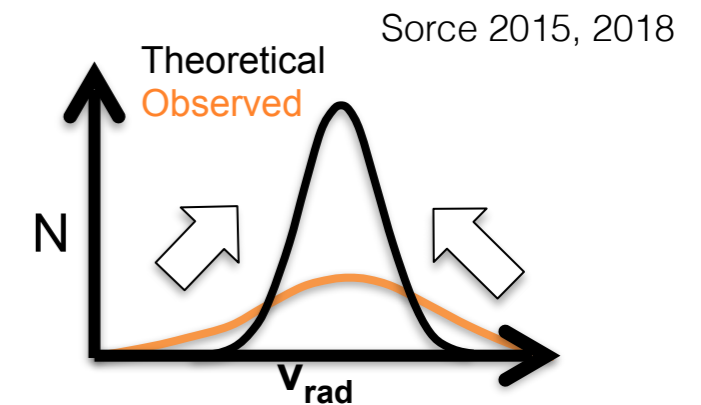
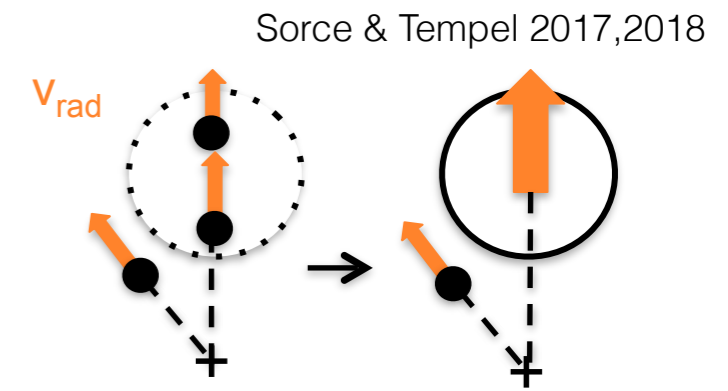
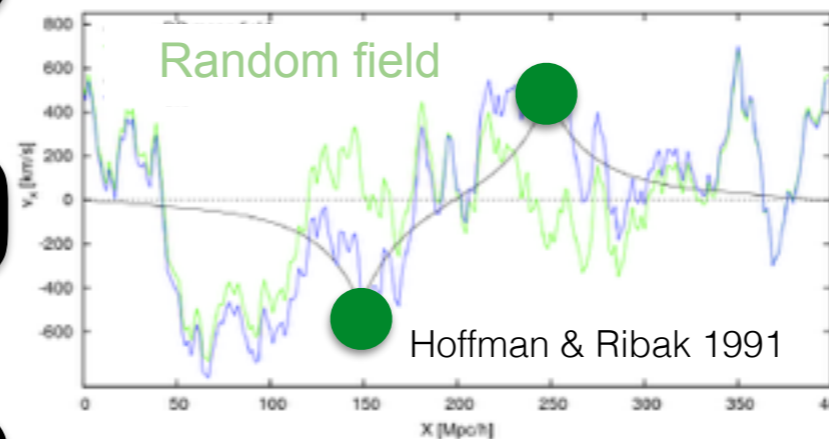
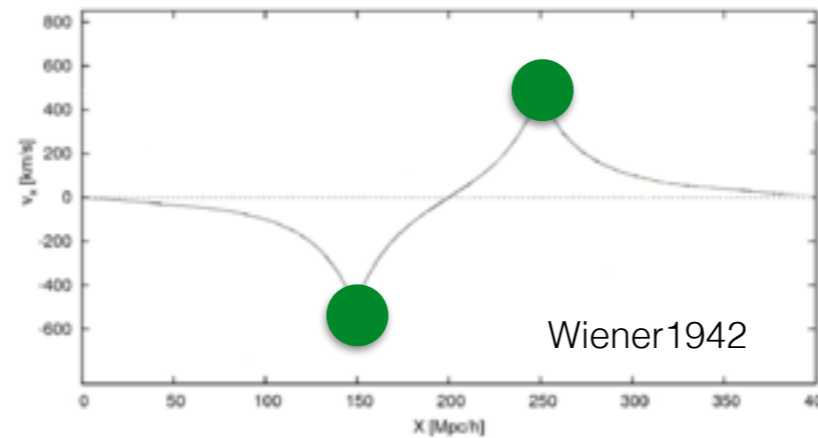
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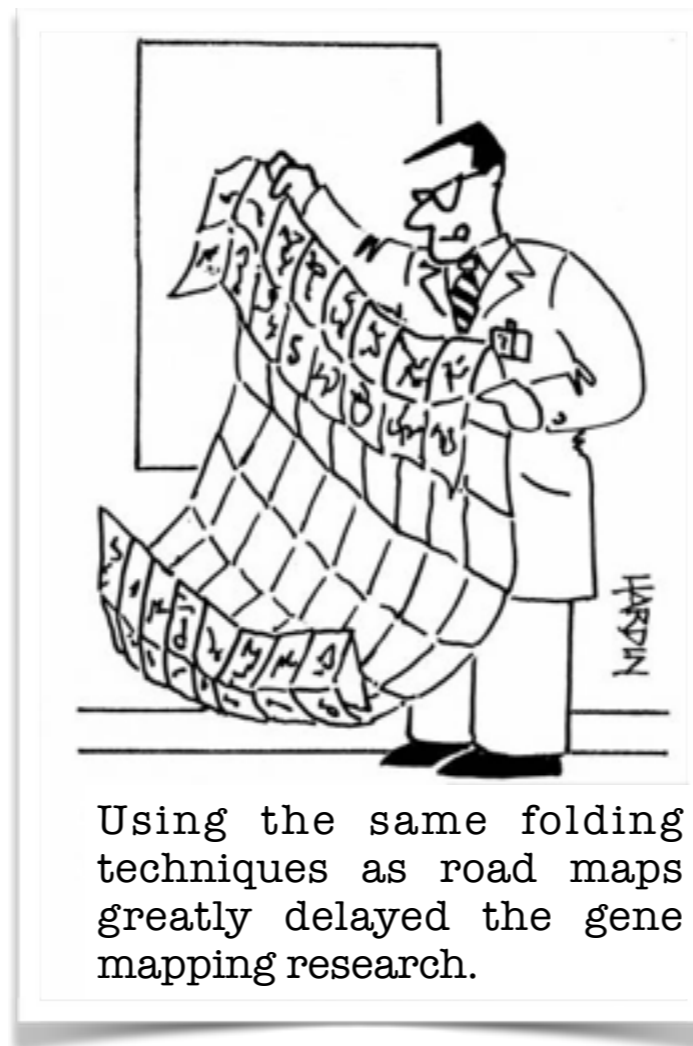
Reverse Zel'dovich Approximation

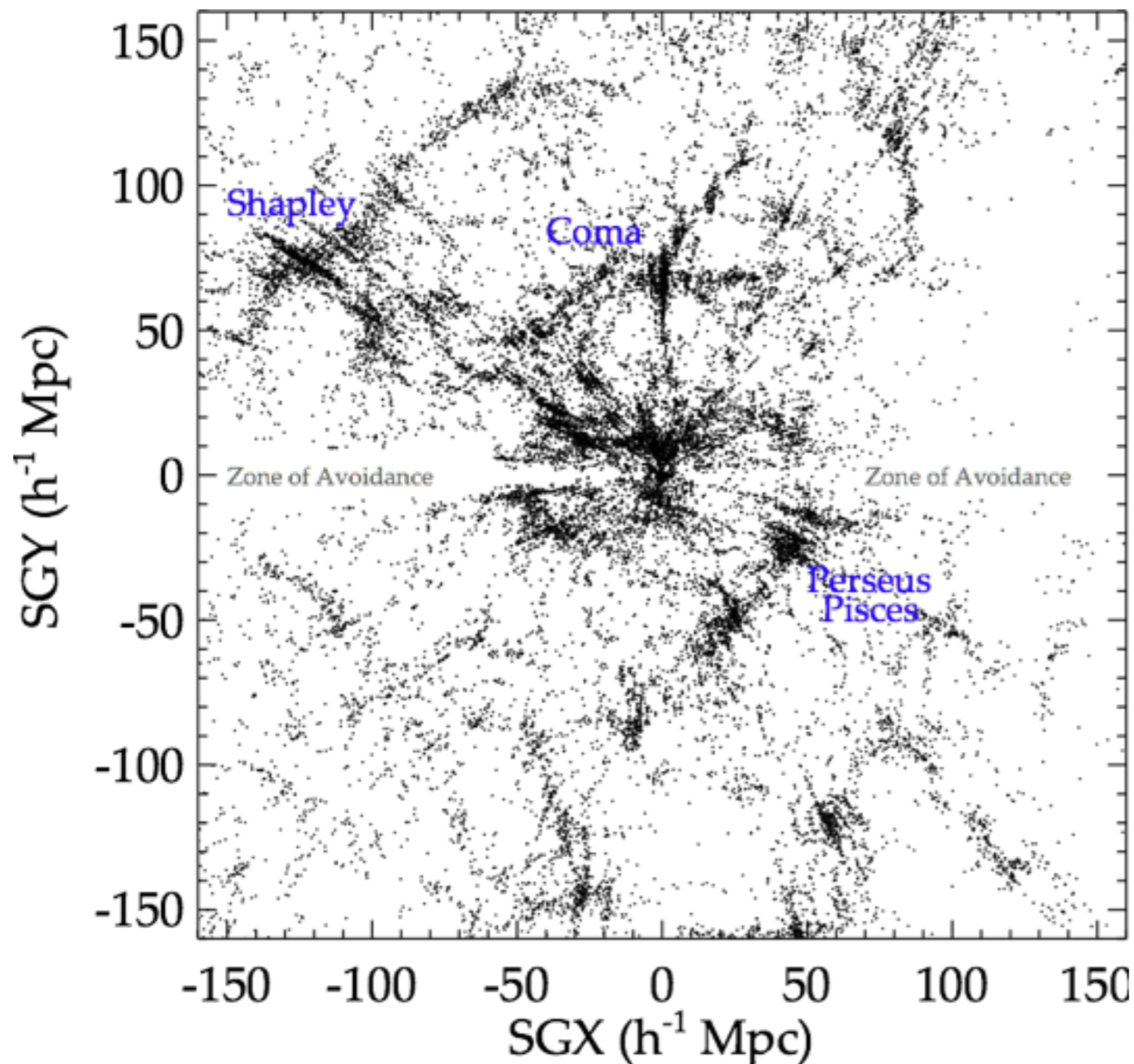
Constrained realization

Constrained initial conditions

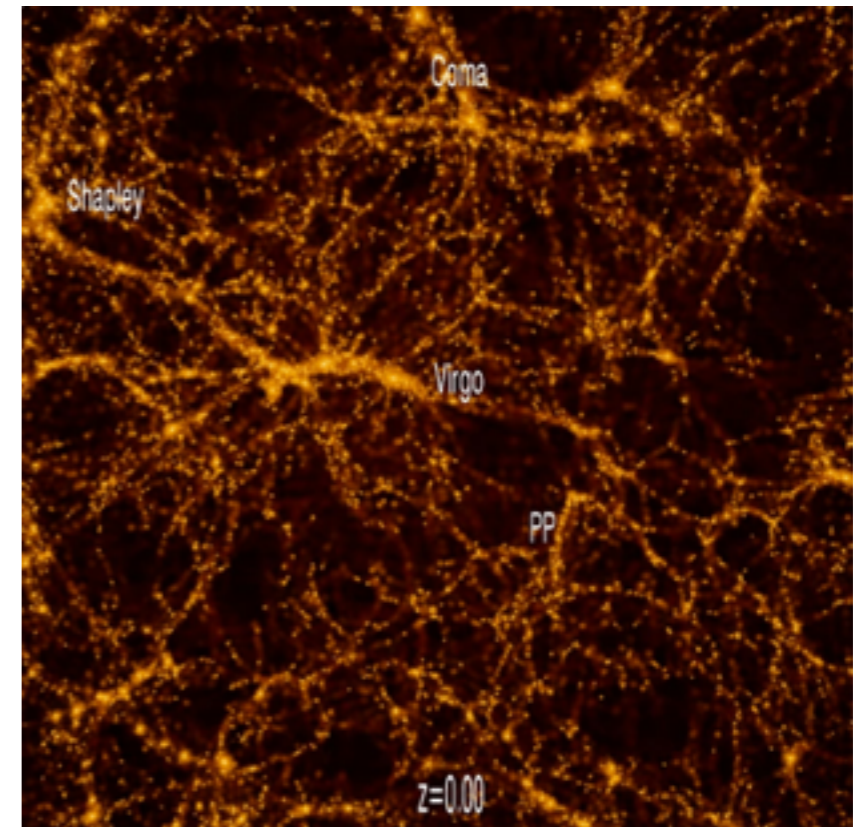


A non-linear map of the local Universe

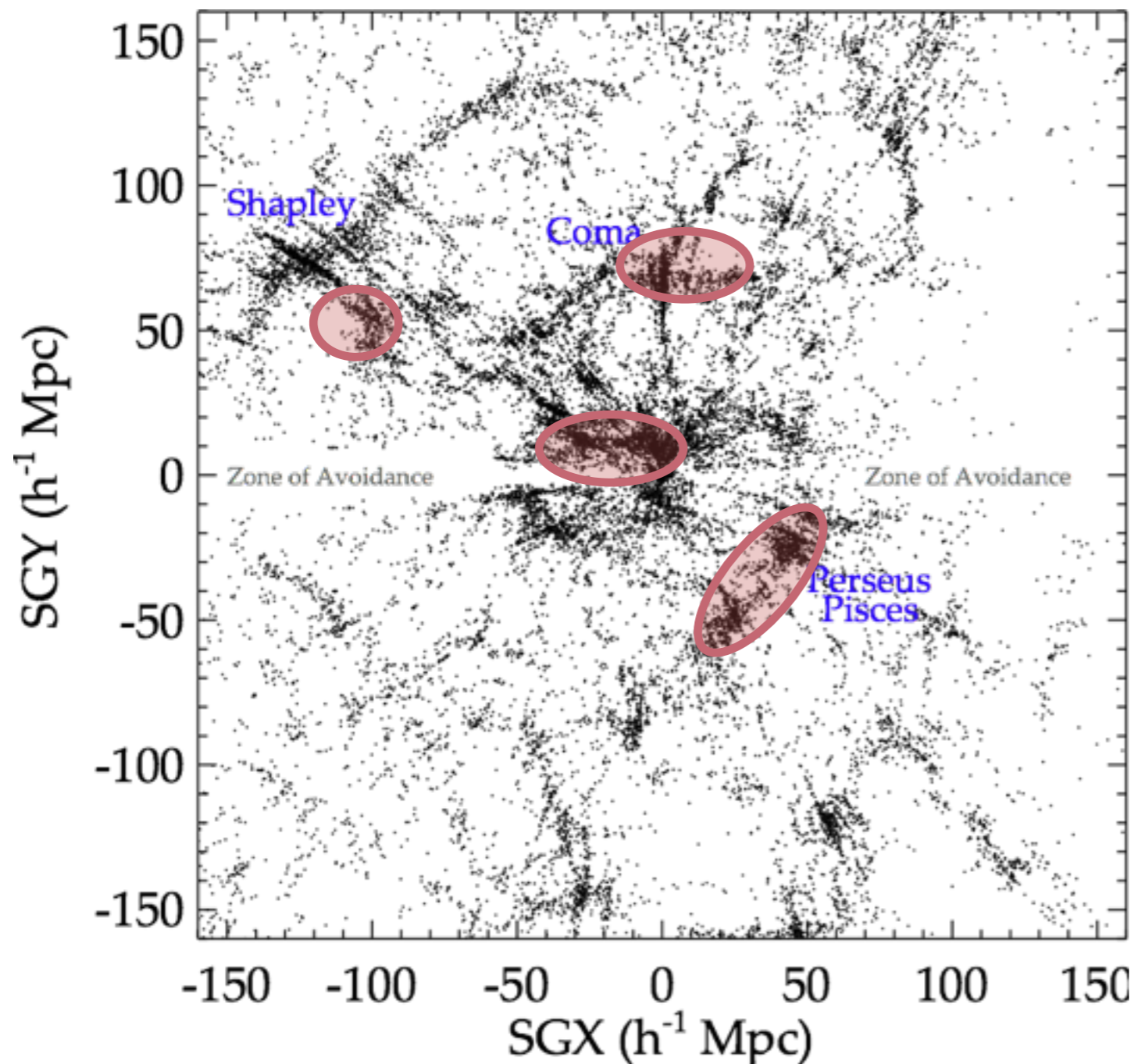




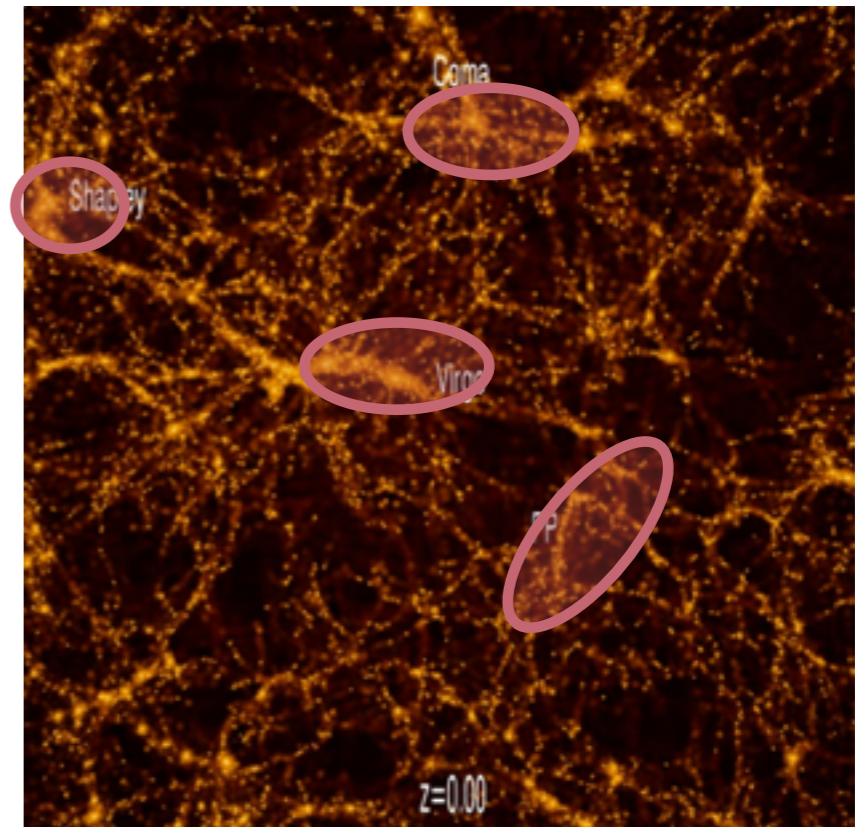
Note the fingers of gods



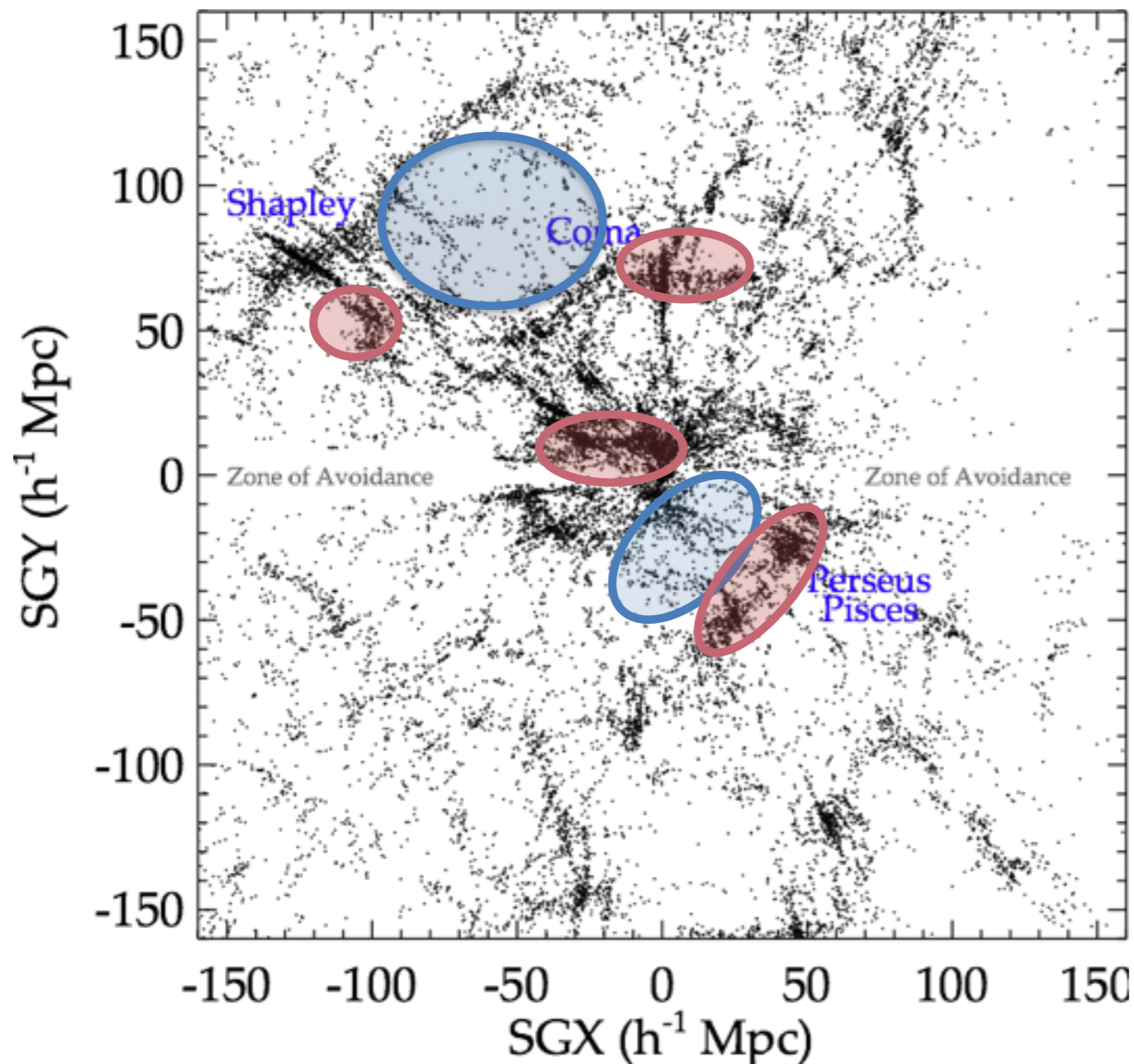
500 Mpc/h, 1024^3 particles,
DM only, Planck cosmology



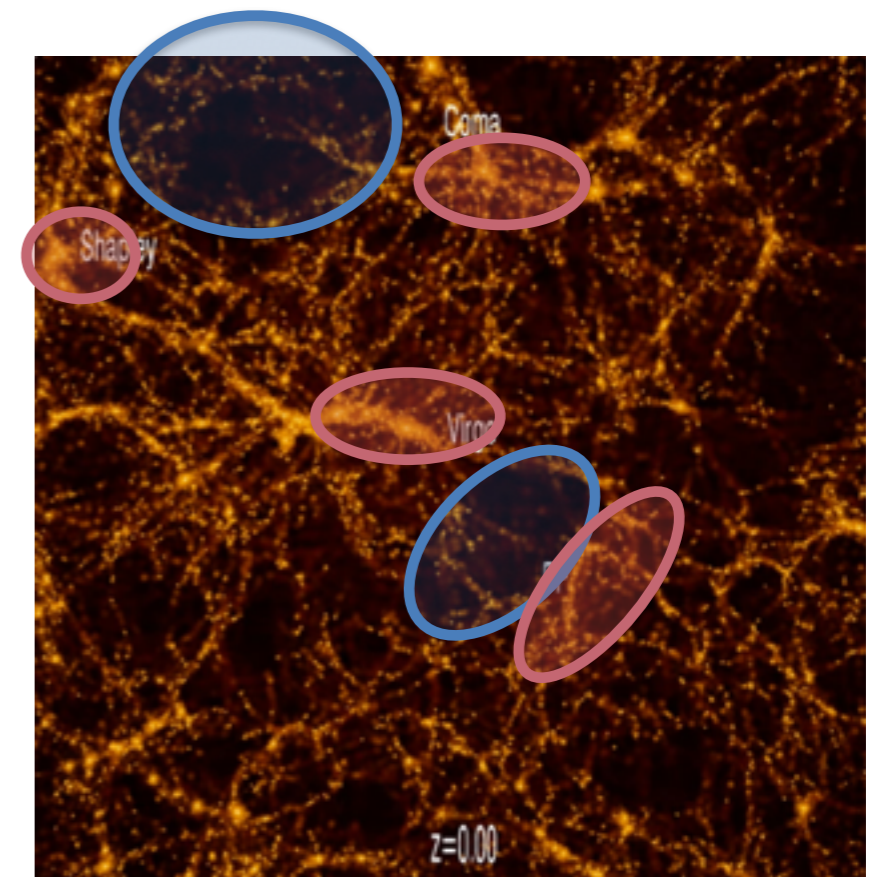
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500 Mpc/h, 1024^3 particles, DM only, Planck cosmology

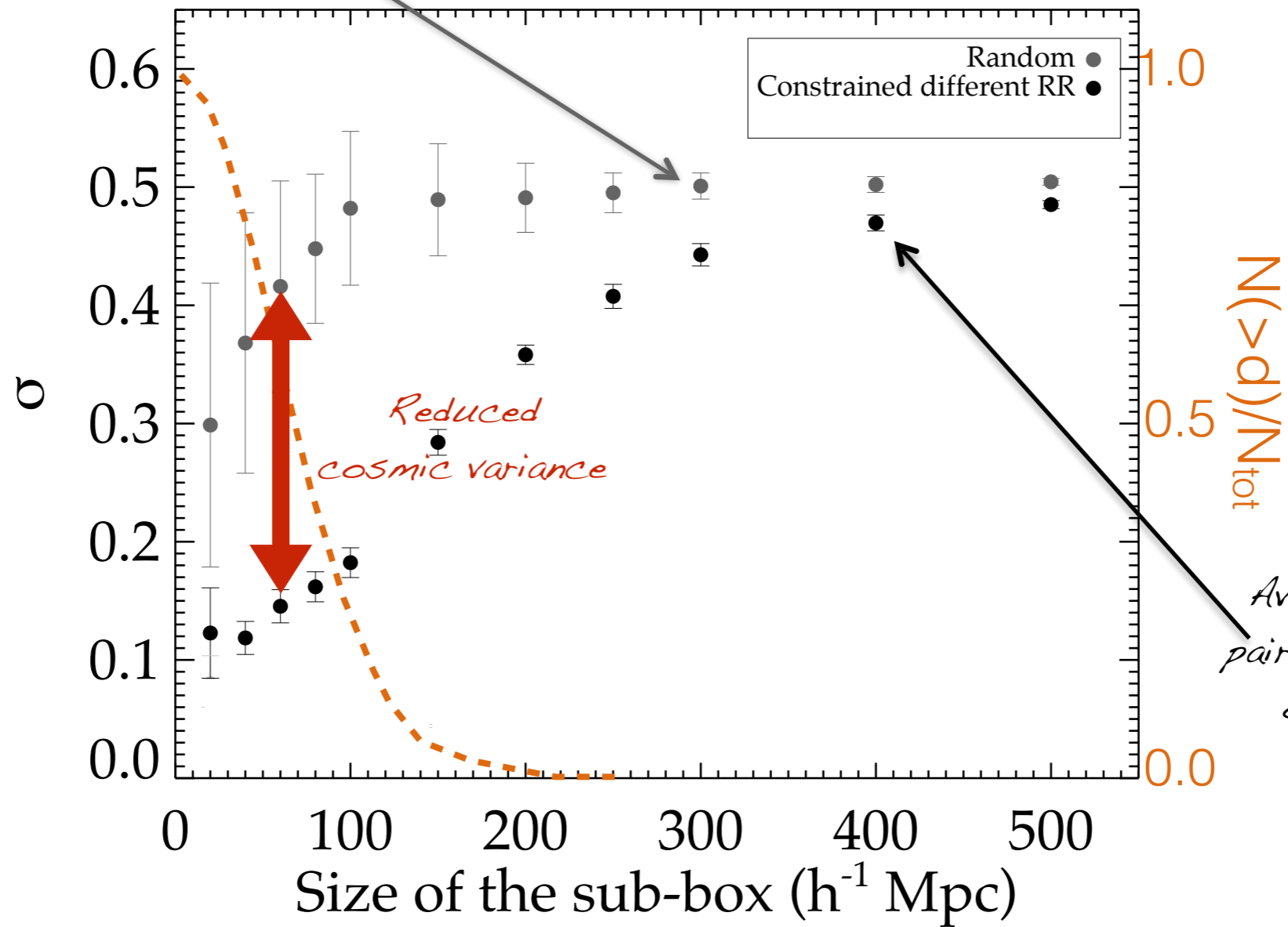


Note the fingers of gods

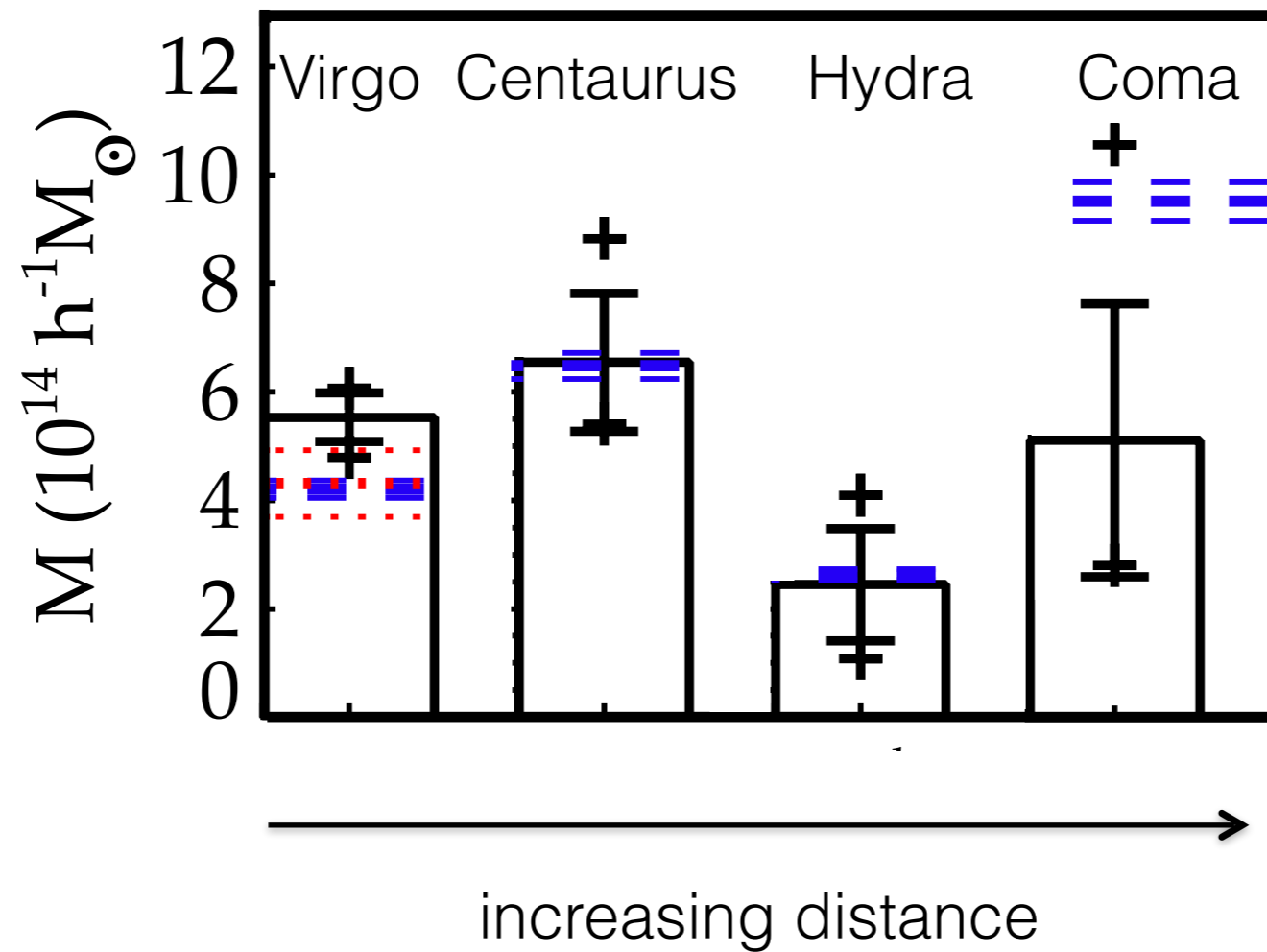


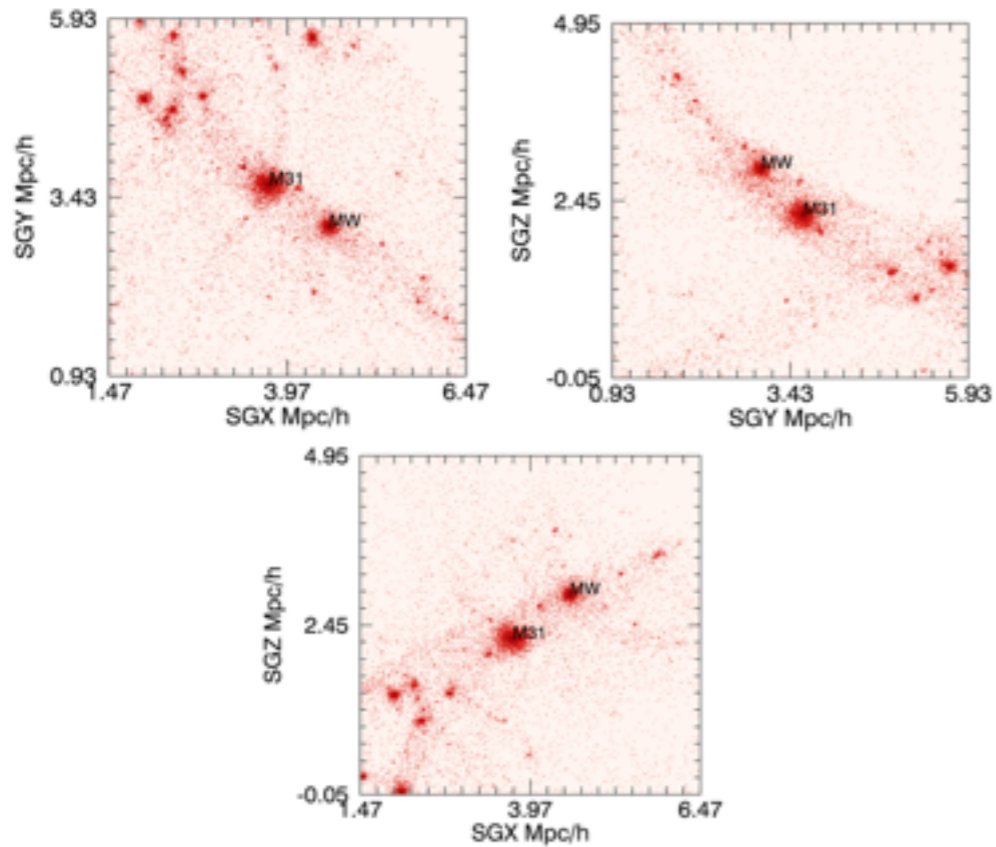
500 Mpc/h, 1024³ particles, DM only, Planck cosmology

Average variance between pairs of random fields of 300 Mpc/h aside



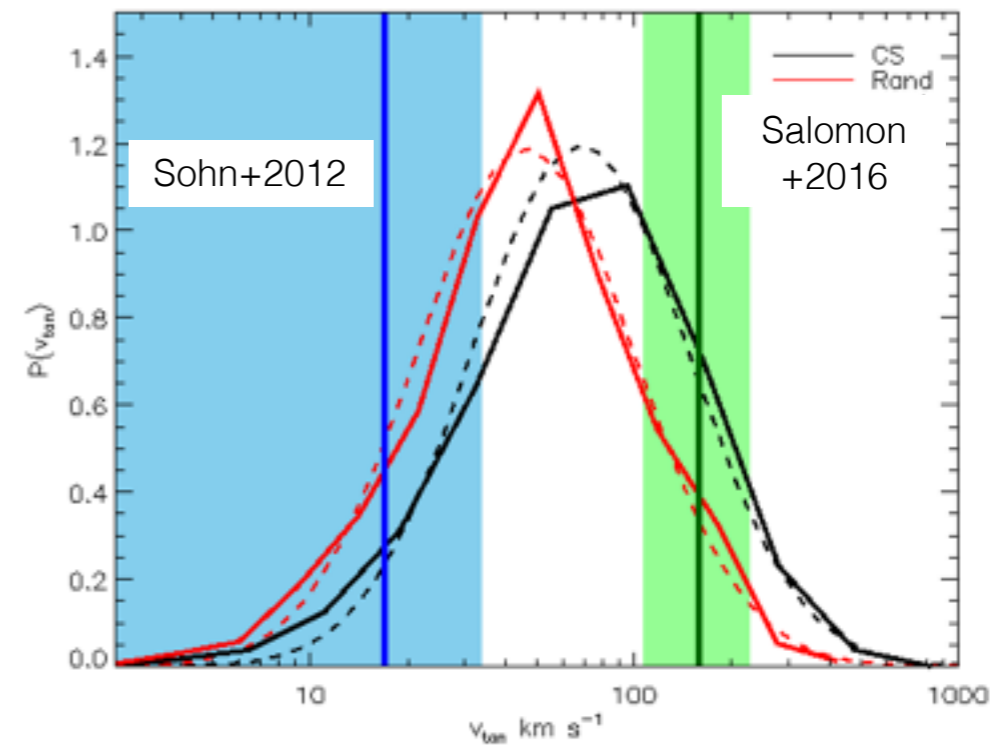
Dark matter halos = counterparts of observed local clusters





induced by the local environment,
not directly constrained
(non-linear scales)

An example of
application: in favor of a
higher tangential velocity



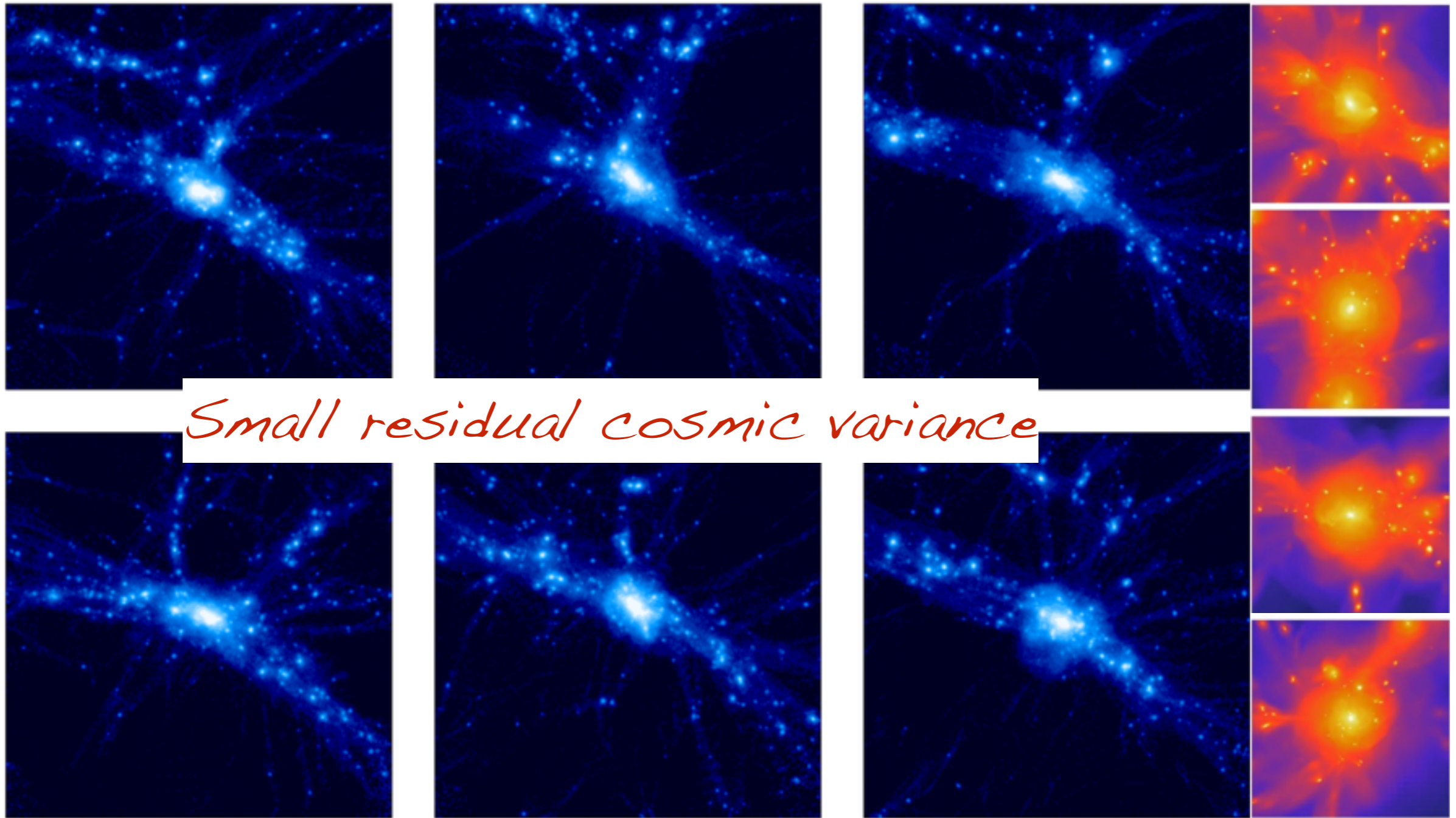
Carlesi,Sorce+2016
Carlesi,Hoffman,Sorce+2016
Carlesi,Hoffman,Sorce+2017

Let's dig into the Virgo cluster of galaxies

Observed Virgo, Simulated Virgo & Random clusters



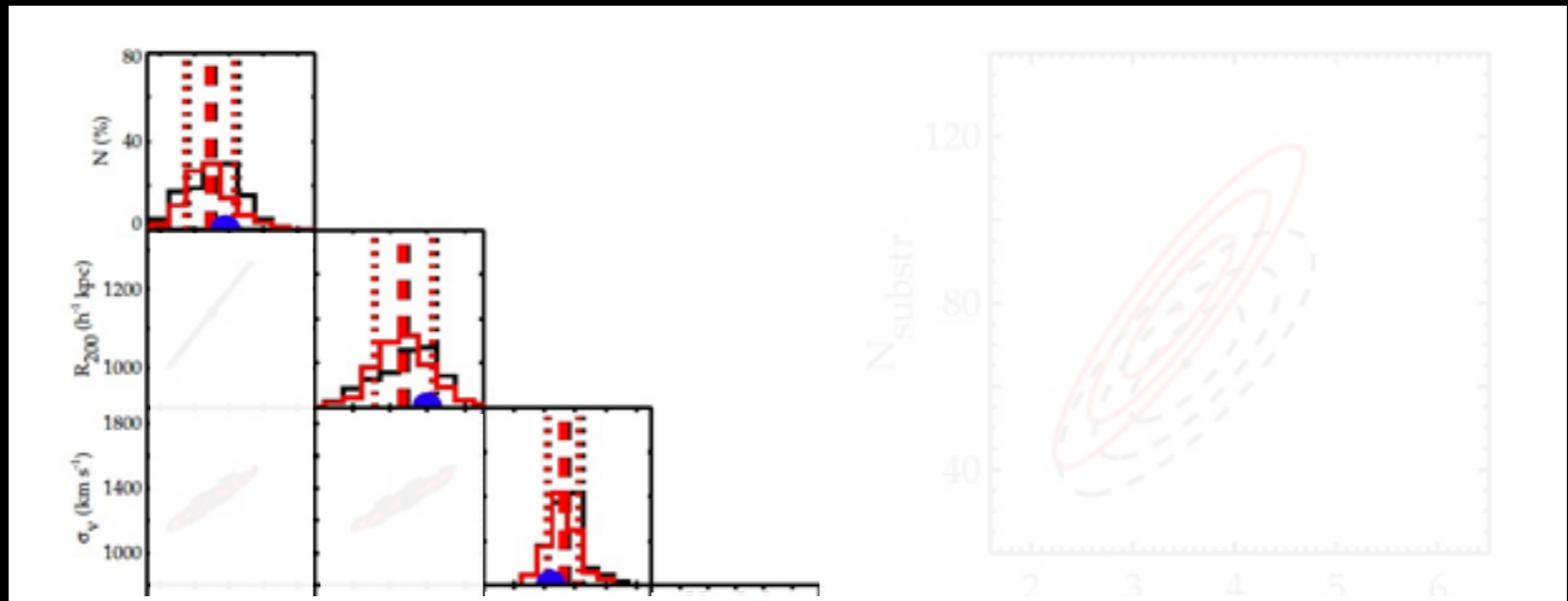
Let's dig into the Virgo cluster of galaxies



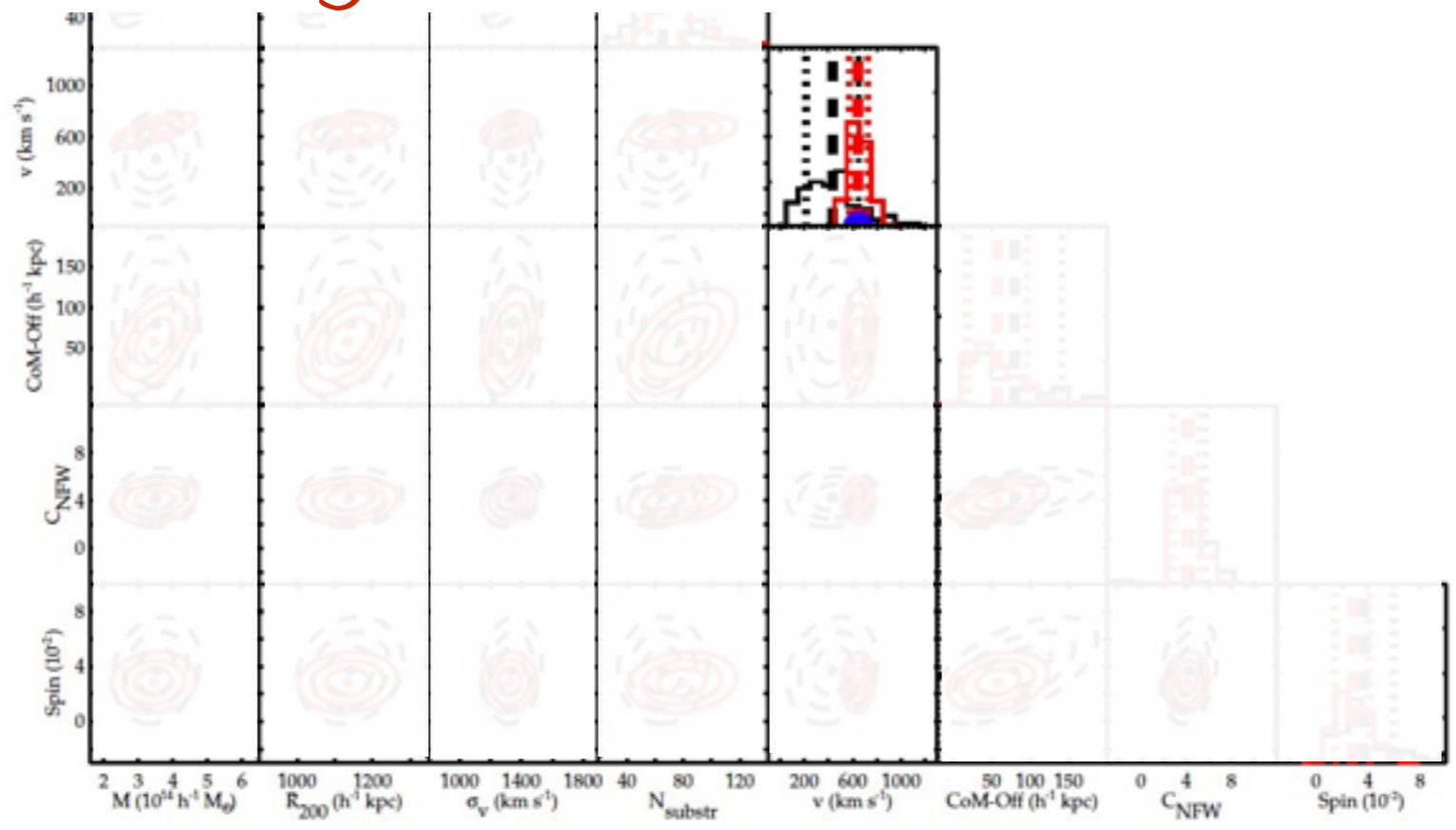
Rhapsody (Hahn +2017)

500 Mpc/h, 2048^3 particles effective (20 Mpc/h zoom), 3.8 kpc/h, DM only, Planck cosmology

Let's dig into the Virgo cluster of galaxies

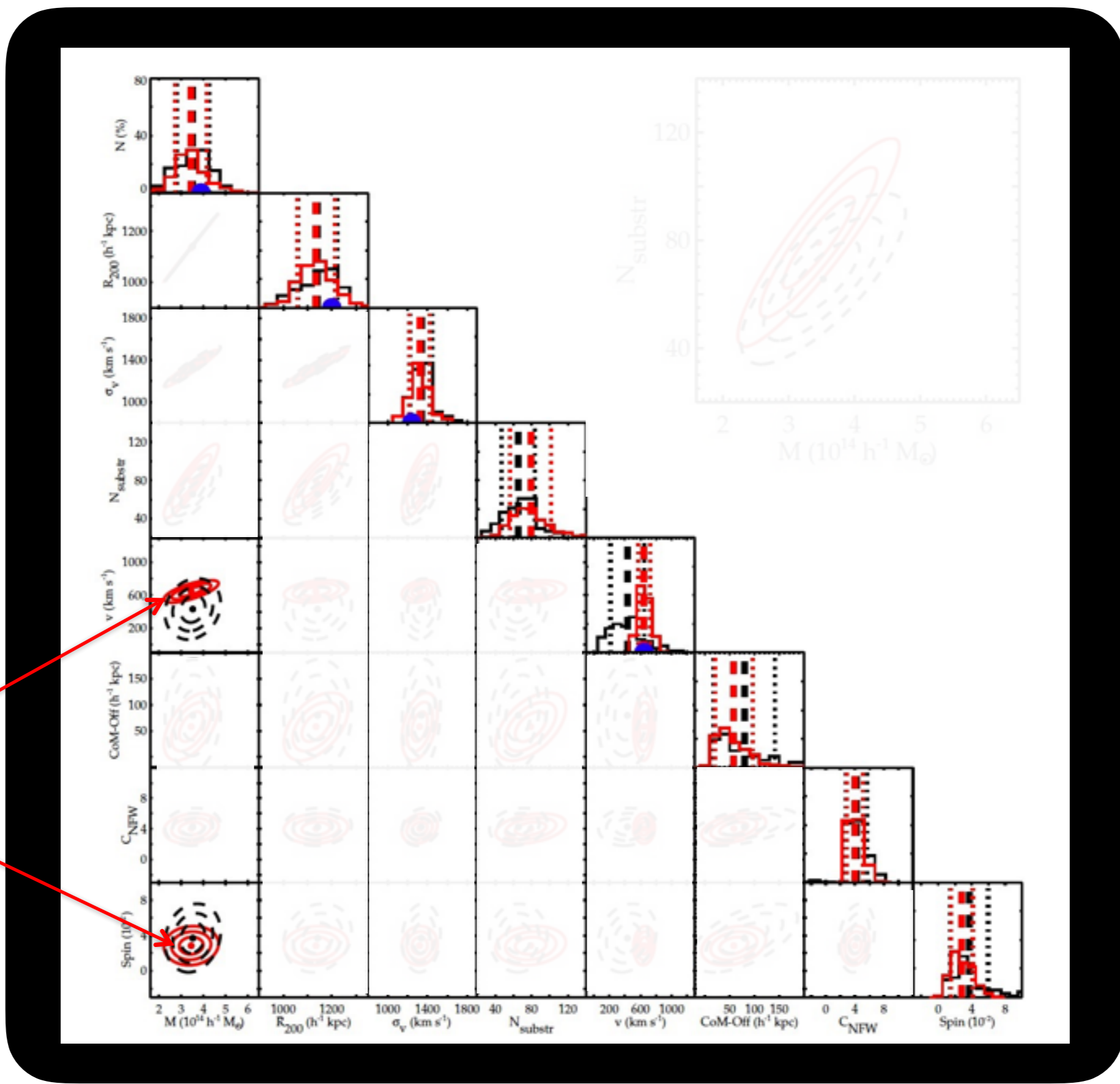


Overall agreement with observations



Sorce, Blaizot, Dubois submitted

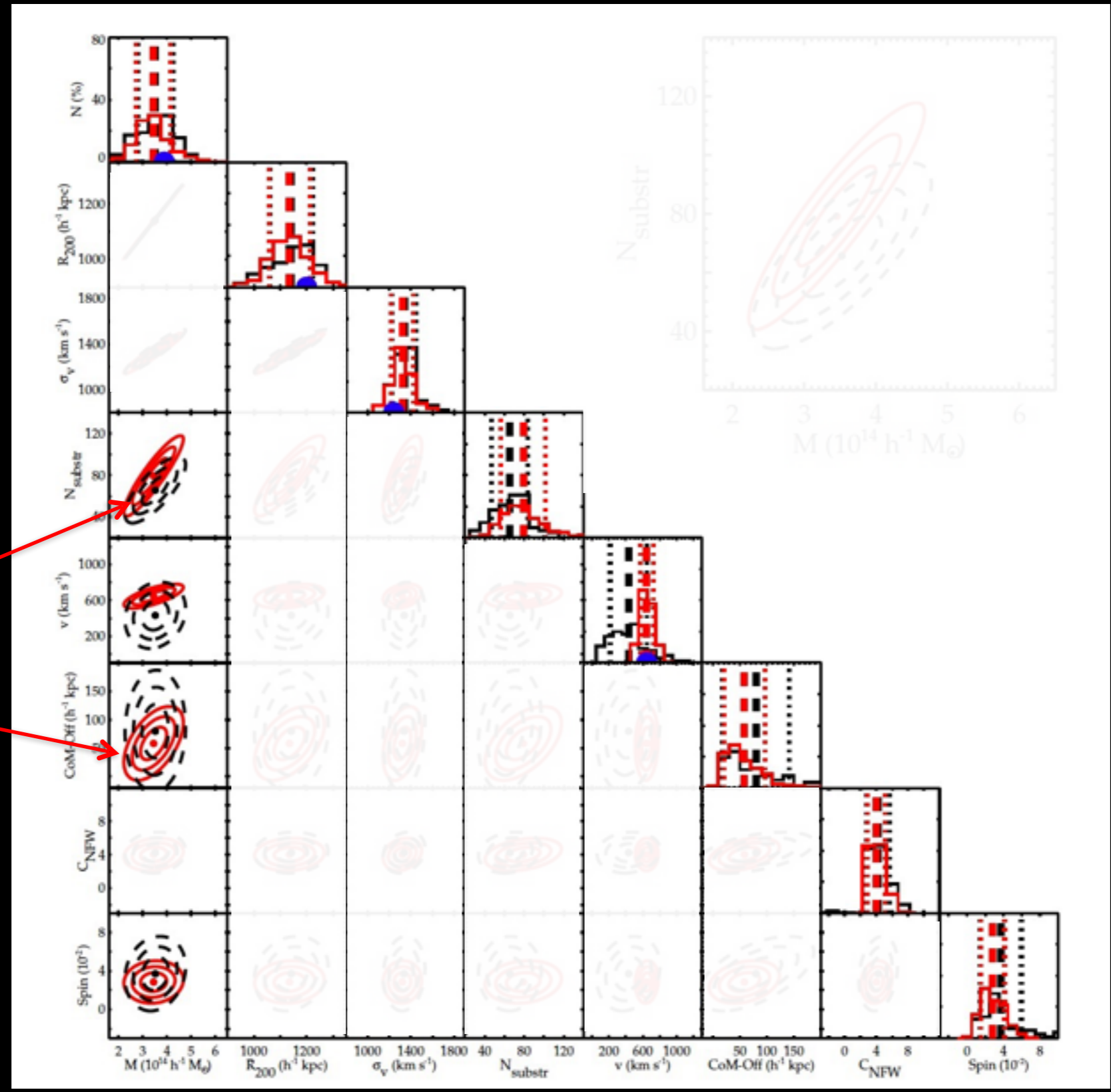
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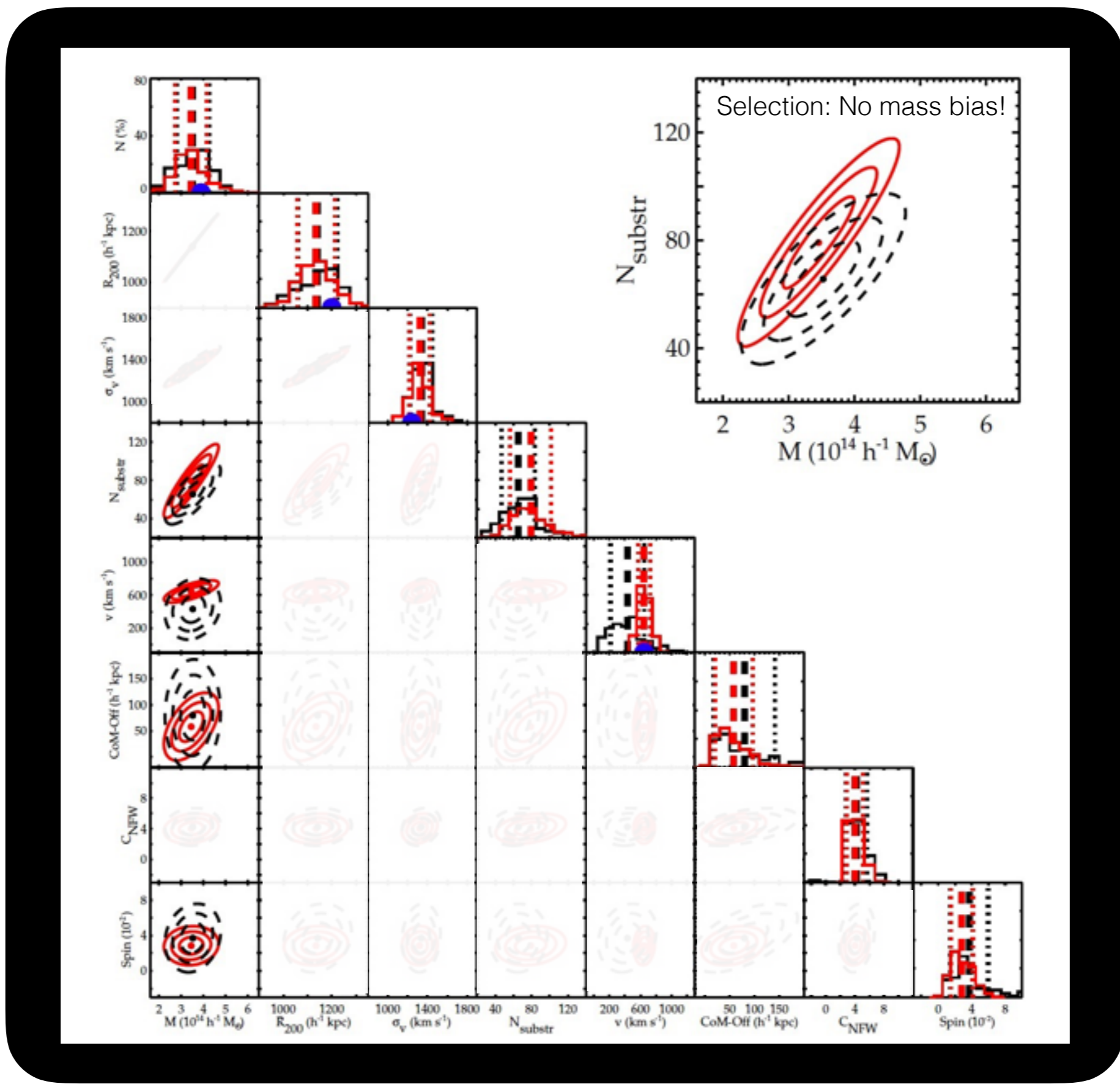
Let's dig into the Virgo cluster of galaxies

Number of substructures
 Center of mass offset wrt spherical center
 → History



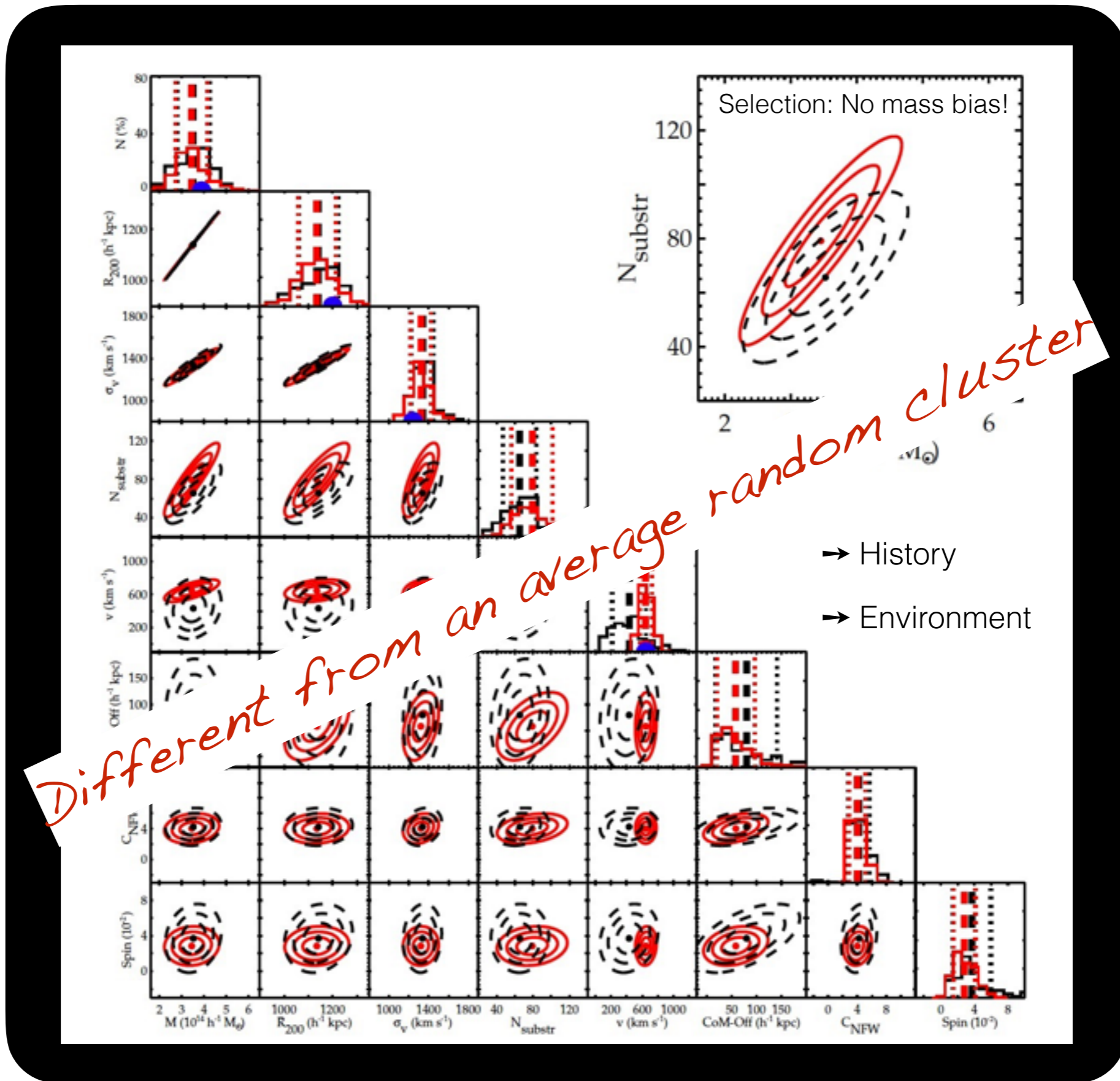
Sorce, Blaizot, Dubois submitted

Let's dig into the Virgo cluster of galaxies



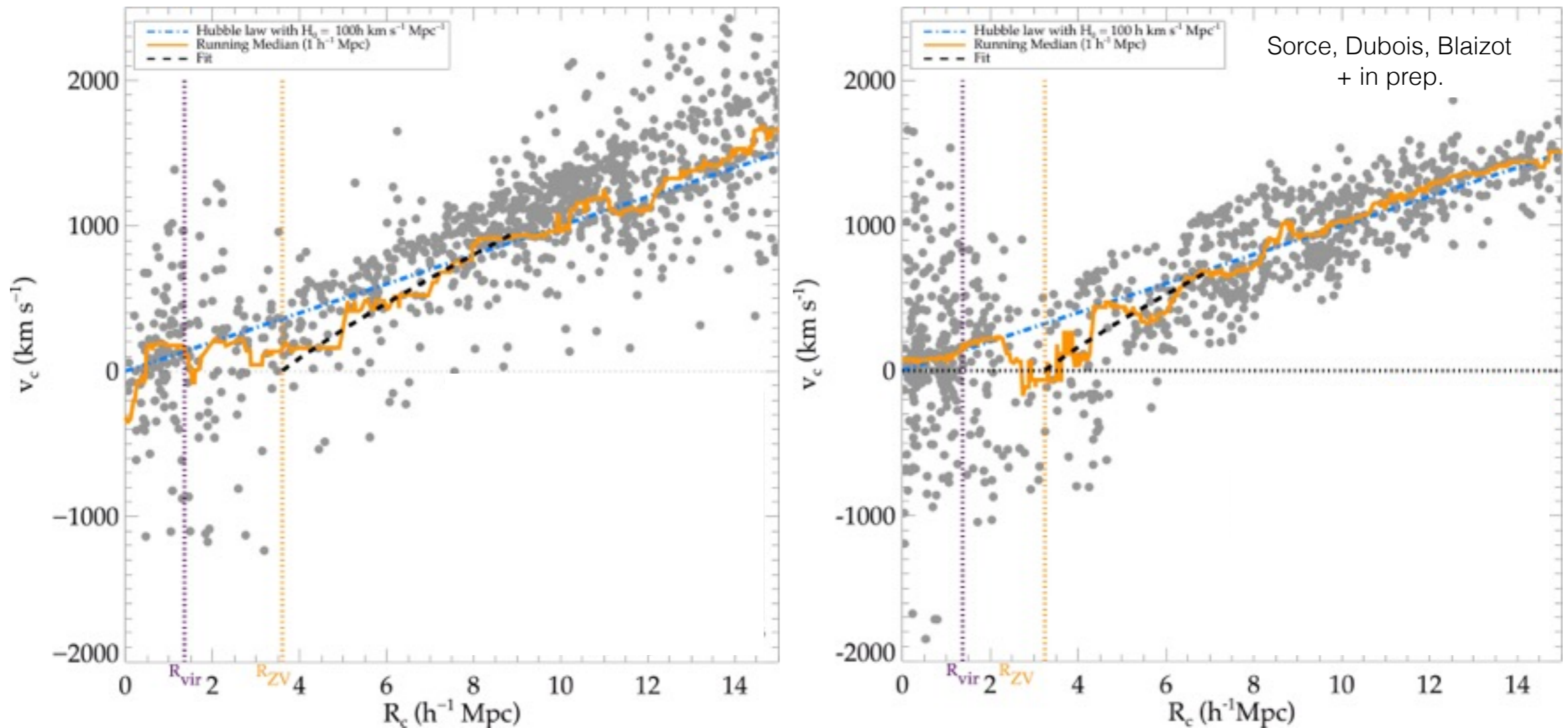
Sorce, Blaizot, Dubois submitted

Let's dig into the Virgo cluster of galaxies



Sorce, Blaizot, Dubois submitted

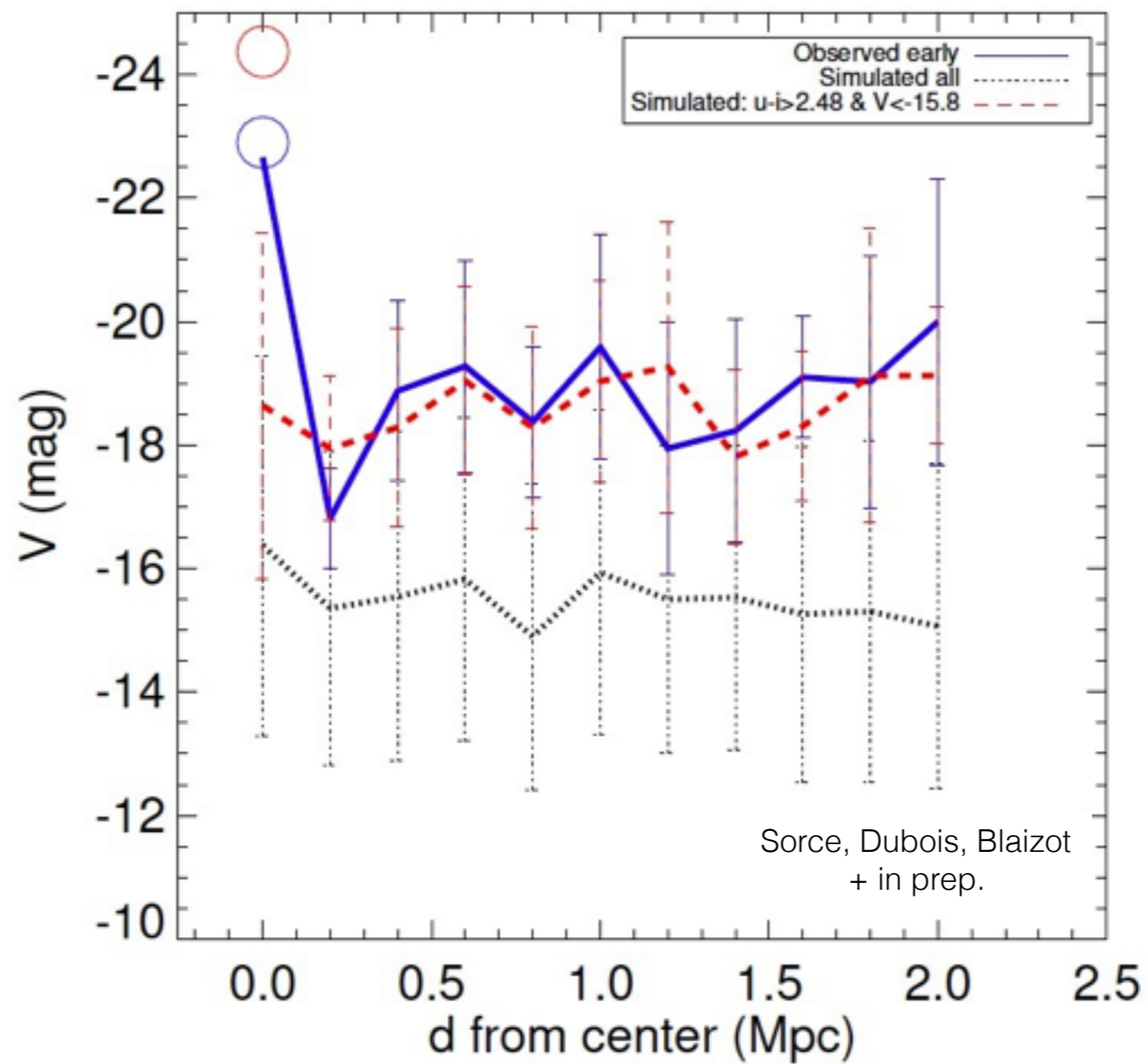
Let's dig into the Virgo cluster of galaxies



500 Mpc/h, 8192³ particles effective (20 Mpc/h zoom), 0.24 kpc/h hydrodynamics: SN and AGN feedback, Planck cosmology

Overall agreement with observations

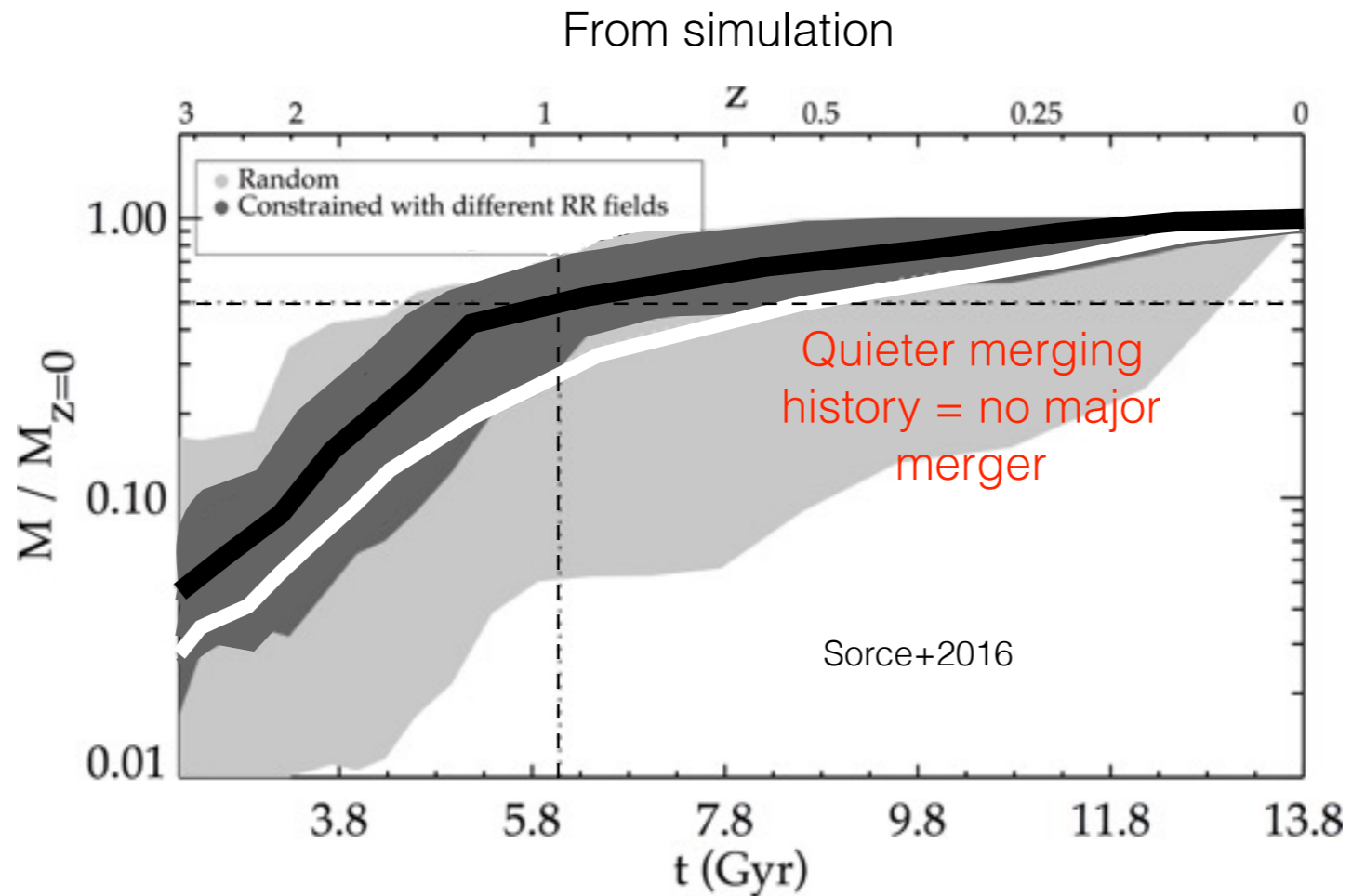
Let's dig into the Virgo cluster of galaxies



Overall agreement with observations

Let's dig into the Virgo cluster of galaxies

Boselli+2008,2014: from observation, only small mergers within the past few Gyrs



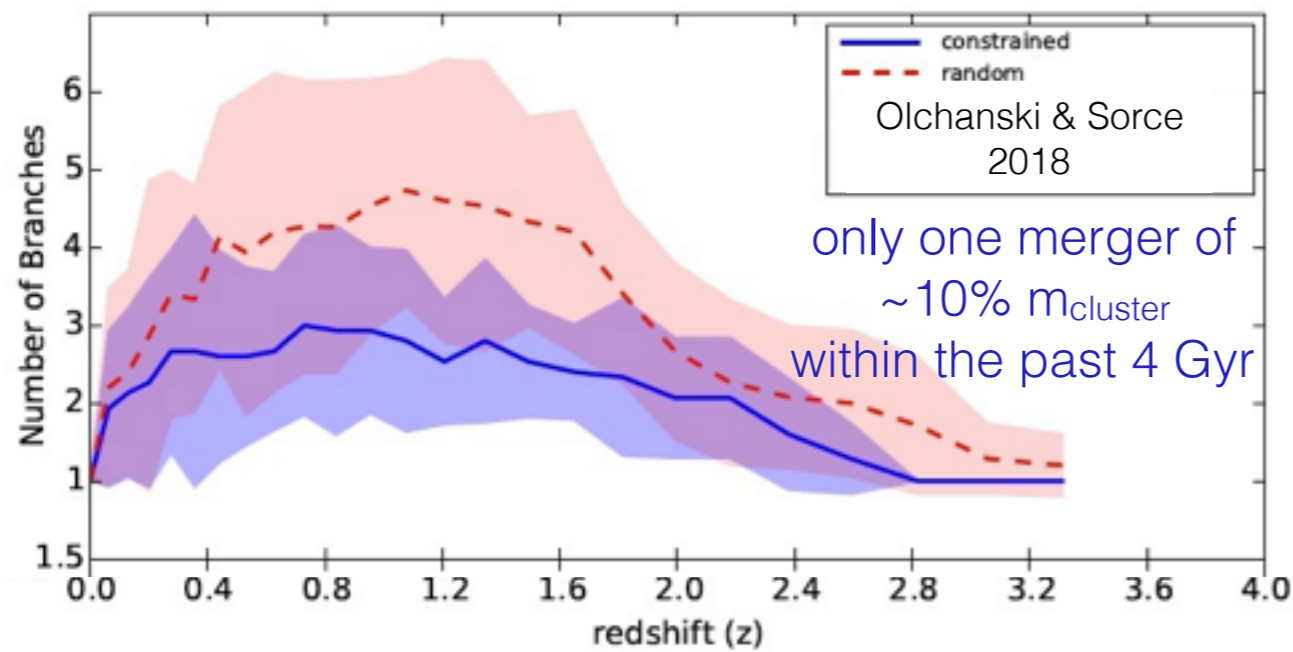
500 Mpc/h, 512^3 particles, DM only, Planck cosmology

Agreement with observational predictions

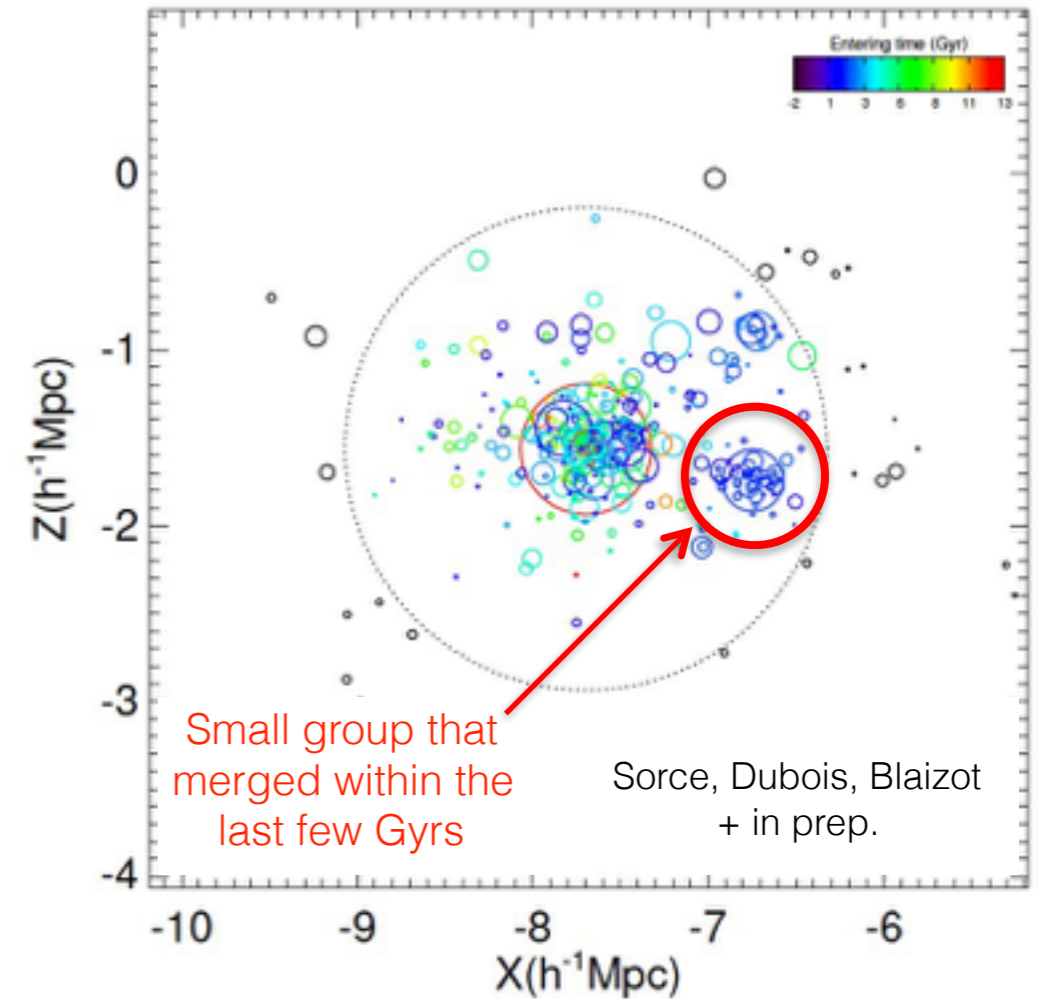
Let's dig into the Virgo cluster of galaxies

Lisker+2018: from observation, remnant of a group of $\sim 10\% m_{\text{cluster}}$ that infall 2-3 Gyr ago

From simulation



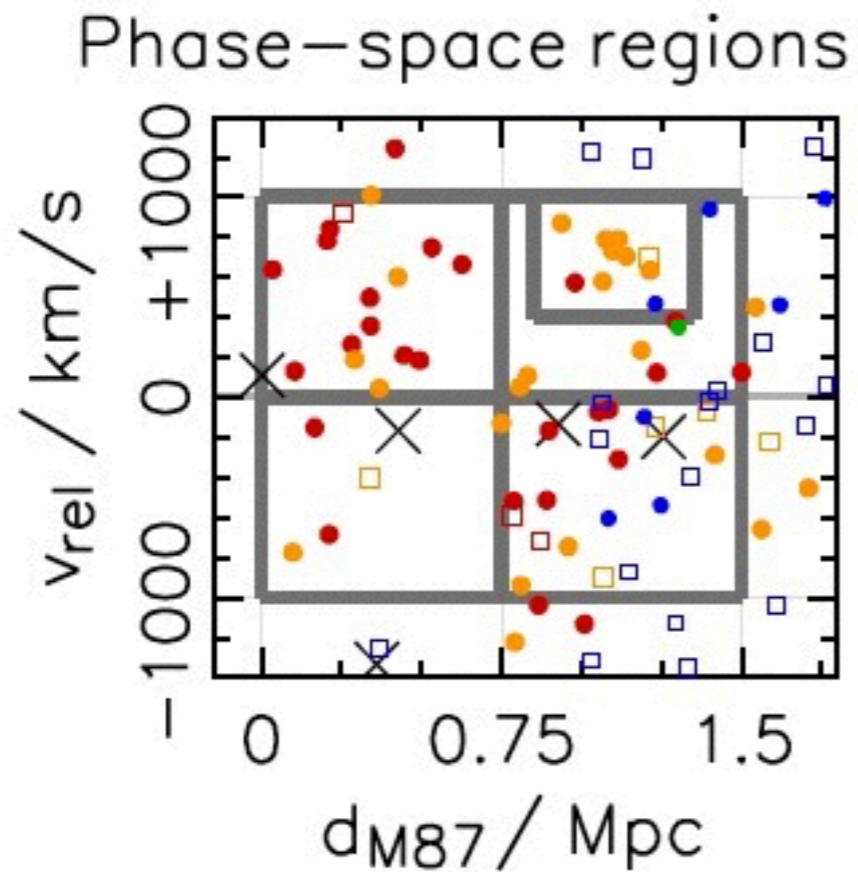
500 Mpc/h, 512^3 particles, DM only, Planck cosmology



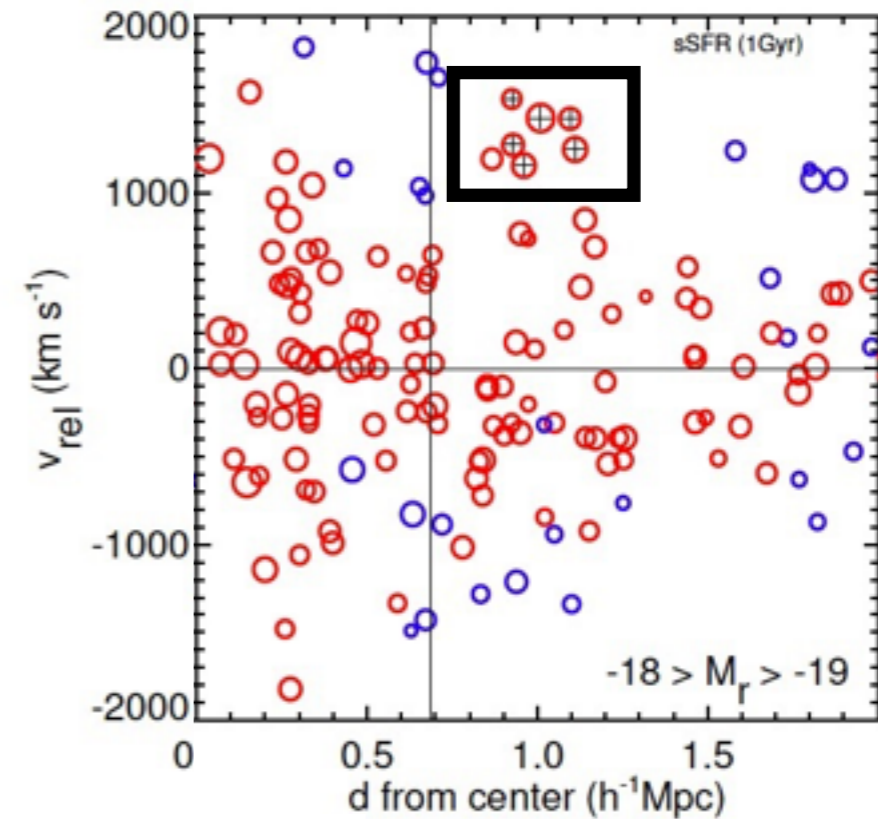
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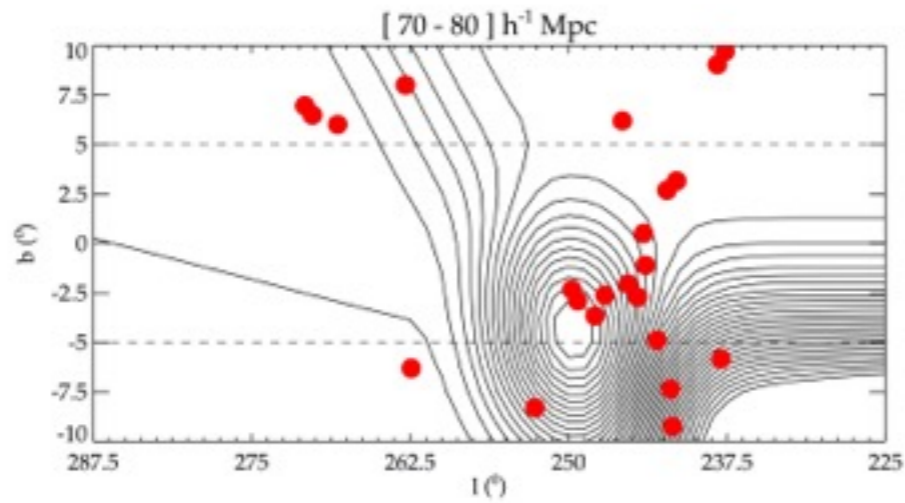


Lisker+2018



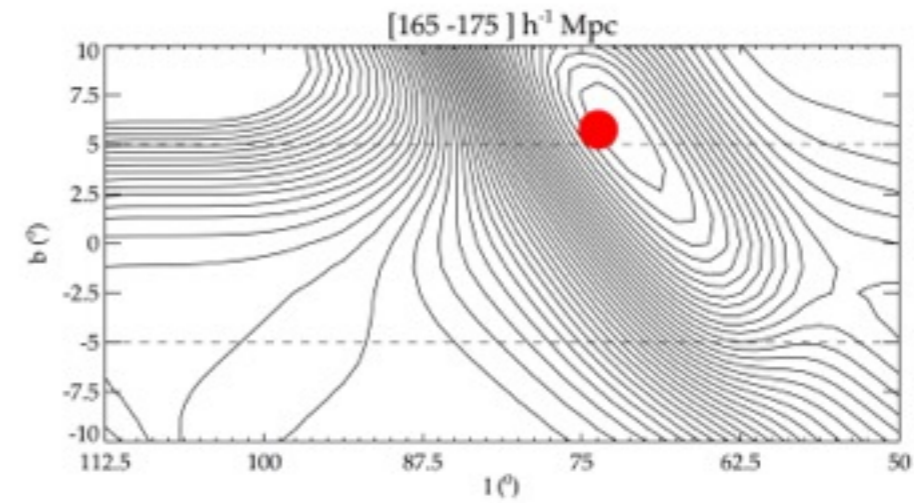
Sorce, Dubois, Blaizot
+ in prep.

Agreement with observational predictions



Puppis-3 Cluster

Chamaraux & Masnoux 2004

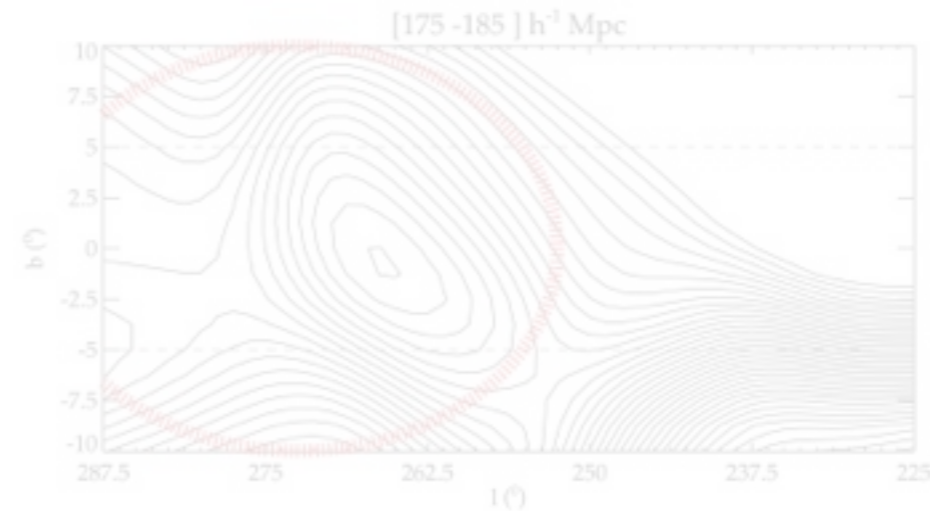


Cygnus A Cluster

Ebeling+2002

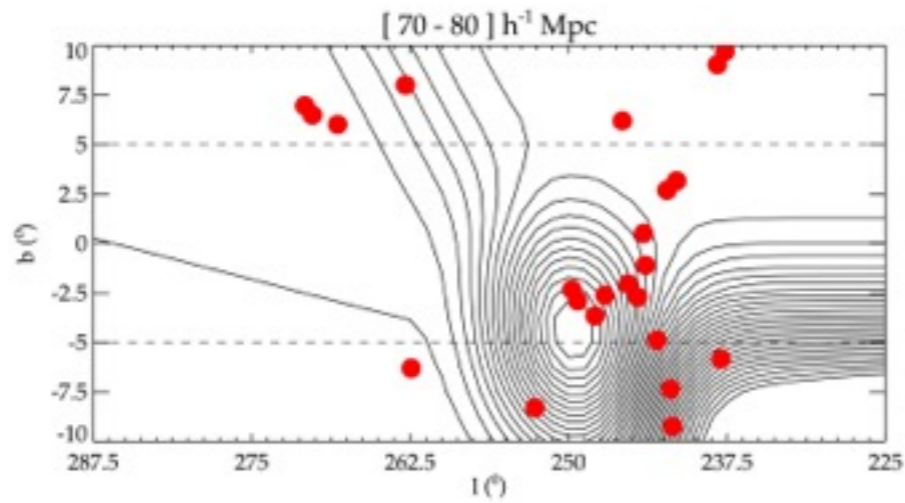
Λ CDM challenges hidden in the Zone of Avoidance?

- number of superclusters
- longest structures



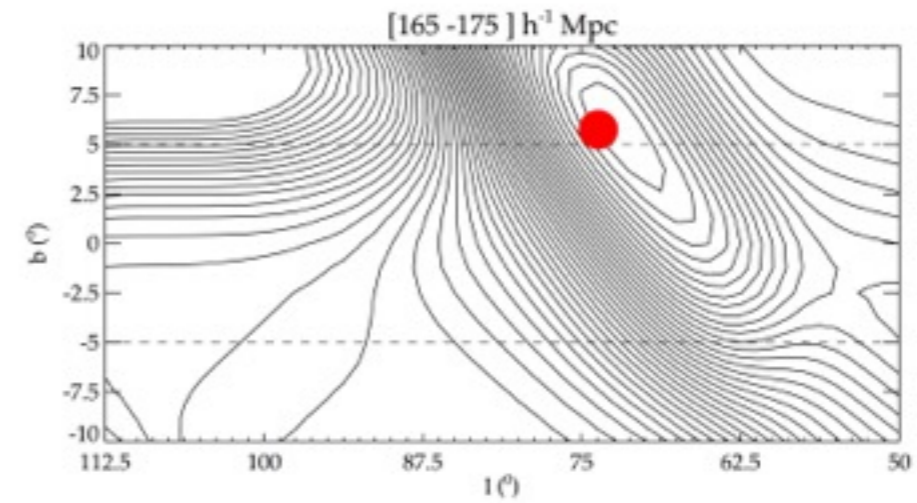
Vela Supercluster

Kraan-Korteweg+2017



Puppis-3 Cluster

Chamaraux & Masnoux 2004

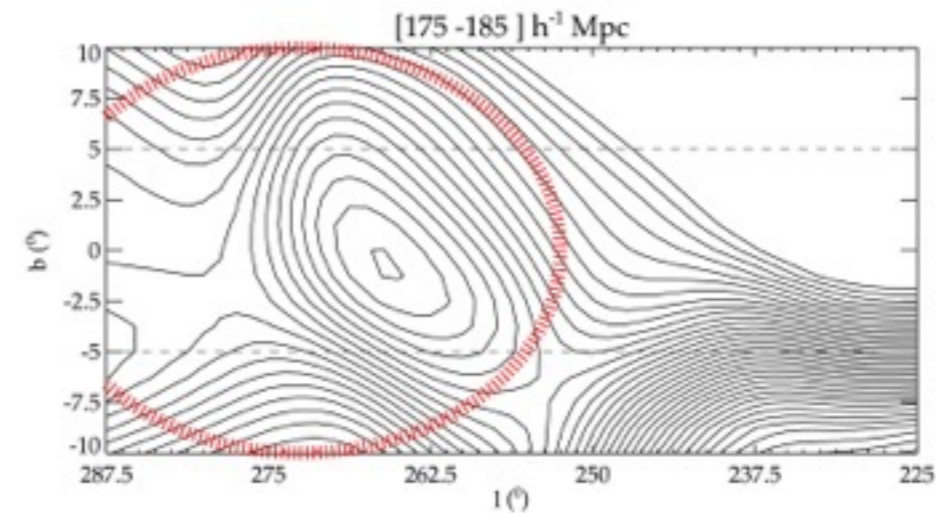


Cygnus A Cluster

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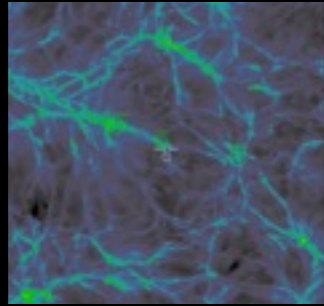
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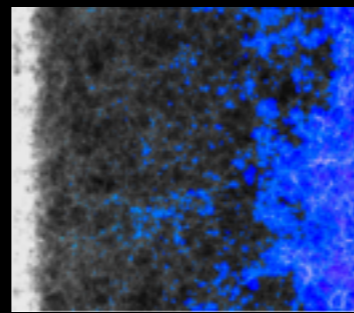


Vela Supercluster

Kraan-Korteweg+2017



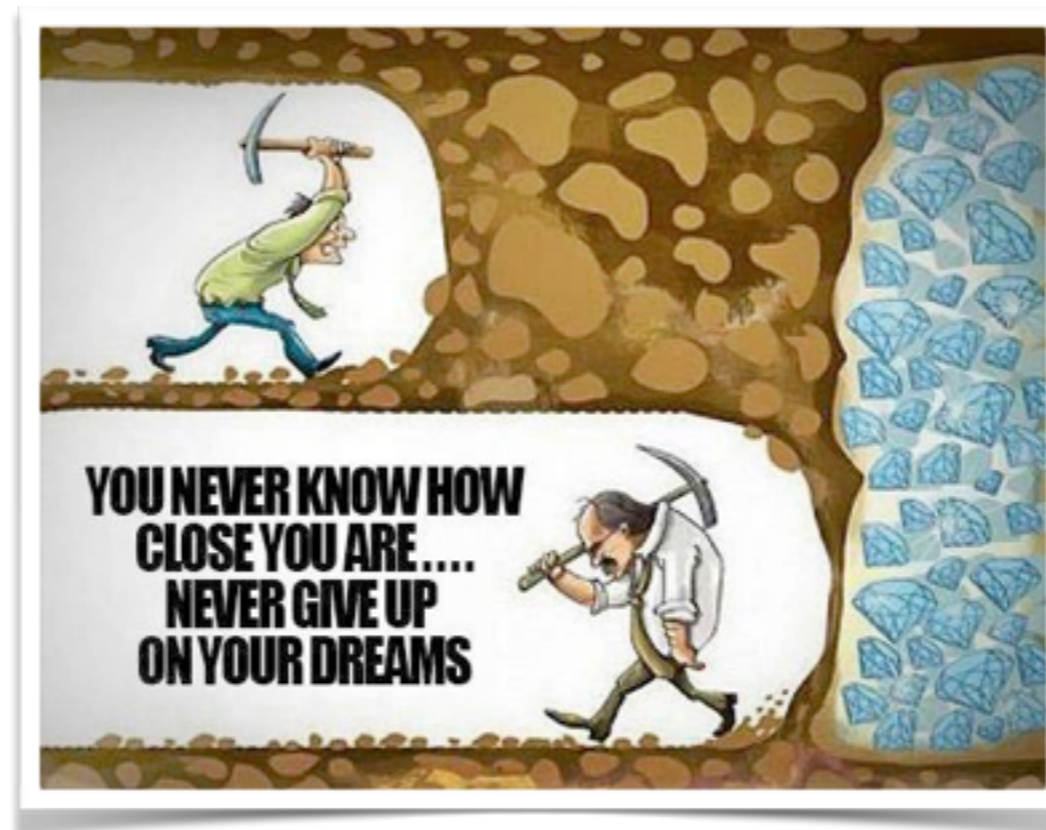
Cosmic Rays in the
local Universe
(Hackstein+2018)



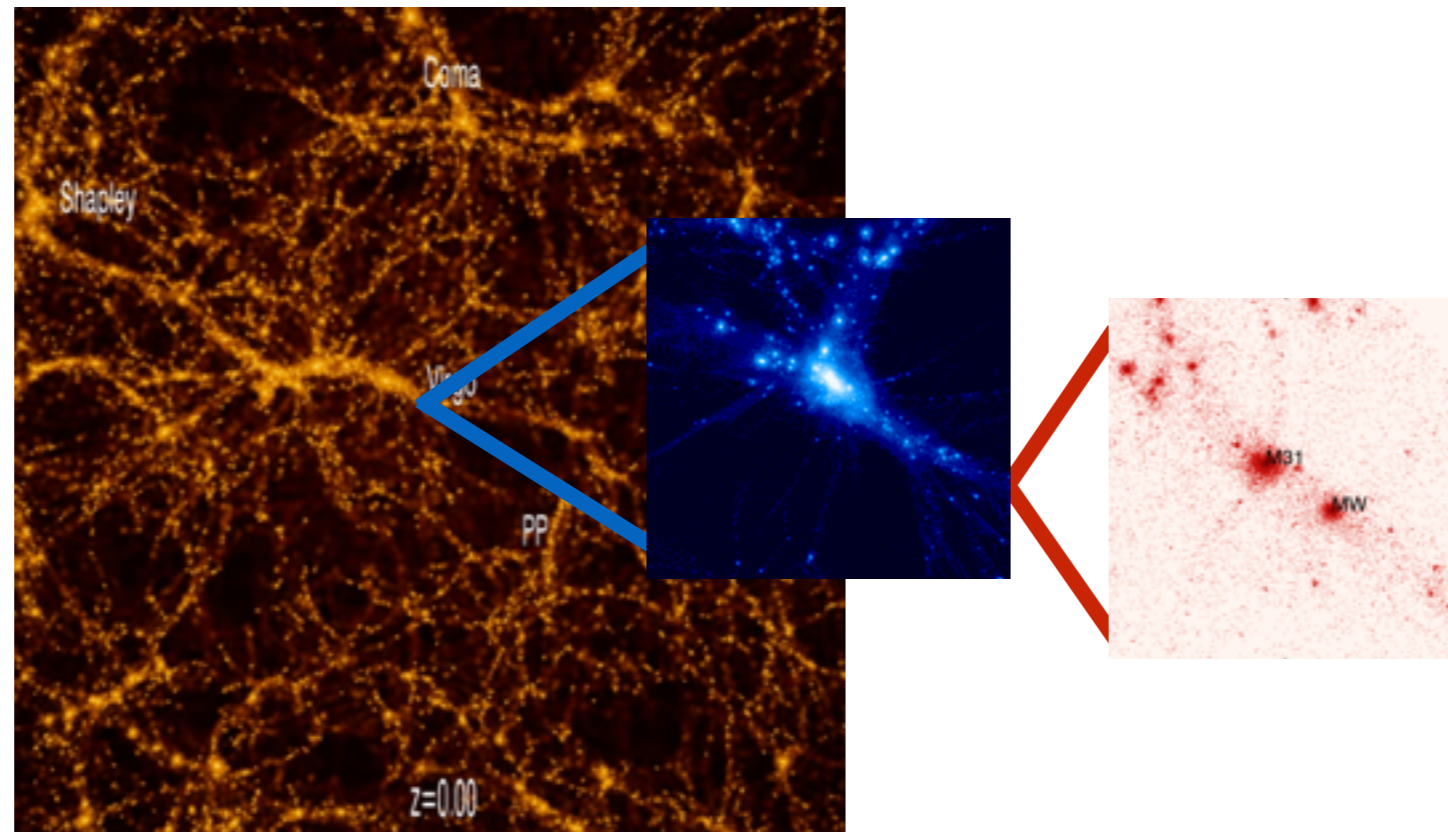
Reionization of the
local Universe
(Ocvirk+ submitted)
(Sorce+ in prep.)

and
more...

Summary: where do we stand?
How far have we come?



Summary of validity



Work	Constraints	large scales	cluster scales	local group scales
Kitaura2008,2012,2013 Hess+2013		☑	☑ no statistics	
Lavaux2010, Jasche+2013-tdy		☑		
Wang+2014-tdy		☑	☑ not nearby, no statistics	
Klypin+2003		☑	☑ mass 'by hand'	☑ induced
Sorce+2014-tdy		☑	☑	☑ induced

} luminosity bias !

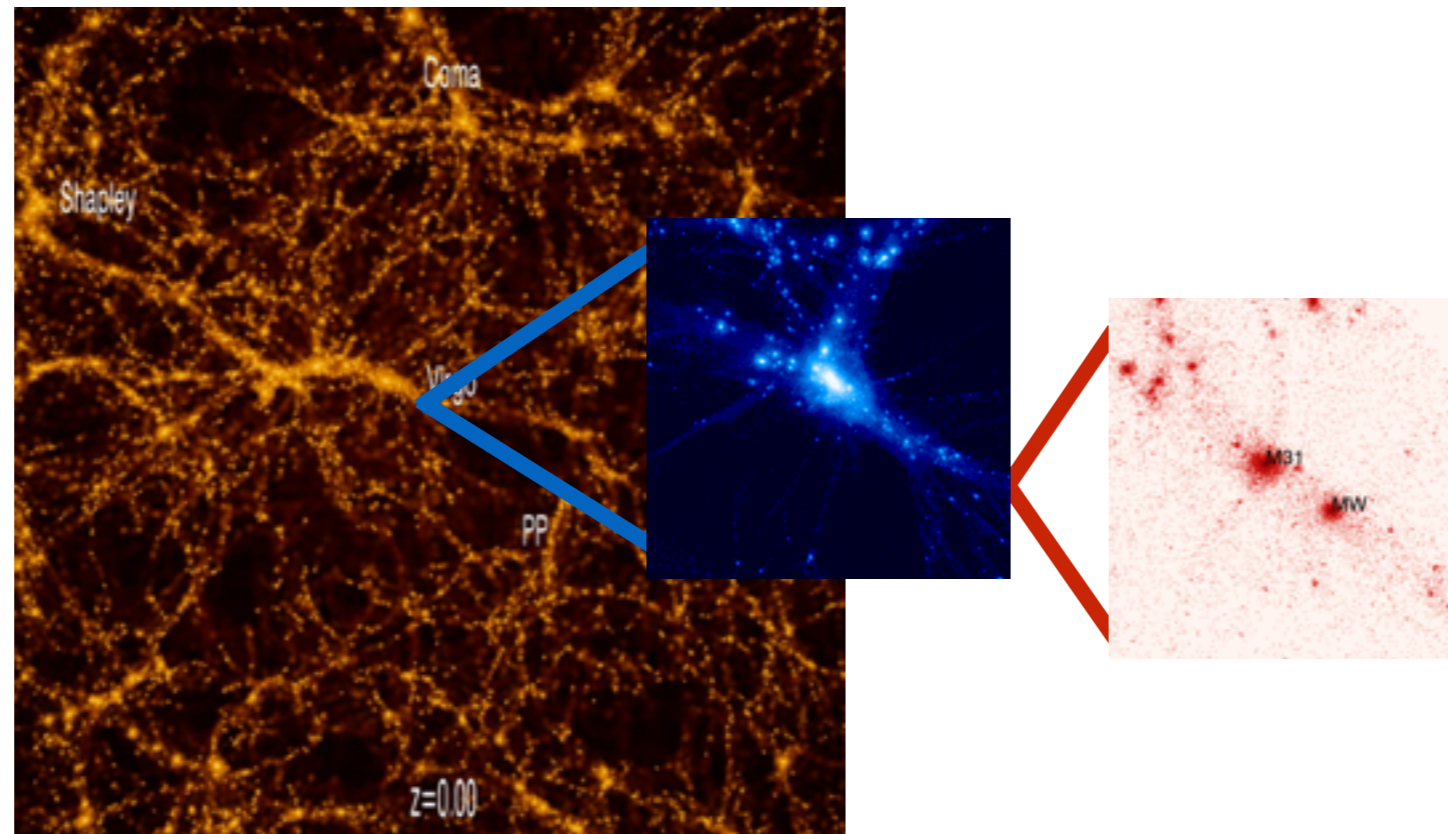
e.g. for the **Virgo cluster**
Sorce+2016b, Sorce
+submitted, Sorce+in
prep. **including the past
history!**

e.g. Carlesi,Sorce+2016
Carlesi,Hoffman,Sorce+2016
Carlesi,Hoffman,Sorce+2017

GM... What?



Summary and Prospectives



Work	Constraints	large scales	cluster scales	local group scales
Kitaura2008,2012,2013 Hess+2013		✓	✓ no statistics	
Lavaux2010, Jasche+2013-tdy		✓		
Wang+2014-tdy		✓	✓ not nearby, no statistics	
Klypin+2003		✓	✓ mass 'by hand'	✓ induced
Sorce+2014-tdy		✓	✓	✓ induced
GMO-CLONES		✓	✓	✓

} luminosity bias !
e.g. for the **Virgo cluster**
Sorce+2016b, Sorce
+submitted, Sorce+in
prep. **including the past
history!**

*Suite of constrained initial conditions of
different resolutions, sizes and focus*

e.g. Carlesi,Sorce+2016
Carlesi,Hoffman,Sorce+2016
Carlesi,Hoffman,Sorce+2017

Do we need a new cosmological model?

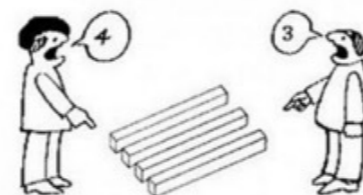
To answer, nowadays (this is on-going)

Small scales



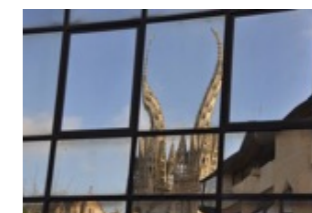
Simulations of
Galaxy formation
& evolution

Local scales



local estimates of
cosmological parameters

Large scales



CMB high sensitivity
experiment and large
scale surveys

**Biased Precision
Cosmology**



Do we need a new cosmological model?

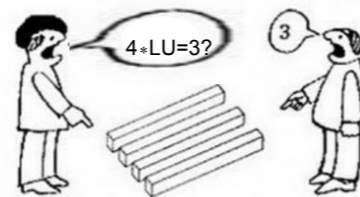
GMO-CLONES

initial conditions for
numerical specialists, theorists and observers

Small scales



Local scales



Large scales



Simulations of Galaxy formation & evolution:
- reproduction
- calibration

unbiased local estimates of cosmological parameters

CMB high sensitivity experiment and large scale surveys :
foreground effect correction

Accurate Precision Cosmology



Thank you, Merci, Grazie,
Gracias, Danke, **спасі́бо**,
Mahalo, 谢谢, **ありがとう**,
תודה, Obrigada, Dank u,
Tak, Cảm ơn, Dziękuję,
Kiitos, Aitäh, ...*

* Missing your 'thanks' spelling? It means I did not get the chance yet to visit your country but I am looking forward to do so !

(exceptions in red: I have not been but I have had the opportunity to learn how to say it)

